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Bis(melaminium) succinate succinic acid monosolvate dihydrate

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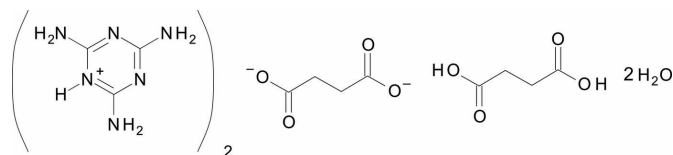
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Key indicators: single-crystal X-ray study; $T = 293$ K; mean $\sigma(\text{C}-\text{C}) = 0.003$ Å; R factor = 0.047; wR factor = 0.142; data-to-parameter ratio = 15.7.

The asymmetric unit of the solvated title salt, $2\text{C}_3\text{H}_7\text{N}_6^{+}\cdot\text{C}_4\text{H}_4\text{O}_4^{2-}\cdot\text{C}_4\text{H}_6\text{O}_4\cdot 2\text{H}_2\text{O}$, contains one essentially planar melaminium (2,4,6-triamino-1,3,5-triazin-1-ium) cation (r.m.s. deviation of the non-H atoms = 0.0097 Å), one-half of a succinate anion, one-half of a succinic acid solvent molecule and one water molecule of crystallization; full molecules are generated by inversion symmetry. Supramolecular layers parallel to (12 $\bar{1}$) are formed through extensive intermolecular hydrogen bonding of the types $\text{O}-\text{H}\cdots\text{O}$, $\text{N}-\text{H}\cdots\text{N}$ and $\text{N}-\text{H}\cdots\text{O}$ between the components.

Related literature

For the use of melaminium salts in polymer science, see: Weinstabl *et al.* (2001). For a list of structurally determined melaminium salts of purely organic carboxylic acids, see: Froschauer & Weil (2012).



Experimental

Crystal data

$2\text{C}_3\text{H}_7\text{N}_6^{+}\cdot\text{C}_4\text{H}_4\text{O}_4^{2-}\cdot\text{C}_4\text{H}_6\text{O}_4\cdot 2\text{H}_2\text{O}$ $\alpha = 88.013$ (2) $^\circ$
 $M_r = 524.48$ $\beta = 84.647$ (2) $^\circ$
 Triclinic, $P\bar{1}$ $\gamma = 88.093$ (2) $^\circ$
 $a = 7.1193$ (7) Å $V = 552.68$ (9) Å³
 $b = 8.1650$ (8) Å $Z = 1$
 $c = 9.5595$ (9) Å Mo $K\alpha$ radiation

$\mu = 0.13$ mm⁻¹
 $T = 293$ K

0.23 × 0.18 × 0.12 mm

Data collection

Siemens SMART CCD diffractometer
 5533 measured reflections

2719 independent reflections
 1545 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.028$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.047$
 $wR(F^2) = 0.142$
 $S = 0.97$
 2719 reflections
 173 parameters
 3 restraints

H atoms treated by a mixture of independent and constrained refinement
 $\Delta\rho_{\text{max}} = 0.30$ e Å⁻³
 $\Delta\rho_{\text{min}} = -0.26$ e Å⁻³

Table 1

Hydrogen-bond geometry (Å, °).

$D-\text{H}\cdots A$	$D-\text{H}$	$\text{H}\cdots A$	$D\cdots A$	$D-\text{H}\cdots A$
$\text{N4}-\text{H3}\cdots\text{N2}^{\text{i}}$	0.86	2.10	2.959 (2)	176
$\text{N1}-\text{H1}\cdots\text{O1}$	0.86	2.01	2.844 (2)	164
$\text{N5}-\text{H4}\cdots\text{O3}^{\text{ii}}$	0.86	2.13	2.976 (2)	170
$\text{N6}-\text{H6}\cdots\text{N3}^{\text{iii}}$	0.86	2.16	3.015 (2)	173
$\text{N1}-\text{H1}\cdots\text{O2}$	0.86	2.50	3.199 (2)	138
$\text{N4}-\text{H2}\cdots\text{O3}^{\text{iv}}$	0.86	2.14	2.799 (2)	134
$\text{N4}-\text{H2}\cdots\text{O1}$	0.86	2.56	3.268 (2)	141
$\text{N6}-\text{H7}\cdots\text{O2}$	0.86	1.94	2.782 (2)	166
$\text{N5}-\text{H5}\cdots\text{O1W}^{\text{v}}$	0.86	2.11	2.912 (2)	154
$\text{O1W}-\text{H1W}\cdots\text{O4}$	0.88 (2)	2.35 (2)	3.195 (2)	162 (3)
$\text{O1W}-\text{H2W}\cdots\text{O2}^{\text{vi}}$	0.86 (2)	1.89 (2)	2.726 (2)	167 (3)
$\text{O4}-\text{H12}\cdots\text{O1}^{\text{iv}}$	1.02 (2)	1.55 (2)	2.5673 (19)	177 (3)

Symmetry codes: (i) $-x, -y + 2, -z$; (ii) $x - 1, y + 1, z$; (iii) $-x + 1, -y + 2, -z + 1$; (iv) $-x + 1, -y + 1, -z$; (v) $-x, -y + 2, -z + 1$; (vi) $x - 1, y, z$.

Data collection: *SMART* (Siemens, 1996); cell refinement: *SAINT* (Siemens, 1996); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *Mercury* (Macrae *et al.*, 2006) and *ATOMS* (Dowty, 2006); software used to prepare material for publication: *pubCIF* (Westrip, 2010).

The X-ray centre of the Vienna University of Technology is acknowledged for financial support and for providing access to the single-crystal diffractometer.

Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: CV5324).

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supporting information

Acta Cryst. (2012). E68, o2555 [https://doi.org/10.1107/S1600536812033387]

Bis(melaminium) succinate succinic acid monosolvate dihydrate**Barbara Froschauer and Matthias Weil****S1. Comment**

The potential substitution of melamine through organic melaminium salts for production of melamine urea formaldehyde (MUF) resins (Weinstabl *et al.*, 2001) render the structural investigation of these compounds interesting. A list of already determined structures of purely organic melaminium salts has been compiled recently by Froschauer & Weil (2012).

The pK_a values of 4.21 and 5.72 for the first and second deprotonation step of succinic acid (the pK_a of the first deprotonation step of melamine is 5.10) led to a doubly deprotonated anion in the title compound, bis-melaminium succinate succinic acid solvate dihydrate, $2(\text{C}_3\text{H}_7\text{N}_6)^+\text{C}_4\text{H}_4\text{O}_4^-\text{C}_4\text{H}_6\text{O}_4\cdot 2(\text{H}_2\text{O})$. However, besides lattice water, there is also one succinic acid solvent molecule present in the unit cell. The succinic acid molecule and the succinate anion are located with their central C—C bond on inversion centres. As observed for all single protonated melaminium cations, the protonation of melamine takes place at one of the triazine N ring atoms (Fig. 1).

The melaminium cation is essentially planar with a r.m.s. deviation of 0.0097 Å. Likewise, the anion (r.m.s. deviation 0.039 Å) and the succinic acid molecule (r.m.s. deviation 0.060 Å) can be considered as planar. The angles between the least-squares planes of 6.59 (9)° and 5.76 (12)° between the anion and the cation and the succinic acid molecule, respectively, lead to the formation of supramolecular layers where cations are arranged in rows alternating with rows of anions, succinic acid solvent and lattice water molecules (Fig. 2). Extensive intermolecular hydrogen bonding of the types O—H...O, N—H...N and N—H...O between the molecular components is present. Details are reported in Table 1. The motif for the hydrogen-bonded assembly of two melaminium cations in such a layer is the same as in the hydrogenmalonate salt and other melaminium salts (Froschauer & Weil, 2012). In the crystal, the supramolecular layers are arranged parallel to (12 $\bar{1}$) (Fig. 3) with an interplanar distance of approximately 3.15 Å.

S2. Experimental

79.3 mmol melamine was dissolved under refluxing conditions in 200 ml distilled water. The stoichiometric quantity (1:1) of succinic acid was added within five minutes. The mixture was then refluxed for 30 minutes and then cooled to room temperature. The precipitate formed on cooling was separated by filtration and washed with cold methanol. The crystalline product was then dried *in vacuo* at 303–313 K. Single crystal growth was accomplished by dissolution of 1 g of the crystalline product under refluxing conditions in an aqueous methanol solution (2:1 v/v) to get a saturated solution. Then the solution was slowly cooled down to room temperature. Suitable crystals were obtained by slow evaporation of the solvents during five days. The crystals were washed with methanol and dried *in vacuo* at room temperature giving analytical pure samples. CHN analysis (found/calc.): C (32.13/32.10), H (5.50/5.38), N (31.93/32.05). NMR: (solution, DMSO) chemical shift [p.p.m.]: ^1H 10.37 (s, 2H), 6.22 (s, 6H), 2.39 (s, 4H); ^{13}C 174.32, 166.43, 29.29.

S3. Refinement

The proton at the triazine ring of the melaminium cation was clearly discernible from a difference Fourier map (like all other H atoms). For refinement, the H atoms attached to C or N atoms were set in calculated positions and treated as riding on their parent atoms with C—H = 0.97 Å and N—H = 0.86 Å and with $U_{\text{iso}}(\text{H}) = 1.2U_{\text{eq}}(\text{C},\text{N})$. The proton of the carboxy group of the succinic acid solvent molecule was refined with a distance restraint O—H = 1.00 (2) Å; H atoms of the water molecule were likewise refined with a distance restraint of O—H = 0.88 (2) Å.

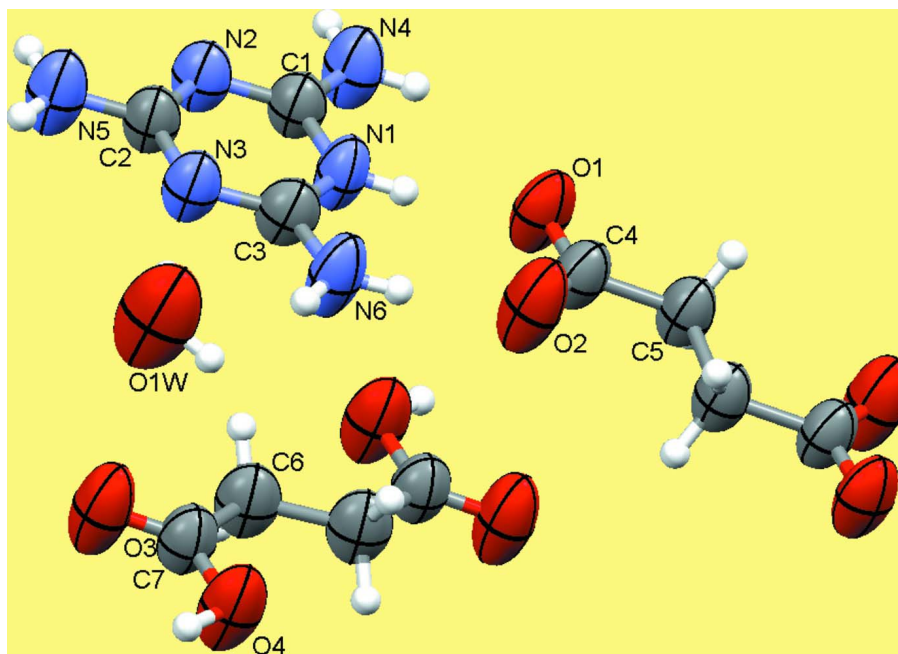


Figure 1

The molecular components of the title compound drawn with atomic displacement factors at the 90% probability level. H atoms are displayed as spheres with an arbitrary radius. For the centrosymmetric succinate anion and the succinic acid solvent molecule the symmetry-equivalent atoms are not labelled.

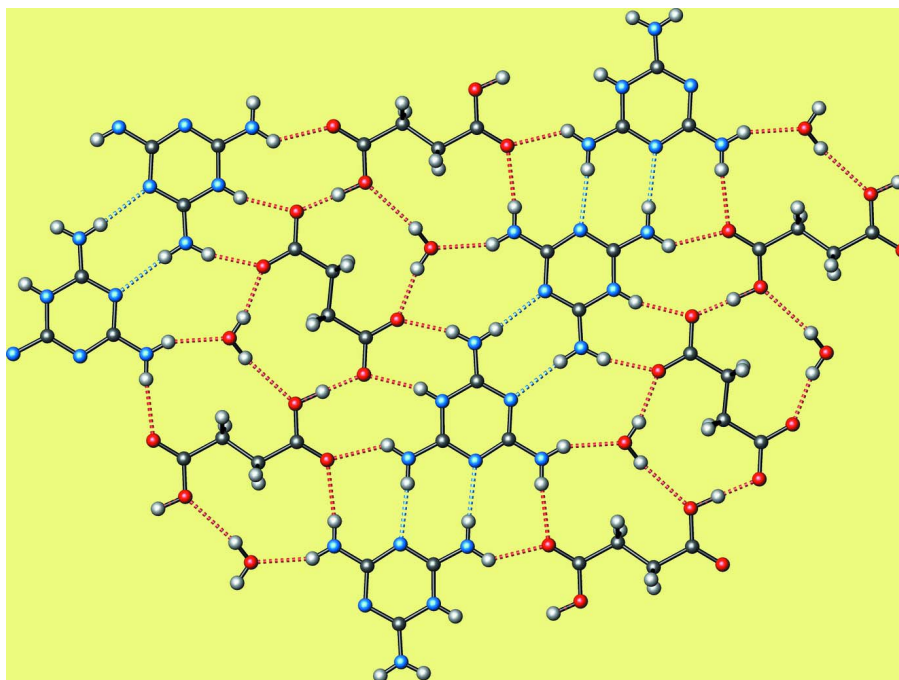


Figure 2

Supramolecular layer built up through hydrogen bonding interactions (dashed lines) between the molecular components.

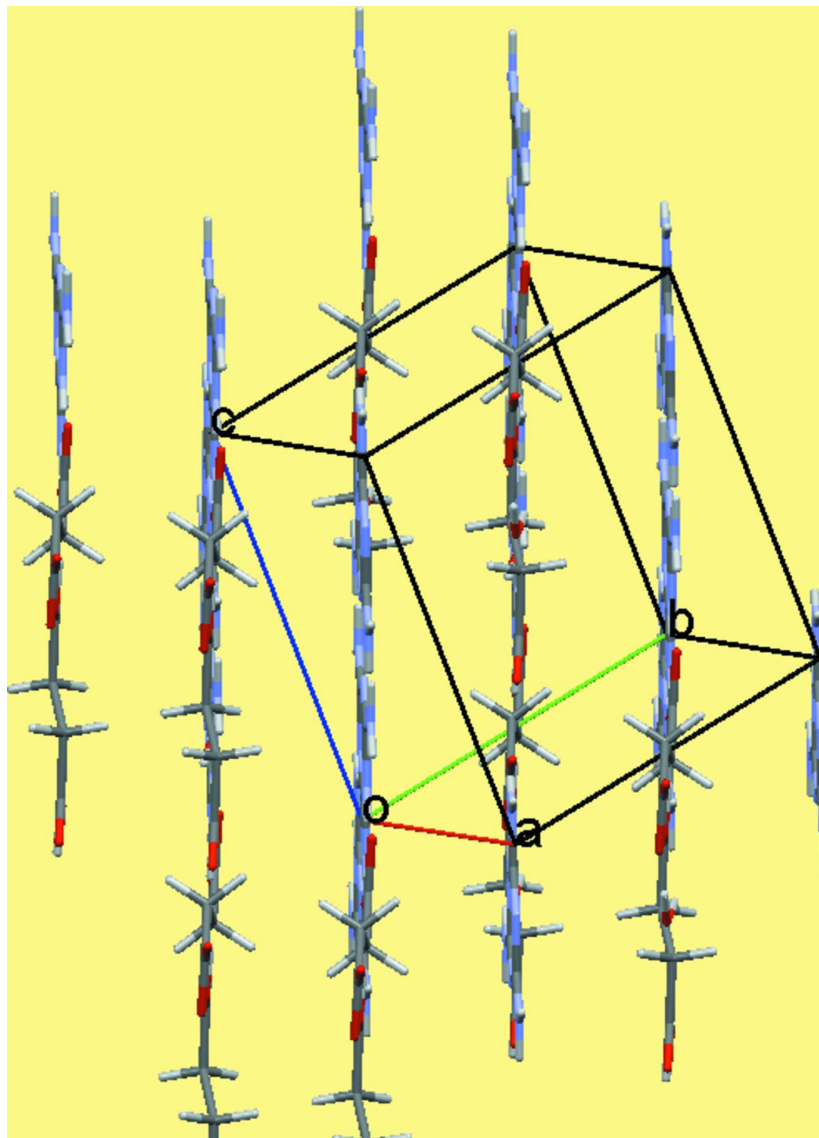
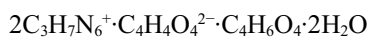


Figure 3

The assembly of supramolecular layers in the crystal parallel to $(12\bar{1})$.

Bis(2,4,6-triamino-1,3,5-triazin-1-ium) succinate succinic acid monosolvate dihydrate

Crystal data



$M_r = 524.48$

Triclinic, $P\bar{1}$

Hall symbol: $-P\ 1$

$a = 7.1193\ (7)\ \text{\AA}$

$b = 8.1650\ (8)\ \text{\AA}$

$c = 9.5595\ (9)\ \text{\AA}$

$\alpha = 88.013\ (2)^\circ$

$\beta = 84.647\ (2)^\circ$

$\gamma = 88.093\ (2)^\circ$

$V = 552.68\ (9)\ \text{\AA}^3$

$Z = 1$

$F(000) = 276$

$D_x = 1.576\ \text{Mg m}^{-3}$

Mo $K\alpha$ radiation, $\lambda = 0.71073\ \text{\AA}$

Cell parameters from 1570 reflections

$\theta = 2.5\text{--}28.8^\circ$

$\mu = 0.13\ \text{mm}^{-1}$

$T = 293\ \text{K}$

Parallelepiped, colourless

$0.23 \times 0.18 \times 0.12\ \text{mm}$

*Data collection*Siemens SMART CCD
diffractometer

Radiation source: fine-focus sealed tube

Graphite monochromator

 ω scans

5533 measured reflections

2719 independent reflections

1545 reflections with $I > 2\sigma(I)$ $R_{\text{int}} = 0.028$ $\theta_{\text{max}} = 28.3^\circ$, $\theta_{\text{min}} = 2.1^\circ$ $h = -9 \rightarrow 9$ $k = -10 \rightarrow 10$ $l = -12 \rightarrow 12$ *Refinement*Refinement on F^2

Least-squares matrix: full

 $R[F^2 > 2\sigma(F^2)] = 0.047$ $wR(F^2) = 0.142$ $S = 0.97$

2719 reflections

173 parameters

3 restraints

Primary atom site location: structure-invariant

direct methods

Secondary atom site location: difference Fourier

map

Hydrogen site location: inferred from
neighbouring sitesH atoms treated by a mixture of independent
and constrained refinement $w = 1/[\sigma^2(F_o^2) + (0.0791P)^2]$ where $P = (F_o^2 + 2F_c^2)/3$ $(\Delta/\sigma)_{\text{max}} < 0.001$ $\Delta\rho_{\text{max}} = 0.30 \text{ e } \text{\AA}^{-3}$ $\Delta\rho_{\text{min}} = -0.26 \text{ e } \text{\AA}^{-3}$ Extinction correction: *SHELXL97* (Sheldrick,
2008), $F_c^* = kF_c[1 + 0.001x F_c^2 \lambda^3 / \sin(2\theta)]^{-1/4}$

Extinction coefficient: 0.010 (4)

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) *etc.* and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	x	y	z	$U_{\text{iso}}^*/U_{\text{eq}}$
N3	0.3081 (2)	1.0330 (2)	0.36672 (15)	0.0308 (4)
N1	0.4064 (2)	0.8895 (2)	0.16163 (15)	0.0323 (4)
H1	0.4894	0.8279	0.1160	0.039*
O1	0.62741 (19)	0.68205 (18)	-0.02657 (14)	0.0385 (4)
O3	0.6682 (2)	0.2996 (2)	0.25900 (15)	0.0456 (4)
O2	0.8071 (2)	0.6984 (2)	0.14806 (15)	0.0480 (5)
O4	0.3997 (2)	0.44613 (19)	0.26505 (14)	0.0431 (4)
C7	0.5535 (3)	0.3930 (3)	0.3191 (2)	0.0309 (5)
C1	0.2450 (3)	0.9365 (2)	0.10469 (19)	0.0284 (4)
N2	0.1121 (2)	1.0287 (2)	0.17327 (15)	0.0305 (4)
C2	0.1488 (3)	1.0729 (2)	0.30373 (18)	0.0281 (4)
C6	0.5839 (3)	0.4567 (3)	0.46117 (19)	0.0339 (5)
H6A	0.6871	0.5321	0.4491	0.041*
H6B	0.6233	0.3651	0.5200	0.041*
N4	0.2251 (2)	0.8874 (2)	-0.02317 (16)	0.0370 (4)

H3	0.1250	0.9151	-0.0632	0.044*
H2	0.3123	0.8277	-0.0664	0.044*
N6	0.5975 (2)	0.8950 (2)	0.34112 (18)	0.0402 (5)
H6	0.6226	0.9242	0.4228	0.048*
H7	0.6778	0.8356	0.2909	0.048*
C3	0.4365 (3)	0.9412 (2)	0.29314 (19)	0.0301 (5)
C4	0.7771 (3)	0.6435 (2)	0.0324 (2)	0.0308 (5)
N5	0.0177 (2)	1.1639 (2)	0.37353 (17)	0.0396 (5)
H5	0.0347	1.1959	0.4561	0.048*
H4	-0.0848	1.1912	0.3365	0.048*
O1W	0.0343 (3)	0.6661 (3)	0.36216 (18)	0.0637 (6)
H1W	0.126 (4)	0.591 (3)	0.353 (3)	0.097*
H2W	-0.024 (4)	0.667 (4)	0.288 (2)	0.097*
H12	0.385 (4)	0.393 (3)	0.171 (2)	0.097*
C5	0.9192 (3)	0.5292 (3)	-0.04228 (19)	0.0306 (5)
H5A	0.9717	0.5841	-0.1280	0.037*
H5B	0.8543	0.4341	-0.0690	0.037*

Atomic displacement parameters (Å²)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
N3	0.0277 (9)	0.0441 (10)	0.0218 (8)	0.0109 (8)	-0.0092 (7)	-0.0101 (7)
N1	0.0283 (9)	0.0444 (10)	0.0248 (8)	0.0147 (8)	-0.0070 (7)	-0.0131 (7)
O1	0.0295 (8)	0.0537 (10)	0.0344 (8)	0.0173 (7)	-0.0150 (6)	-0.0151 (7)
O3	0.0392 (9)	0.0659 (11)	0.0337 (8)	0.0230 (8)	-0.0151 (7)	-0.0236 (7)
O2	0.0455 (9)	0.0664 (11)	0.0351 (8)	0.0258 (8)	-0.0193 (7)	-0.0285 (8)
O4	0.0381 (9)	0.0635 (11)	0.0303 (8)	0.0209 (7)	-0.0178 (6)	-0.0191 (7)
C7	0.0278 (10)	0.0395 (12)	0.0261 (9)	0.0081 (9)	-0.0067 (8)	-0.0069 (8)
C1	0.0269 (10)	0.0366 (11)	0.0222 (9)	0.0051 (8)	-0.0061 (8)	-0.0061 (8)
N2	0.0281 (9)	0.0428 (10)	0.0217 (8)	0.0076 (7)	-0.0085 (7)	-0.0097 (7)
C2	0.0250 (10)	0.0386 (11)	0.0215 (9)	0.0063 (8)	-0.0062 (8)	-0.0067 (8)
C6	0.0296 (11)	0.0479 (13)	0.0257 (10)	0.0076 (9)	-0.0106 (8)	-0.0085 (9)
N4	0.0332 (9)	0.0548 (12)	0.0245 (8)	0.0131 (8)	-0.0107 (7)	-0.0169 (8)
N6	0.0330 (10)	0.0596 (12)	0.0295 (9)	0.0231 (9)	-0.0130 (7)	-0.0173 (8)
C3	0.0301 (10)	0.0372 (12)	0.0243 (9)	0.0055 (9)	-0.0095 (8)	-0.0070 (8)
C4	0.0282 (10)	0.0357 (11)	0.0294 (10)	0.0105 (9)	-0.0083 (8)	-0.0083 (8)
N5	0.0322 (9)	0.0630 (13)	0.0255 (8)	0.0174 (9)	-0.0127 (7)	-0.0182 (8)
O1W	0.0646 (12)	0.0902 (15)	0.0408 (9)	0.0294 (10)	-0.0287 (8)	-0.0315 (9)
C5	0.0299 (10)	0.0388 (12)	0.0243 (9)	0.0108 (9)	-0.0087 (8)	-0.0104 (8)

Geometric parameters (Å, °)

N3—C3	1.328 (2)	C6—H6A	0.9700
N3—C2	1.358 (2)	C6—H6B	0.9700
N1—C1	1.356 (2)	N4—H3	0.8600
N1—C3	1.378 (2)	N4—H2	0.8600
N1—H1	0.8600	N6—C3	1.313 (2)
O1—C4	1.277 (2)	N6—H6	0.8600

O3—C7	1.217 (2)	N6—H7	0.8600
O2—C4	1.246 (2)	C4—C5	1.500 (3)
O4—C7	1.309 (2)	N5—H5	0.8600
O4—H12	1.023 (17)	N5—H4	0.8600
C7—C6	1.507 (3)	O1W—H1W	0.882 (17)
C1—N4	1.321 (2)	O1W—H2W	0.856 (18)
C1—N2	1.328 (2)	C5—C5 ⁱⁱ	1.522 (3)
N2—C2	1.361 (2)	C5—H5A	0.9700
C2—N5	1.319 (2)	C5—H5B	0.9700
C6—C6 ⁱ	1.514 (4)		
C3—N3—C2	115.93 (15)	C1—N4—H2	120.0
C1—N1—C3	119.48 (16)	H3—N4—H2	120.0
C1—N1—H1	120.3	C3—N6—H6	120.0
C3—N1—H1	120.3	C3—N6—H7	120.0
C7—O4—H12	111.6 (17)	H6—N6—H7	120.0
O3—C7—O4	122.87 (17)	N6—C3—N3	122.22 (17)
O3—C7—C6	121.05 (18)	N6—C3—N1	116.61 (17)
O4—C7—C6	116.07 (17)	N3—C3—N1	121.17 (17)
N4—C1—N2	120.96 (17)	O2—C4—O1	121.88 (17)
N4—C1—N1	117.14 (17)	O2—C4—C5	120.22 (17)
N2—C1—N1	121.90 (16)	O1—C4—C5	117.90 (16)
C1—N2—C2	115.70 (16)	C2—N5—H5	120.0
N5—C2—N3	117.76 (16)	C2—N5—H4	120.0
N5—C2—N2	116.44 (16)	H5—N5—H4	120.0
N3—C2—N2	125.80 (17)	H1W—O1W—H2W	107 (3)
C7—C6—C6 ⁱ	116.3 (2)	C4—C5—C5 ⁱⁱ	115.00 (19)
C7—C6—H6A	108.2	C4—C5—H5A	108.5
C6 ⁱ —C6—H6A	108.2	C5 ⁱⁱ —C5—H5A	108.5
C7—C6—H6B	108.2	C4—C5—H5B	108.5
C6 ⁱ —C6—H6B	108.2	C5 ⁱⁱ —C5—H5B	108.5
H6A—C6—H6B	107.4	H5A—C5—H5B	107.5
C1—N4—H3	120.0		

Symmetry codes: (i) $-x+1, -y+1, -z+1$; (ii) $-x+2, -y+1, -z$.

Hydrogen-bond geometry (\AA , $^\circ$)

$D-H\cdots A$	$D-H$	$H\cdots A$	$D\cdots A$	$D-H\cdots A$
N4—H3 \cdots N2 ⁱⁱⁱ	0.86	2.10	2.959 (2)	176
N1—H1 \cdots O1	0.86	2.01	2.844 (2)	164
N5—H4 \cdots O3 ^{iv}	0.86	2.13	2.976 (2)	170
N6—H6 \cdots N3 ^v	0.86	2.16	3.015 (2)	173
N1—H1 \cdots O2	0.86	2.50	3.199 (2)	138
N4—H2 \cdots O3 ^{vi}	0.86	2.14	2.799 (2)	134
N4—H2 \cdots O1	0.86	2.56	3.268 (2)	141
N6—H7 \cdots O2	0.86	1.94	2.782 (2)	166
N5—H5 \cdots O1W ^{vii}	0.86	2.11	2.912 (2)	154

O1 <i>W</i> —H1 <i>W</i> ···O4	0.88 (2)	2.35 (2)	3.195 (2)	162 (3)
O1 <i>W</i> —H2 <i>W</i> ···O2 ^{viii}	0.86 (2)	1.89 (2)	2.726 (2)	167 (3)
O4—H12···O1 ^{vi}	1.02 (2)	1.55 (2)	2.5673 (19)	177 (3)

Symmetry codes: (iii) $-x, -y+2, -z$; (iv) $x-1, y+1, z$; (v) $-x+1, -y+2, -z+1$; (vi) $-x+1, -y+1, -z$; (vii) $-x, -y+2, -z+1$; (viii) $x-1, y, z$.