

**s1.m1.p1** Invariants of Automorphisms of the d-Dimensional Tori as a Criterion of Commensurability and Incommensurability of Crystal Structures. J. Warczewski, P. Gusin, *University of Silesia, Institute of Physics, Uniwersytecka 4, 40007 Katowice, Poland.*

Keywords: modulated structure, compaction of the (3+d)-dimensional space, automorphisms of the d-dimensional torus.

De Wolff<sup>1</sup> has described a crystal modulated structure in an appropriate (3+d)-dimensional superspace, where d – dimension of modulation. Such a structure is called a supercrystal. A real 3-dimensional modulated crystal can be dealt with as a result of compaction of d dimensions of (3+d)-dimensional superspace in which a supercrystal is embedded. As every particular atom is represented in superspace by a d-dimensional atomic surface, then after the compaction such an atomic surface becomes a d-dimensional torus. It turns out that invariants (e.g. number of rotations) of the automorphisms of such a torus are connected with the type of crystal modulation, namely for an incommensurately modulated structure the values of corresponding invariants are irrational, whereas for a commensurately modulated structure they are rational<sup>2</sup>.

**s1.m1.p2** Magnetic Modulated Structures in Terms of the Language of the Fibre Bundles. P. Gusin, J. Warczewski, *University of Silesia, Institute of Physics, Uniwersytecka 4, 40007 Katowice, Poland.*

Keywords: magnetic modulated structure, order parameter, fibre bundle.

A magnetic modulated structure can be described with the aid of the order parameter which reveals to be a section of a fibre bundle over  $\mathbf{R}^3$ . A magnetic structure is created as a result of a phase transition<sup>1</sup>. Such a phase transition can be investigated with the aid of a thermodynamic potential, whose arguments are: the order parameter and its covariant derivative, the latter being a generalization of an ordinary derivative. Because an order parameter makes a section of a bundle one has to introduce an additional structure called a connection<sup>2</sup>. Taking into account the above mentioned ideas we have obtained for the thermodynamic potential in the simplest form a sine-Gordon equation for the order parameter.

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