inorganic compounds

Caesium europium(III) polyphosphate, $CsEu(PO_3)_4$

Jing Zhu,[a]* Wen-Dan Cheng[b] and Hao Zhang[b]

[a]Department of Materials Science and Engineering, Yunnan University, Kunming, Yunnan 650091, People's Republic of China, and [b]State Key Laboratory of Structural Chemistry, Fujian Institute of Research on the Structure of Matter, Chinese Academy of Sciences, Fuzhou, Fujian 350002, People's Republic of China
Correspondence e-mail: jzhu@ynu.edu.cn

Caesium europium polyphosphate, $CsEu(PO_3)_4$, was synthesized by a high-temperature solution reaction. Its structure is charaterized by a three-dimensional framework made up of double PO_4 spiral chains and EuO_8 and CsO_{11} polyhedra.

Related literature

For the structures, properties and applications of condensed alkaline metal–rare earth polyphosphates with the general formula $MLn(PO_3)_4$ (M = alkali metal, Ln = rare earth metal), see: Chinn & Hong (1975); Ettis *et al.* (2003); Hong (1975); Koizumi (1976); Koizumi & Nakano (1978); Maksimova *et al.* (1982); Naïli & Mhiri (2005); Otsuka *et al.* (1977); Palkina *et al.* (1978); Rekik *et al.* (2004); Tsujimoto *et al.* (1977).

Experimental

Crystal data

$CsEu(PO_3)_4$	V = 997.09 (13) Å^3
M_r = 600.75	Z = 4
Monoclinic, $P2_1/n$	Mo $K\alpha$ radiation
a = 10.3571 (9) Å	μ = 10.60 mm^{-1}
b = 8.9615 (5) Å	T = 293 K
c = 11.1957 (8) Å	0.25 × 0.20 × 0.15 mm
β = 106.354 (3)°	

Data collection

Bruker P4 diffractometer	2185 reflections with $I > 2\sigma(I)$
Absorption correction: ψ-scan	R_{int} = 0.025
(*XSCANS*; Bruker, 1996)	3 standard reflections
T_{min} = 0.545, T_{max} = 1.000	every 97 reflections
7446 measured reflections	intensity decay: none
2284 independent reflections	

Refinement

$R[F^2 > 2\sigma(F^2)]$ = 0.019	164 parameters
$wR(F^2)$ = 0.048	$\Delta\rho_{max}$ = 1.16 e Å^{-3}
S = 1.00	$\Delta\rho_{min}$ = −1.17 e Å^{-3}
2284 reflections	

Data collection: *XSCANS* (Bruker, 1996); cell refinement: *XSCANS*; data reduction: *SHELXTL* (Sheldrick, 2008); program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *SHELXTL*; software used to prepare material for publication: *SHELXTL*.

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supporting information

Caesium europium(III) polyphosphate, CsEu(PO₃)₄

Jing Zhu, Wen-Dan Cheng and Hao Zhang

S1. Comment

Condensed alkaline metal-rare earth polyphosphates with the general formula $MLn(PO_3)_4$ (M = alkali metal, Ln = rare earth metal) possess various structures (Ettis *et al.*, 2003; Rekik *et al.*, 2004) and desirable optical properties (Chinn *et al.*, 1975; Otsuka *et al.*, 1977; Tsujimoto *et al.*, 1977; Hong *et al.*, 1975; Koizumi *et al.*, 1976). Furthermore, their chemical and thermal stability ensures the feasibility of the industrial applications. For this reason some polyphosphates (Naïli *et al.*, 2005; Palkina *et al.*, 1978; Maksimova *et al.*, 1982) were synthesized and investigated in the Cs–Ln–P–O system as an important potential. However, polyphosphates containing europium have not to date been fully explored in the system. Our exploration on the system afforded caesium europium polyphosphate $CsEu(PO_3)_4$. We report herein the synthesis and crystal structure of $CsEu(PO_3)_4$.

Crystallographic data and structural refinement of $CsEu(PO_3)_4$ are summarized in Table 1. The atomic coordinates and thermal parameters are listed in Table 2. Selected bond lengths and angles are given in Table 3.

The structure of crystal $CsEu(PO_3)_4$ is shown in Fig. 1. It belongs to the monoclinic space group $P2_1/n$, which is isostructural with $CsGd(PO_3)_4$ (Naïli *et al.*, 2005). The crystallographically distinct atoms of the asymmetric unit in the structure are one caesium, one europium, four phosphorus, and twelve oxygen atoms. It is described as a three-dimensional framework made up from double PO_4 spiral chains and Cs- and Eu-polyhedra. As illustrated in Fig. 2, the double PO_4 spiral chains have the same repeating unit (eight PO_4 tetrahedra) as single one of $CsNd(PO_3)_4$ (Koizumi *et al.*, 1978). These spiral chains are linked by EuO_8 and CsO_{11} polyhedra. In addition, comparing with $CsNd(PO_3)_4$, the different characteristics are noted in the coordination environments of the cations. The Eu cation is eight-coordinated with the Eu—O band distances ranging from 2.344 (3) to 2.471 (3) Å. Each EuO_8 polyhedron is corner- and face-connected with two and two CsO_{11} polyhedra, respectively (Fig. 3). The isolation of EuO_8 polyhedra gives rise to the large Eu—Eu distances, the shortest of which is 5.7415 (3) Å. The Cs cation is coordinated by eleven oxygen atoms, and the large range of the Cs—O bond distances implies that CsO_{11} polyhedra are distorted. Neighboring two CsO_{11} polyhedra are linked by corner-sharing (Fig. 4).

S2. Experimental

The title compound was prepared by the high temperature solution reaction, using analytical reagents Cs_2CO_3, Eu_2O_3, and $NH_4H_2PO_4$ in the molar ratio of Cs/Eu/P = 7:1:12. Starting mixtures were finely ground in an agate mortar to ensure the best homogeneity and reactivity, then placed in a platinum crucible and heated at 373 K for 4 h. Afterwards, the mixtures were reground and heated to 973 K for 24 h. Finally, the temperature was cooled to 773 K at a rate of 2 K/h and air-quenched to room temperature. A few colorless and block-shaped crystals were obtained from the melt of the mixture.

S3. Refinement

A single-crystal of the compound was selected for X-ray Diffraction determination. The structure was solved using direct methods and refined on F2 by the full-matrix least-squares method with the *SHELXL97* program package (Sheldrick, 2008). The position of the Eu atom was refined by the application of the direct method, and the remaining atoms were located in succeeding difference Fourier synthesis. In order to confirm the chemical composition of the the the compound, the single-crystal investigated on the diffractometer was analyzed by Energy-dispersive X-ray spectrometry (EDX) using a JSM6700F scanning electron microscope. The obtained result is in good agreement with that obtained by the refinement of the crystal structure. No impurity elements have been detected.
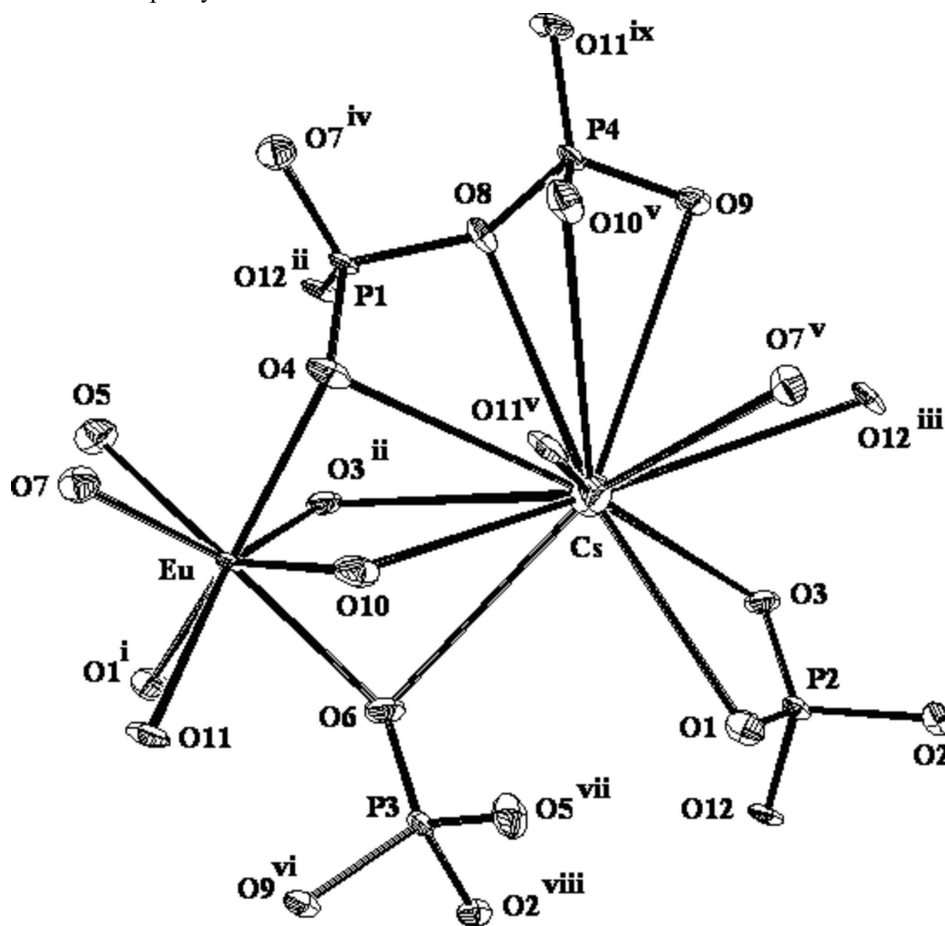
Figure 1

Displacement ellipsoid plot (50% probability) of CsEu(PO₃)₄.

Caesium europium(III) polyphosphate

Crystal data

CsEu(PO₃)₄	$\beta = 106.354\,(3)°$
$M_r = 600.75$	$V = 997.09\,(13)$ Å³
Monoclinic, $P2_1/n$	$Z = 4$
Hall symbol: -P 2yn	$F(000) = 1096$
$a = 10.3571\,(9)$ Å	$D_x = 4.002$ Mg m⁻³
$b = 8.9615\,(5)$ Å	Mo $K\alpha$ radiation, $\lambda = 0.71073$ Å
$c = 11.1957\,(8)$ Å	Cell parameters from 2827 reflections

$\theta = 2.3–27.5°$
$\mu = 10.60$ mm^{-1}
$T = 293$ K

Prism, colorless
$0.25 \times 0.20 \times 0.15$ mm

Data collection

Bruker P4 diffractometer	7446 measured reflections
Radiation source: fine-focus sealed tube	2284 independent reflections
Graphite monochromator	2185 reflections with $I > 2\sigma(I)$
Detector resolution: 14.6306 pixels mm^{-1}	$R_{int} = 0.025$
ω scans	$\theta_{max} = 27.5°$, $\theta_{min} = 2.4°$
Absorption correction: ψ scan	$h = -10 \rightarrow 13$
(*XSCANS*; Bruker, 1996)	$k = -10 \rightarrow 11$
$T_{min} = 0.545$, $T_{max} = 1.000$	$l = -14 \rightarrow 14$

Refinement

Refinement on F^2
Least-squares matrix: full
$R[F^2 > 2\sigma(F^2)] = 0.019$
$wR(F^2) = 0.048$
$S = 1.00$
2284 reflections
164 parameters
0 restraints
Primary atom site location: structure-invariant direct methods

Secondary atom site location: difference Fourier map
$w = 1/[\sigma^2(F_o^2) + (0.0273P)^2 + 2.176P]$
where $P = (F_o^2 + 2F_c^2)/3$
$(\Delta/\sigma)_{max} = 0.001$
$\Delta\rho_{max} = 1.16$ e Å^{-3}
$\Delta\rho_{min} = -1.17$ e Å^{-3}
Extinction correction: *SHELXL97* (Sheldrick, 2008), Fc*=kFc[1+0.001xFc$^2\lambda^3$/sin(2θ)]$^{-1/4}$
Extinction coefficient: 0.0154 (3)

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R-factor wR and goodness of fit S are based on F^2, conventional R-factors R are based on F, with F set to zero for negative F^2. The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R-factors(gt) *etc*. and is not relevant to the choice of reflections for refinement. R-factors based on F^2 are statistically about twice as large as those based on F, and R- factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (Å^2)

	x	y	z	U_{iso}*/U_{eq}
Eu	0.498050 (16)	0.226449 (17)	0.180852 (15)	0.00580 (8)
Cs	0.67980 (2)	−0.06549 (3)	0.45979 (2)	0.01775 (9)
P1	0.45959 (9)	−0.17482 (9)	0.13333 (8)	0.00609 (17)
P2	0.75501 (8)	0.02838 (9)	0.78552 (8)	0.00606 (17)
P3	0.67259 (9)	0.39350 (9)	0.47427 (8)	0.00652 (17)
P4	0.64481 (9)	−0.40738 (9)	0.25829 (8)	0.00669 (17)
O1	0.8311 (3)	0.0968 (3)	0.7052 (2)	0.0103 (5)
O2	0.8623 (2)	−0.0428 (3)	0.9043 (2)	0.0084 (5)
O3	0.6485 (3)	−0.0823 (3)	0.7252 (2)	0.0097 (5)
O4	0.5366 (2)	−0.0336 (3)	0.1654 (2)	0.0112 (5)
O5	0.3125 (3)	0.1627 (3)	0.0137 (2)	0.0122 (5)
O6	0.5645 (3)	0.2902 (3)	0.4047 (2)	0.0110 (5)
O7	0.5603 (3)	0.2458 (3)	−0.0102 (2)	0.0110 (5)

O8	0.5213 (2)	−0.2937 (3)	0.2424 (2)	0.0097 (5)	
O9	0.6665 (3)	−0.4514 (3)	0.4006 (2)	0.0116 (5)	
O10	0.7367 (2)	0.1781 (3)	0.2529 (2)	0.0120 (5)	
O11	0.6003 (3)	0.4610 (3)	0.1767 (2)	0.0115 (5)	
O12	0.6881 (2)	0.1588 (3)	0.8470 (2)	0.0085 (5)	

Atomic displacement parameters (Å²)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Eu	0.00621 (11)	0.00206 (10)	0.00886 (11)	−0.00049 (5)	0.00168 (7)	−0.00068 (5)
Cs	0.02071 (15)	0.01835 (13)	0.01329 (14)	0.00425 (9)	0.00334 (10)	−0.00079 (8)
P1	0.0062 (4)	0.0021 (4)	0.0096 (4)	0.0002 (3)	0.0017 (3)	−0.0003 (3)
P2	0.0059 (4)	0.0031 (4)	0.0094 (4)	−0.0003 (3)	0.0026 (3)	0.0003 (3)
P3	0.0070 (4)	0.0036 (4)	0.0082 (4)	0.0000 (3)	0.0009 (3)	0.0006 (3)
P4	0.0074 (4)	0.0025 (4)	0.0094 (4)	0.0003 (3)	0.0011 (3)	0.0006 (3)
O1	0.0109 (12)	0.0084 (11)	0.0128 (12)	−0.0017 (9)	0.0056 (10)	0.0008 (9)
O2	0.0074 (11)	0.0076 (11)	0.0101 (12)	0.0008 (9)	0.0025 (10)	0.0017 (9)
O3	0.0114 (12)	0.0069 (11)	0.0104 (12)	−0.0026 (9)	0.0020 (10)	−0.0032 (9)
O4	0.0085 (12)	0.0052 (11)	0.0203 (14)	−0.0010 (9)	0.0048 (10)	−0.0013 (10)
O5	0.0105 (13)	0.0127 (12)	0.0133 (13)	−0.0055 (10)	0.0032 (10)	−0.0025 (10)
O6	0.0111 (13)	0.0081 (12)	0.0127 (13)	−0.0027 (9)	0.0016 (10)	−0.0037 (9)
O7	0.0109 (13)	0.0108 (11)	0.0116 (13)	−0.0016 (9)	0.0035 (10)	−0.0014 (9)
O8	0.0092 (12)	0.0066 (11)	0.0130 (13)	0.0032 (9)	0.0028 (10)	0.0032 (9)
O9	0.0189 (13)	0.0047 (11)	0.0104 (12)	−0.0017 (10)	0.0027 (10)	−0.0002 (9)
O10	0.0085 (12)	0.0084 (12)	0.0177 (13)	0.0018 (9)	0.0015 (10)	−0.0041 (10)
O11	0.0165 (13)	0.0037 (11)	0.0152 (13)	−0.0027 (9)	0.0063 (10)	−0.0019 (9)
O12	0.0053 (11)	0.0028 (10)	0.0171 (13)	−0.0006 (8)	0.0024 (10)	−0.0022 (9)

Geometric parameters (Å, º)

Eu—O5	2.344 (3)	P2—O1	1.485 (2)
Eu—O11	2.360 (2)	P2—O3	1.495 (3)
Eu—O4	2.379 (2)	P2—O2	1.605 (3)
Eu—O7	2.408 (3)	P2—O12	1.609 (2)
Eu—O10	2.413 (2)	P2—Eu[ii]	3.5752 (9)
Eu—O1[i]	2.416 (2)	P3—O5[viii]	1.479 (3)
Eu—O3[ii]	2.445 (2)	P3—O6	1.492 (3)
Eu—O6	2.471 (3)	P3—O2[ix]	1.607 (2)
Eu—P2[ii]	3.5752 (9)	P3—O9[x]	1.609 (3)
Eu—P3	3.5994 (9)	P4—O10[iv]	1.481 (3)
Eu—Cs	4.1024 (3)	P4—O11[xi]	1.484 (3)
Eu—Cs[iii]	4.4773 (4)	P4—O9	1.594 (3)
Cs—O3	3.083 (2)	P4—O8	1.605 (3)
Cs—O11[iv]	3.089 (2)	P4—Cs[iv]	3.7102 (9)
Cs—O7[iv]	3.093 (3)	O1—Eu[viii]	2.416 (2)
Cs—O1	3.114 (3)	O2—P3[v]	1.607 (2)
Cs—O4	3.224 (3)	O3—Eu[ii]	2.445 (2)
Cs—O8	3.249 (3)	O3—Cs[ii]	3.693 (3)

Cs—O12^v	3.315 (2)	O5—P3^i	1.479 (3)
Cs—O10	3.354 (3)	O7—P1^{vi}	1.479 (3)
Cs—O6	3.399 (3)	O7—Cs^{iii}	3.093 (3)
Cs—O9	3.517 (2)	O9—P3^{xi}	1.609 (3)
Cs—O10^{iv}	3.586 (3)	O10—P4^{iii}	1.481 (3)
Cs—P2	3.6075 (9)	O10—Cs^{iii}	3.586 (3)
P1—O7^{vi}	1.479 (3)	O11—P4^x	1.484 (3)
P1—O4	1.485 (2)	O11—Cs^{iii}	3.089 (2)
P1—O8	1.611 (3)	O12—P1^{ii}	1.612 (2)
P1—O12^{ii}	1.612 (2)	O12—Cs^{ix}	3.315 (2)
P1—Cs^{vii}	3.7970 (9)		
O5—Eu—O11	118.20 (9)	O4—Cs—O10^{iv}	60.36 (6)
O5—Eu—O4	79.62 (9)	O8—Cs—O10^{iv}	42.64 (6)
O11—Eu—O4	141.79 (8)	O12^v—Cs—O10^{iv}	79.81 (6)
O5—Eu—O7	70.90 (9)	O10—Cs—O10^{iv}	80.580 (8)
O11—Eu—O7	71.60 (8)	O6—Cs—O10^{iv}	128.21 (6)
O4—Eu—O7	85.04 (9)	O9—Cs—O10^{iv}	41.28 (6)
O5—Eu—O10	139.03 (9)	O3—Cs—P2	24.24 (5)
O11—Eu—O10	75.15 (9)	O11^{iv}—Cs—P2	120.18 (5)
O4—Eu—O10	70.81 (8)	O7^{iv}—Cs—P2	90.79 (5)
O7—Eu—O10	78.72 (9)	O1—Cs—P2	24.12 (4)
O5—Eu—O1^i	78.33 (9)	O4—Cs—P2	156.80 (5)
O11—Eu—O1^i	75.98 (8)	O8—Cs—P2	145.49 (5)
O4—Eu—O1^i	142.22 (8)	O12^v—Cs—P2	65.31 (5)
O7—Eu—O1^i	115.59 (9)	O10—Cs—P2	121.11 (5)
O10—Eu—O1^i	141.10 (9)	O6—Cs—P2	85.97 (5)
O5—Eu—O3^{ii}	75.28 (8)	O9—Cs—P2	113.94 (4)
O11—Eu—O3^{ii}	144.64 (8)	O10^{iv}—Cs—P2	142.83 (4)
O4—Eu—O3^{ii}	69.56 (8)	O7^{vi}—P1—O4	121.10 (15)
O7—Eu—O3^{ii}	140.72 (8)	O7^{vi}—P1—O8	110.06 (14)
O10—Eu—O3^{ii}	117.57 (9)	O4—P1—O8	108.01 (15)
O1^i—Eu—O3^{ii}	75.37 (8)	O7^{vi}—P1—O12^{ii}	106.09 (14)
O5—Eu—O6	142.87 (8)	O4—P1—O12^{ii}	110.89 (13)
O11—Eu—O6	79.39 (9)	O8—P1—O12^{ii}	98.32 (13)
O4—Eu—O6	107.21 (9)	O7^{vi}—P1—Cs^{vii}	51.19 (10)
O7—Eu—O6	144.72 (9)	O4—P1—Cs^{vii}	157.90 (11)
O10—Eu—O6	74.71 (9)	O8—P1—Cs^{vii}	93.73 (10)
O1^i—Eu—O6	74.81 (9)	O12^{ii}—P1—Cs^{vii}	60.52 (9)
O3^{ii}—Eu—O6	73.47 (8)	O7^{vi}—P1—Cs	152.14 (11)
O5—Eu—P2^{ii}	57.86 (6)	O4—P1—Cs	54.51 (10)
O11—Eu—P2^{ii}	156.53 (6)	O8—P1—Cs	56.39 (10)
O4—Eu—P2^{ii}	61.64 (6)	O12^{ii}—P1—Cs	100.29 (10)
O7—Eu—P2^{ii}	121.82 (6)	Cs^{vii}—P1—Cs	143.55 (2)
O10—Eu—P2^{ii}	124.21 (6)	O1—P2—O3	116.76 (15)
O1^i—Eu—P2^{ii}	80.66 (6)	O1—P2—O2	107.71 (14)
O3^{ii}—Eu—P2^{ii}	19.06 (6)	O3—P2—O2	111.15 (14)
O6—Eu—P2^{ii}	92.51 (6)	O1—P2—O12	108.98 (14)

O5—Eu—P3	156.63 (6)	O3—P2—O12	108.82 (14)
O11—Eu—P3	62.28 (6)	O2—P2—O12	102.45 (13)
O4—Eu—P3	114.99 (6)	O1—P2—Eu^{ii}	149.02 (11)
O7—Eu—P3	126.11 (6)	O3—P2—Eu^{ii}	32.27 (10)
O10—Eu—P3	64.27 (6)	O2—P2—Eu^{ii}	90.91 (9)
O1^{i}—Eu—P3	79.40 (6)	O12—P2—Eu^{ii}	90.11 (9)
O3^{ii}—Eu—P3	92.32 (6)	O1—P2—Cs	58.96 (10)
O6—Eu—P3	18.85 (6)	O3—P2—Cs	57.81 (10)
P2^{ii}—Eu—P3	111.36 (2)	O2—P2—Cs	130.28 (9)
O5—Eu—Cs	123.34 (6)	O12—P2—Cs	127.26 (10)
O11—Eu—Cs	118.09 (6)	Eu^{ii}—P2—Cs	90.08 (2)
O4—Eu—Cs	51.71 (6)	O5^{viii}—P3—O6	118.20 (15)
O7—Eu—Cs	122.82 (6)	O5^{viii}—P3—O2^{ix}	107.64 (14)
O10—Eu—Cs	54.82 (6)	O6—P3—O2^{ix}	110.36 (14)
O1^{i}—Eu—Cs	121.45 (6)	O5^{viii}—P3—O9^{x}	109.94 (14)
O3^{ii}—Eu—Cs	62.80 (6)	O6—P3—O9^{x}	110.66 (15)
O6—Eu—Cs	55.84 (6)	O2^{ix}—P3—O9^{x}	98.14 (13)
P2^{ii}—Eu—Cs	72.864 (15)	O5^{viii}—P3—Eu	109.19 (11)
P3—Eu—Cs	64.255 (15)	O6—P3—Eu	32.35 (10)
O5—Eu—Cs^{iii}	110.19 (6)	O2^{ix}—P3—Eu	138.19 (9)
O11—Eu—Cs^{iii}	40.47 (6)	O9^{x}—P3—Eu	87.37 (10)
O4—Eu—Cs^{iii}	103.03 (6)	O5^{viii}—P3—Cs	69.17 (11)
O7—Eu—Cs^{iii}	40.98 (6)	O6—P3—Cs	51.61 (10)
O10—Eu—Cs^{iii}	52.97 (6)	O2^{ix}—P3—Cs	113.51 (9)
O1^{i}—Eu—Cs^{iii}	113.24 (6)	O9^{x}—P3—Cs	147.29 (10)
O3^{ii}—Eu—Cs^{iii}	170.28 (6)	Eu—P3—Cs	63.810 (14)
O6—Eu—Cs^{iii}	103.77 (6)	O10^{iv}—P4—O11^{xi}	118.71 (15)
P2^{ii}—Eu—Cs^{iii}	160.739 (15)	O10^{iv}—P4—O9	108.98 (15)
P3—Eu—Cs^{iii}	85.139 (15)	O11^{xi}—P4—O9	110.52 (14)
Cs—Eu—Cs^{iii}	107.796 (7)	O10^{iv}—P4—O8	108.41 (14)
O3—Cs—O11^{iv}	140.63 (7)	O11^{xi}—P4—O8	109.63 (15)
O3—Cs—O7^{iv}	96.87 (7)	O9—P4—O8	98.71 (14)
O11^{iv}—Cs—O7^{iv}	53.65 (6)	O10^{iv}—P4—Cs^{iv}	64.61 (11)
O3—Cs—O1	48.36 (6)	O11^{xi}—P4—Cs^{iv}	54.28 (10)
O11^{iv}—Cs—O1	98.19 (7)	O9—P4—Cs^{iv}	127.28 (10)
O7^{iv}—Cs—O1	84.17 (7)	O8—P4—Cs^{iv}	133.76 (10)
O3—Cs—O4	147.89 (6)	O10^{iv}—P4—Cs	71.77 (11)
O11^{iv}—Cs—O4	71.25 (6)	O11^{xi}—P4—Cs	167.85 (11)
O7^{iv}—Cs—O4	111.18 (6)	O9—P4—Cs	68.87 (9)
O1—Cs—O4	146.42 (6)	O8—P4—Cs	59.27 (10)
O3—Cs—O8	121.57 (6)	Cs^{iv}—P4—Cs	136.34 (2)
O11^{iv}—Cs—O8	88.01 (6)	P2—O1—Eu^{viii}	149.05 (16)
O7^{iv}—Cs—O8	91.30 (6)	P2—O1—Cs	96.92 (12)
O1—Cs—O8	167.93 (6)	Eu^{viii}—O1—Cs	113.90 (9)
O4—Cs—O8	45.55 (6)	P2—O2—P3^{v}	125.03 (15)
O3—Cs—O12^{v}	58.05 (6)	P2—O3—Eu^{ii}	128.67 (14)
O11^{iv}—Cs—O12^{v}	98.84 (6)	P2—O3—Cs	97.95 (11)
O7^{iv}—Cs—O12^{v}	45.19 (6)	Eu^{ii}—O3—Cs	133.38 (9)

O1—Cs—O12^{v}	76.10 (6)	P2—O3—Cs^{ii}	117.46 (12)
O4—Cs—O12^{v}	136.03 (6)	Eu^{ii}—O3—Cs^{ii}	81.12 (7)
O8—Cs—O12^{v}	92.77 (6)	Cs—O3—Cs^{ii}	76.82 (6)
O3—Cs—O10	141.66 (6)	P1—O4—Eu	139.70 (15)
O11^{iv}—Cs—O10	46.43 (6)	P1—O4—Cs	103.46 (12)
O7^{iv}—Cs—O10	99.72 (6)	Eu—O4—Cs	92.90 (8)
O1—Cs—O10	99.37 (6)	P3^{i}—O5—Eu	146.62 (16)
O4—Cs—O10	49.90 (6)	P3—O6—Eu	128.80 (15)
O8—Cs—O10	92.42 (6)	P3—O6—Cs	108.25 (13)
O12^{v}—Cs—O10	144.62 (6)	Eu—O6—Cs	87.17 (7)
O3—Cs—O6	95.38 (6)	P1^{vi}—O7—Eu	142.64 (15)
O11^{iv}—Cs—O6	96.23 (6)	P1^{vi}—O7—Cs^{iii}	106.94 (12)
O7^{iv}—Cs—O6	142.10 (6)	Eu—O7—Cs^{iii}	108.31 (9)
O1—Cs—O6	77.64 (6)	P4—O8—P1	129.62 (16)
O4—Cs—O6	72.20 (6)	P4—O8—Cs	95.59 (11)
O8—Cs—O6	112.13 (6)	P1—O8—Cs	99.22 (11)
O12^{v}—Cs—O6	151.27 (6)	P4—O9—P3^{xi}	134.46 (17)
O10—Cs—O6	52.07 (6)	P4—O9—Cs	86.11 (10)
O3—Cs—O9	97.16 (6)	P3^{xi}—O9—Cs	139.40 (13)
O11^{iv}—Cs—O9	88.72 (6)	P4^{iii}—O10—Eu	149.26 (16)
O7^{iv}—Cs—O9	58.85 (6)	P4^{iii}—O10—Cs	91.87 (12)
O1—Cs—O9	127.52 (6)	Eu—O10—Cs	89.14 (7)
O4—Cs—O9	84.95 (6)	P4^{iii}—O10—Cs^{iii}	85.12 (11)
O8—Cs—O9	41.82 (6)	Eu—O10—Cs^{iii}	94.52 (8)
O12^{v}—Cs—O9	51.48 (6)	Cs—O10—Cs^{iii}	176.32 (8)
O10—Cs—O9	121.00 (6)	P4^{x}—O11—Eu	139.40 (15)
O6—Cs—O9	153.49 (6)	P4^{x}—O11—Cs^{iii}	102.77 (12)
O3—Cs—O10^{iv}	136.01 (6)	Eu—O11—Cs^{iii}	109.80 (8)
O11^{iv}—Cs—O10^{iv}	51.06 (6)	P2—O12—P1^{ii}	131.54 (16)
O7^{iv}—Cs—O10^{iv}	53.89 (6)	P2—O12—Cs^{ix}	132.22 (12)
O1—Cs—O10^{iv}	136.86 (6)	P1^{ii}—O12—Cs^{ix}	94.44 (10)

Symmetry codes: (i) $x-1/2$, $-y+1/2$, $z-1/2$; (ii) $-x+1$, $-y$, $-z+1$; (iii) $-x+3/2$, $y+1/2$, $-z+1/2$; (iv) $-x+3/2$, $y-1/2$, $-z+1/2$; (v) $-x+3/2$, $y-1/2$, $-z+3/2$; (vi) $-x+1$, $-y$, $-z$; (vii) $x-1/2$, $-y-1/2$, $z-1/2$; (viii) $x+1/2$, $-y+1/2$, $z+1/2$; (ix) $-x+3/2$, $y+1/2$, $-z+3/2$; (x) x, $y+1$, z; (xi) x, $y-1$, z.