

**11.4-05** ANHARMONIC CONTRIBUTION TO DEBYE-WALLER FACTORS OF SOME HCP METALS. By P.D. Pathak, Physics Department, University School of Sciences, Ahmedabad 380 009, India, and R.J. Desai, Nanavati Hospital, Ville Parle (West), Bombay 400 056, India.

Debye-Waller factors of zinc, cadmium and magnesium are determined from room temperature up to about their melting points by X-ray diffraction using a specially designed furnace. For all the three metals, the Debye-Waller factor B is found to rise rapidly at higher temperatures. It is assumed that the deviations  $\Delta B$  from the extrapolated initial part of the curve is due to the contribution of higher order anharmonic terms in the potential energy function of the metals. It is shown for the first time that  $\Delta B$  or  $B(\text{anh})$  varies exponentially with  $1/T$ . When reduced values of B are plotted against reduced temperature, the points corresponding to all the three metals fall approximately on the same curve. Thus, the metals obey a "law of corresponding states". A common relation, applicable to all the three metals, between the total anharmonic contribution to B and the melting temperature is established.

**11.4-06** TEMPERATURE DEPENDENCE OF THERMAL MOTION IN CRYSTALLINE NAPHTHALENE AND ANTHRACENE. By C. P. Brock\* and J. D. Dunitz, Lab. für Organische Chemie, ETH-Zentrum, 8092 Zürich, Switzerland.

Although Cruickshank's classic study (*Acta Cryst.*, **9**, 1005 (1956)) of the thermal motion in crystalline naphthalene and anthracene was based on what are by present standards poor experimental data, the conclusions are still widely quoted. In the present study we attempt to provide better results for comparison with theoretical calculations.

Single-crystal data for naphthalene have been measured at five temperatures between 90 and 240°K. Positional and thermal parameters for C and H atoms at each temperature were refined by conventional least-squares techniques. The effect of varying the weighting scheme was examined. Contributions of internal molecular modes to the motions of the C atoms turn out to be important. They were estimated at each temperature from a standard force field and subtracted from the experimental Uij values. The corrected Uij's were then analyzed to determine rigid-body translational and librational tensors for the naphthalene molecule. The absolute magnitudes and temperature dependence of these quantities have been compared with values calculated from atom-atom potentials and from spectroscopic data.

An analogous study of the thermal motion in anthracene between 90 and 300°K is in progress.

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**11.5-01** ANALYSIS OF ERRORS IN QUANTITATIVE STUDIES OF DIFFUSE X-RAY SCATTERING. By T. B. Wu, E. Matsubara, and V. A. Kramb, Department of Material Science and Engineering, Technological Institute, Northwestern University, Evanston, IL 60201, USA.

Errors in separating the contributions of the diffuse x-ray scattering for binary solid solutions have been examined. The Georgopoulos-Cohen procedure was employed which divides the intensity due to displacements into several terms each involving a different atomic pair, as well as the short-range order intensity. A linear least-squares analysis was adopted to solve the intensity equations, from which an optimized solution and a standard deviation of each intensity component can be obtained. An error equation was derived and the standard deviations and the expected errors in the corresponding Fourier coefficients were evaluated. It was found that a large variation in the ratio of the scattering factors across the volume measured in reciprocal space improved the accuracy of the separation of the individual displacement intensity terms. For the case where one is concerned with the goodness of the separated displacement intensities, a shorter wavelength radiation, say molybdenum  $K\alpha$  radiation, is thus suggested. It was also found that weighting the intensity equation with respect to the counting error improved the separation. Although uncertain errors from Compton scattering and other sources still induce a significant error in the separated short-range order intensity, after Fourier inversion, error in the Warren SRO coefficients is quite low. Typical results will be shown. An attempt to extend this approach to ternary systems will be described.

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**11.5-02** ELECTROSTATIC INTERACTIONS INVOLVING CHARGED DISLOCATIONS AND IMPURITY IONS IN IONIC CRYSTALS. By A. S. Párasnis, Department of Physics, Indian Institute of Technology, Kanpur 208 016, India

We deal only with configurationally charged dislocations. Examples are: type A or C dislocation,  $b = (a/2)\langle 1\bar{1}0 \rangle$ , lying along  $\langle 11\bar{2} \rangle$  in crystals of NaCl structure; type A or C dislocation,  $b = (a/2)\langle 110 \rangle$ , lying along  $\langle 110 \rangle$  in crystals of  $\text{CaF}_2$  structure. Due to the excess electric energy thus acquired normally they do not exist. Some sort of neutralizing factors are required. For NaCl structure Párasnis *et al* (*Phil. Mag.* (1963) **8**, 1053) proposed, and found evidence for, substitutional replacement of alternate cations along the core of type A dislocation by aliovalent impurity ions; for  $\text{CaF}_2$  structure Evans and Pratt (*Phil. Mag.* (1969) **20**, 1213) proposed removal of alternate cations at the core of type C or of a row of anions at the core of type A dislocation.

Dislocations thus neutralized are more or less immobilized due to pinning by impurity ions or because of the need for indigenous ions to move along the core during glide. They participate in ordinary deformation not at all or with difficulty. It is suggested that there is a way for type A (or C) dislocation in NaCl structure to neutralize but still be mobile to some extent if the aliovalent impurity ions form an interstitial atmosphere around the charged core rather than go into substitutional sites at it. Appropriately small ions, e.g.  $\text{Au}^{3+}$  in MgO, could move along with the dislocation more easily now, especially at high enough temper-

atures. This glide will be in  $\{111\}$  planes which are normally not allowed.

It is further suggested that an individual  $\langle 112 \rangle$  dislocation in, for example,  $\text{MgO}+\text{Au}^{3+}$  would form an electrostatic dipole together with its ionic atmosphere. Consider a zigzag dislocation lying in  $\{1\bar{1}0\}$  and made of alternate  $\langle 112 \rangle$  and  $\langle 1\bar{1}\bar{2} \rangle$  segments of separation  $\ell$ . Since Bragg planes around dislocation cores are slightly bent this is equivalent to a chain of dipoles at slight angles  $\delta$  to one another, alternate dipoles being identically oriented. Now imagine a configuration such that zigs and zags are separated by a distance  $d$  parallel to  $b$ , each segment retaining its ionic atmosphere. The difference of energy between the "unseparated" and "separated" chains is calculated to be

$$\Delta E = 2\sqrt{2} (p^2/\ell^3) (d/\ell) \sin\delta \zeta(4)$$

where  $p$  is the macroscopic, averaged dipole moment of a single segment (zig or zag) and  $\zeta$  is Riemann zeta function.  $\Delta E$  is positive if  $\sin\delta$  is. This implies that the separation due to purely dipole-dipole interaction actually occurs for suitably oriented dipoles. Evidence that certain dislocation configurations observed in  $\text{MgO}+\text{Au}^{3+}$  by microscopy are consistent with this separation occurring has been obtained by G. Kameswara Rao (Thesis (1980) I. I. T. Kanpur; being published).

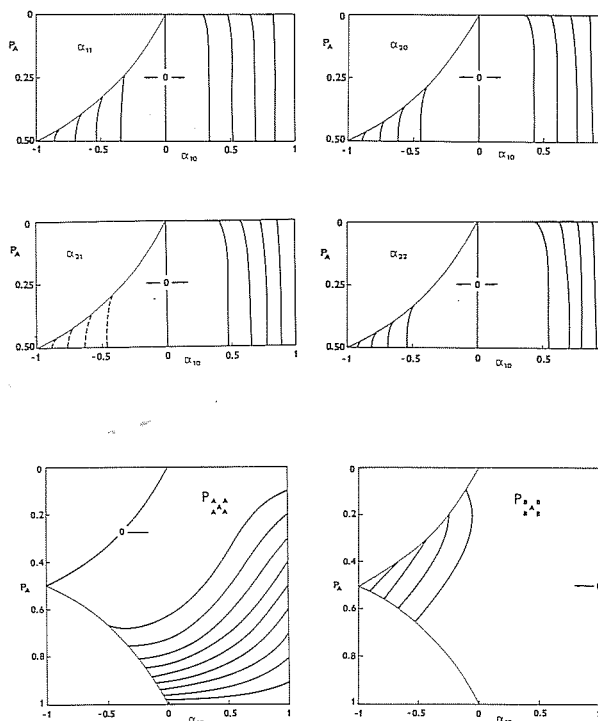
These ideas may be extended to other structures, *mutatis mutandis*.

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**11.5-03 EXACT RELATIONS FOR THE STRUCTURE OF SOLID SOLUTIONS FROM DIFFRACTION DATA.** M. Simerská and V. Syneček, Institute of Physics, Czechoslovak Academy of Sciences, 180 40 Praha 8, Na Slovance 2, Czechoslovakia.

Exact mathematical relations have been established revealing the structure of binary substitutional solid solutions in terms of local order parameters accessible directly from measured intensities of diffuse scattering. The relations are deduced from a general physical principle of the existence of the finite ranges of many-atom site interactions governing the interrelations of local order parameters. The Figures present the results obtained for the case of A and B atoms arranged on a square lattice with the nearest-neighbour site interactions only. The decrease of site correlations with the increase of interatomic vectors  $\vec{r}_{UV}$  is apparent from the contour maps of several local order parameters  $\alpha_{UV}$  ( $P_A$ ,  $\alpha_{10}$ ), where  $P_A$  is the fraction of A atoms. The contour maps of densities are given for clusters comprising an A atom with all like and with all unlike nearest neighbours. We can generally get the densities of clusters from a limited set of  $\alpha$ 's. Such a set permits to calculate all measured  $\alpha$ 's from relations corresponding to the existing ranges of site interactions. This allows to solve the many-body problem irrespective of the nature of atomic interactions.

Similar calculations for bcc, fcc, and hcp lattices as well as for the solid solution separation into coherent phases are in progress. The aim is to provide a real structure basis for the quantitative studies of physical properties of materials based on realistic many-body atomic interactions.



Contour lines: — positive, ---- negative; in 0.2 steps for  $\alpha_{UV}$ , in 0.1 steps for clusters.

**11.5-04 DETERMINATION OF CHARGE DISTRIBUTIONS NEAR VACANCY IN NbO.** By A. Aoki, K. Sato, M. Morinaga, Toyohashi University of Technology, Toyohashi 440 Japan J. Harada, Department of Applied Physics, Nagoya University, Chikusa-ku, Nagoya 464 Japan.

NbO has a defective structure, derived from the NaCl type cell by the ordered omission of 25 % of the ions on both cation and anion sublattices. These ordered vacancies affect charge distributions in NbO. In the present study integrated X-ray intensities of Bragg reflections were obtained from a single crystal of NbO (This crystal was grown by the arc-Czochralski method). The X-ray measurements were carried out at 188 K and 296 K, employing the monochromatic Mo K $\alpha$  radiation. About one hundred and thirty independent  $hkl$ 's were measured in the range of  $0.1 < \sin\theta/\lambda < 1.2 \text{ \AA}^{-1}$ . Both standard least-squares refinements and difference electron density synthesis techniques were used to examine the structure in detail. Extinction was remarkable. The R values after refinements were 1.3% for the result at 188 K and 2.0% for 296 K. In both temperatures the anisotropy of electron density at cation and anion sites near a vacancy was clearly observed. For instance, large positive electron density peak ( $2 e/\text{\AA}^3$ ) was present around a cation site near an anion vacancy. There was no indication that direct coupling between cation- and anion-vacancy exists in charge distributions. Also, broad electron distribution was found mainly in the Nb-Nb direction, whereas this trend was scarcely observed in the O-O direction. This may imply that the cation-cation overlapping bands are important for considering band scheme in NbO. These experimental results will be compared with the theoretical calculations by the DV-X $\alpha$  cluster method.