

Phenazin-5-ium hydrogen sulfate mono-hydrate

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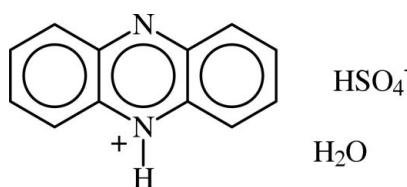
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Key indicators: single-crystal X-ray study; $T = 120\text{ K}$; mean $\sigma(\text{C}-\text{C}) = 0.002\text{ \AA}$; R factor = 0.032; wR factor = 0.088; data-to-parameter ratio = 12.1.

The crystal structure of the title salt, $\text{C}_{12}\text{H}_9\text{N}_2^+\cdot\text{HSO}_4^-\cdot\text{H}_2\text{O}$, comprises inversion-related pairs of phenazinium ions linked by $\text{C}-\text{H}\cdots\text{N}$ hydrogen bonds. The phenazinium $\text{N}-\text{H}$ atoms are hydrogen bonded to the bisulfate anions. The bisulfate anions and water molecules are linked by $\text{O}-\text{H}\cdots\text{O}$ hydrogen-bonding interactions into a structural ladder motif parallel to the a axis.

Related literature

For related structures, see: Sieroń (2007) [phenazinium perchlorate]; Plasseraud *et al.* (2009) [phenazinium trifluoromethanesulfonate]; Braga *et al.* (2010) [phenazinium chloride and phenazine monohydrate]; G.-X. Zhang *et al.* (2012) [phenazinium bromide]; N.-Q. Zhang *et al.* (2012) [phenazinium methanesulfonate]. For copper(II) salts of phenazine, see: Schneider *et al.* (2007). For graph-set analysis of hydrogen bonding, see: Bernstein *et al.* (1995).



Experimental

Crystal data

$\text{C}_{12}\text{H}_9\text{N}_2^+\cdot\text{HSO}_4^-\cdot\text{H}_2\text{O}$

$M_r = 296.30$

Triclinic, $P\bar{1}$

$a = 5.6565 (4)\text{ \AA}$

$b = 10.4019 (6)\text{ \AA}$

$c = 10.9500 (5)\text{ \AA}$

$\alpha = 89.693 (4)^\circ$

$\beta = 87.202 (5)^\circ$

$\gamma = 76.412 (5)^\circ$

$V = 625.49 (6)\text{ \AA}^3$

$Z = 2$

$\text{Cu K}\alpha$ radiation

$\mu = 2.53\text{ mm}^{-1}$

$T = 120\text{ K}$

$0.45 \times 0.40 \times 0.30\text{ mm}$

Data collection

Agilent SuperNova (Dual, Cu at zero, Atlas) diffractometer
Absorption correction: multi-scan (*CrysAlis PRO*; Agilent, 2011)
 $T_{\min} = 0.786$, $T_{\max} = 1.000$

3789 measured reflections
2341 independent reflections
2276 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.013$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.032$
 $wR(F^2) = 0.088$
 $S = 1.09$
2341 reflections
193 parameters

H atoms treated by a mixture of independent and constrained refinement
 $\Delta\rho_{\max} = 0.30\text{ e \AA}^{-3}$
 $\Delta\rho_{\min} = -0.39\text{ e \AA}^{-3}$

Table 1
Hydrogen-bond geometry (\AA , $^\circ$).

$D-\text{H}\cdots A$	$D-\text{H}$	$\text{H}\cdots A$	$D\cdots A$	$D-\text{H}\cdots A$
N1—H1 \cdots O1	0.86 (2)	1.81 (2)	2.6685 (18)	173.3 (19)
O2—H2 \cdots O1 <i>S</i>	0.93 (2)	1.59 (2)	2.5223 (16)	177 (2)
O1 <i>S</i> —H1 <i>A</i> \cdots O4 ⁱ	0.89 (2)	1.87 (2)	2.7577 (18)	176 (2)
O1 <i>S</i> —H1 <i>B</i> \cdots O3 ⁱⁱ	0.84 (2)	1.90 (2)	2.7405 (18)	173 (2)
C6—H6 \cdots N8 ⁱⁱⁱ	0.93	2.61	3.538 (2)	172

Symmetry codes: (i) $x - 1, y, z$; (ii) $-x, -y + 1, -z + 2$; (iii) $-x - 2, -y + 2, -z + 1$.

Data collection: *CrysAlis PRO* (Agilent, 2011); cell refinement: *CrysAlis PRO*; data reduction: *CrysAlis PRO*; program(s) used to solve structure: *SHELXTL* (Sheldrick, 2008); program(s) used to refine structure: *SHELXTL*; molecular graphics: *SHELXTL* and *Mercury* (Macrae *et al.*, 2008); software used to prepare material for publication: *SHELXL97* (Sheldrick, 2008), *enCIFer* (Allen *et al.*, 2004) and *publCIF* (Westrip, 2010).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: SJ5299).

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supporting information

Acta Cryst. (2013). E69, o471 [doi:10.1107/S160053681300562X]

Phenazin-5-ium hydrogen sulfate monohydrate

Joseph deGeorge, Christopher P. Landee and Mark M. Turnbull

S1. Comment

Phenazinium bisulfate monohydrate (Figure 1) crystallized originally as a biproduct of our work with copper (II) salts of phenazine (Schneider, *et al.*, 2007). The phenazinium ions crystallize as weakly hydrogen bonded centrosymmetric dimers (see Figure 2), forming $R^2_2(8)$ rings (Bernstein *et al.*, 1995), similar to the structures of the chloride [Braga, *et al.*, 2010] and perchlorate salts [Sierón, 2007] and to the phenazinium trifluoromethanesulfonate:phenazine co-crystal [Plasseraud, *et al.*, 2009]. The phenazinium proton is involved in a strong hydrogen bond to one of the bisulfate oxygen atoms [$d_{D\cdots A} = 2.6685(18)$ Å] (see Figure 1). The phenazinium rings are stacked parallel to the a -axis with a distance of 3.9156(9) Å between the ring centroids of the diazine rings and a slip angle of 30.1°.

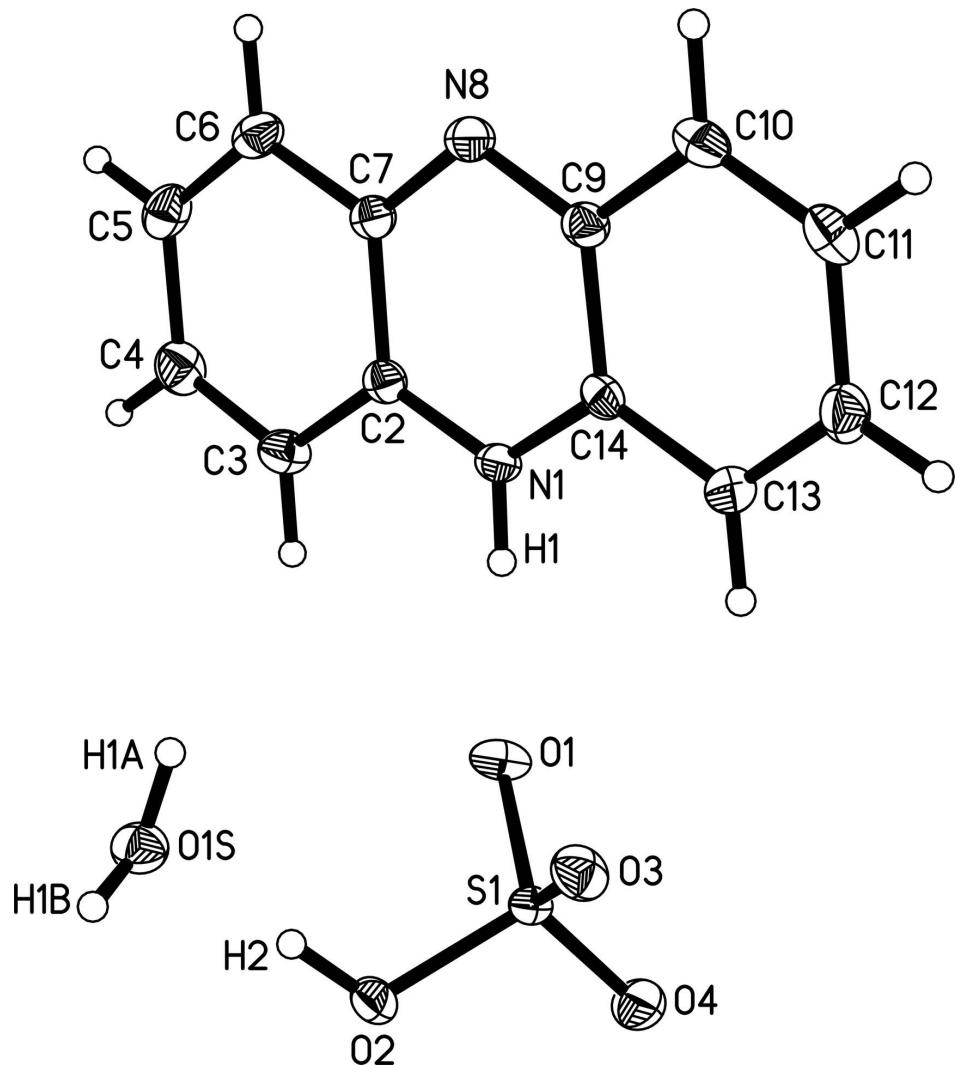
Perhaps the most interesting aspect of the structure results from the hydrogen bonding between the bisulfate anions and the solvent water molecule. This results in the formation of a ladder motif that runs parallel to the a -axis (see Figure 3). Each bisulfate ion serves as a hydrogen bond donor to one water molecule and a hydrogen bond acceptor from a second water molecule forming the rails of the ladder, of form $C^2_2(6)$. The rungs are formed *via* a second water-donor/bisulfate-acceptor pair, which generates rings within the ladder structure (two rungs and two rail sections in each ring), $R^4_4(12)$. There are two chemically different rings formed in this case since one involves rail sections with water molecules serving as the hydrogen bond donor and the other involves the bisulfate ion serving as the hydrogen bond donor.

S2. Experimental

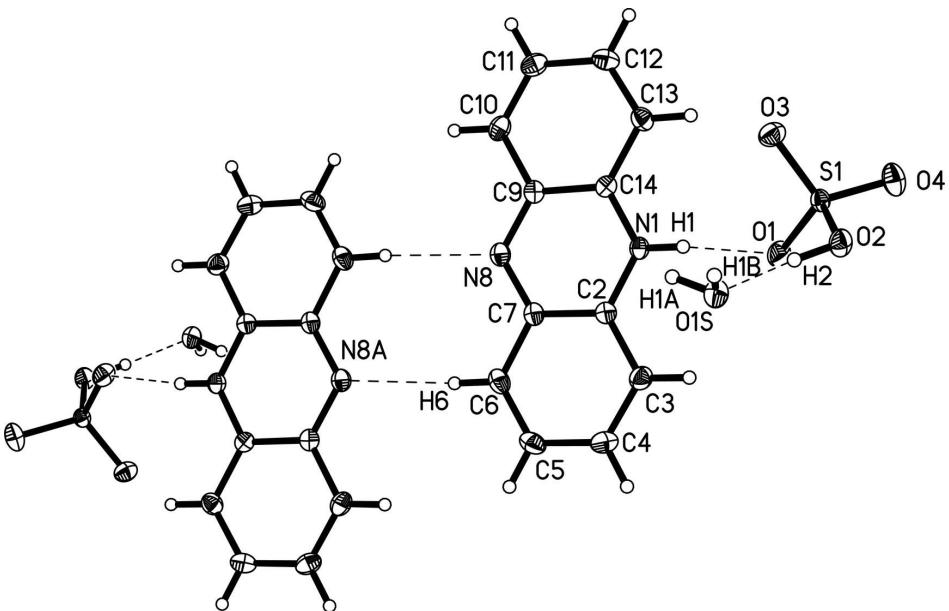
Phenazine was dissolved methanol (90 ml) to which 40% aqueous sulfuric acid (2.5 ml) had been added. Small, prismatic, ruby red crystals formed over the course of two months of slow evaporation at room temperature.

S3. Refinement

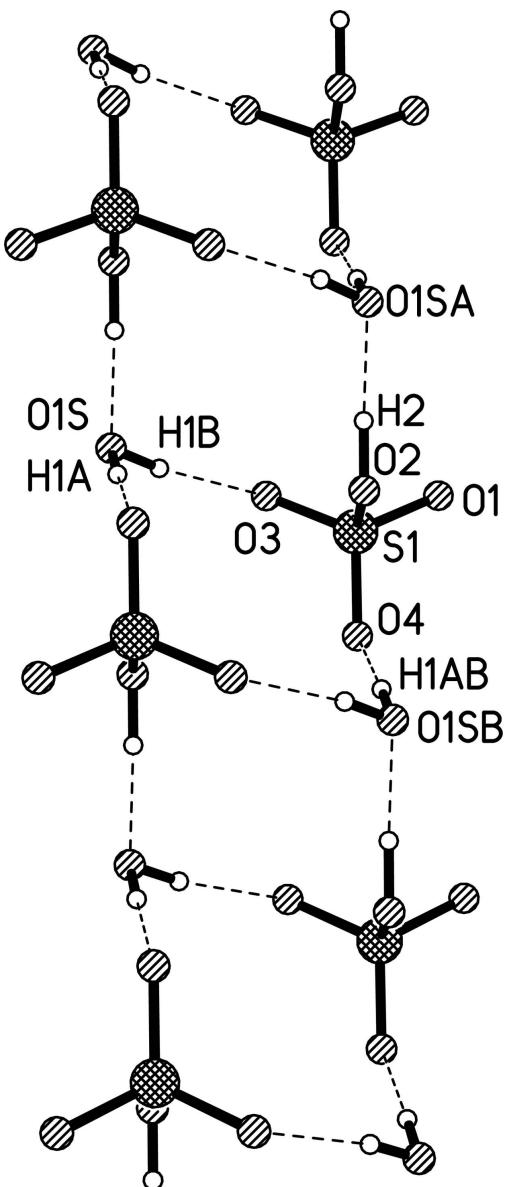
All H-atoms bound to carbon were refined using a riding model with $d(C—H) = 0.93$ Å, $U_{iso}=1.2U_{eq}(C)$. Hydrogen atoms bonded to oxygen or nitrogen atoms were located in a difference map and their positions refined using fixed isotropic U values. There are two Level-B warnings in the checkCIF file for short intermolecular H···H distances. These result from the very strong hydrogen bond between the bisulfate ion and the solvent water molecule ($d_{D\cdots A} = 2.5223(16)$ Å).

**Figure 1**

Thermal ellipsoid plot (50% probability) of compound 1. Hydrogen atoms are shown as spheres of arbitrary size and only hydrogen atoms whose positions were refined are labeled.

**Figure 2**

Thermal ellipsoid plot of 1 (50% probability) showing two inversion related asymmetric units. Only those H-atoms involved in hydrogen bonding are labeled. Hydrogen atoms are shown as spheres of arbitrary size.

**Figure 3**

Packing diagram showing the structure of the ladder motif formed by hydrogen bonding between the bisulfate ions and water molecules. Details of the hydrogen bonding may be found in Table 1.

Phenazin-5-i um hydrogen sulfate monohydrate

Crystal data

$C_{12}H_9N_2^+ \cdot HSO_4^- \cdot H_2O$
 $M_r = 296.30$
Triclinic, $P\bar{1}$
Hall symbol: -P 1
 $a = 5.6565 (4)$ Å
 $b = 10.4019 (6)$ Å
 $c = 10.9500 (5)$ Å
 $\alpha = 89.693 (4)^\circ$
 $\beta = 87.202 (5)^\circ$

$\gamma = 76.412 (5)^\circ$
 $V = 625.49 (6)$ Å³
 $Z = 2$
 $F(000) = 308$
 $D_x = 1.573$ Mg m⁻³
Cu $K\alpha$ radiation, $\lambda = 1.54184$ Å
Cell parameters from 3015 reflections
 $\theta = 4.0\text{--}73.7^\circ$
 $\mu = 2.53$ mm⁻¹

$T = 120\text{ K}$

Prism, red

 $0.45 \times 0.40 \times 0.30\text{ mm}$ *Data collection*Agilent SuperNova (Dual, Cu at zero, Atlas)
diffractometerRadiation source: SuperNova (Cu) X-ray
Source

Mirror monochromator

Detector resolution: 10.6501 pixels mm^{-1} ω scansAbsorption correction: multi-scan
(*CrysAlis PRO*; Agilent, 2011) $T_{\min} = 0.786, T_{\max} = 1.000$

3789 measured reflections

2341 independent reflections

2276 reflections with $I > 2\sigma(I)$ $R_{\text{int}} = 0.013$ $\theta_{\max} = 70.1^\circ, \theta_{\min} = 4.0^\circ$ $h = -6 \rightarrow 6$ $k = -12 \rightarrow 12$ $l = -13 \rightarrow 10$ *Refinement*Refinement on F^2

Least-squares matrix: full

 $R[F^2 > 2\sigma(F^2)] = 0.032$ $wR(F^2) = 0.088$ $S = 1.09$

2341 reflections

193 parameters

0 restraints

Primary atom site location: structure-invariant
direct methodsSecondary atom site location: difference Fourier
mapHydrogen site location: inferred from
neighbouring sitesH atoms treated by a mixture of independent
and constrained refinement $w = 1/[\sigma^2(F_o^2) + (0.0466P)^2 + 0.3904P]$
where $P = (F_o^2 + 2F_c^2)/3$ $(\Delta/\sigma)_{\max} < 0.001$ $\Delta\rho_{\max} = 0.30\text{ e } \text{\AA}^{-3}$ $\Delta\rho_{\min} = -0.39\text{ e } \text{\AA}^{-3}$ *Special details*

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) etc. and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	x	y	z	$U_{\text{iso}}^*/U_{\text{eq}}$
N1	-0.2593 (2)	0.82964 (13)	0.67912 (12)	0.0146 (3)
H1	-0.121 (4)	0.782 (2)	0.6983 (18)	0.018*
C2	-0.3721 (3)	0.78622 (15)	0.58835 (14)	0.0147 (3)
C3	-0.2635 (3)	0.66885 (16)	0.52306 (15)	0.0196 (3)
H3	-0.1104	0.6194	0.5420	0.024*
C4	-0.3861 (3)	0.62898 (17)	0.43183 (15)	0.0223 (4)
H4	-0.3161	0.5514	0.3890	0.027*
C5	-0.6203 (3)	0.70454 (17)	0.40110 (15)	0.0217 (4)
H5	-0.6999	0.6760	0.3379	0.026*
C6	-0.7286 (3)	0.81763 (17)	0.46292 (15)	0.0192 (3)
H6	-0.8810	0.8660	0.4416	0.023*
C7	-0.6090 (3)	0.86222 (15)	0.56042 (14)	0.0152 (3)
N8	-0.7194 (2)	0.97138 (13)	0.62387 (12)	0.0170 (3)

C9	-0.6022 (3)	1.00957 (15)	0.71603 (14)	0.0156 (3)
C10	-0.7157 (3)	1.12367 (16)	0.78748 (15)	0.0195 (3)
H10	-0.8713	1.1714	0.7708	0.023*
C11	-0.5958 (3)	1.16250 (16)	0.88007 (15)	0.0211 (4)
H11	-0.6713	1.2364	0.9269	0.025*
C12	-0.3575 (3)	1.09182 (16)	0.90608 (15)	0.0209 (4)
H12	-0.2782	1.1214	0.9688	0.025*
C13	-0.2415 (3)	0.98128 (16)	0.84123 (15)	0.0186 (3)
H13	-0.0857	0.9352	0.8597	0.022*
C14	-0.3633 (3)	0.93855 (15)	0.74565 (14)	0.0142 (3)
S1	0.28595 (6)	0.63836 (3)	0.83817 (3)	0.01403 (14)
O1	0.1783 (2)	0.67614 (11)	0.72006 (10)	0.0209 (3)
O2	0.3077 (2)	0.48835 (11)	0.85361 (11)	0.0193 (3)
H2	0.155 (4)	0.469 (2)	0.8530 (18)	0.023*
O3	0.1275 (2)	0.70674 (11)	0.93855 (11)	0.0214 (3)
O4	0.5331 (2)	0.65395 (12)	0.84063 (12)	0.0247 (3)
O1S	-0.0979 (2)	0.42771 (13)	0.84748 (11)	0.0207 (3)
H1A	-0.221 (4)	0.498 (2)	0.8448 (19)	0.025*
H1B	-0.120 (4)	0.387 (2)	0.912 (2)	0.025*

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
N1	0.0135 (6)	0.0134 (6)	0.0161 (6)	-0.0012 (5)	-0.0020 (5)	0.0022 (5)
C2	0.0157 (7)	0.0149 (7)	0.0140 (7)	-0.0043 (6)	-0.0002 (6)	0.0024 (6)
C3	0.0195 (8)	0.0184 (8)	0.0189 (8)	-0.0002 (6)	-0.0016 (6)	-0.0003 (6)
C4	0.0276 (9)	0.0197 (8)	0.0190 (8)	-0.0043 (7)	-0.0006 (7)	-0.0036 (6)
C5	0.0248 (9)	0.0272 (9)	0.0158 (8)	-0.0108 (7)	-0.0044 (6)	-0.0006 (6)
C6	0.0170 (8)	0.0238 (8)	0.0179 (8)	-0.0062 (6)	-0.0041 (6)	0.0040 (6)
C7	0.0144 (7)	0.0163 (7)	0.0154 (7)	-0.0045 (6)	-0.0005 (6)	0.0033 (6)
N8	0.0152 (7)	0.0173 (7)	0.0183 (7)	-0.0030 (5)	-0.0017 (5)	0.0022 (5)
C9	0.0152 (7)	0.0147 (7)	0.0169 (7)	-0.0035 (6)	-0.0008 (6)	0.0028 (6)
C10	0.0182 (8)	0.0150 (8)	0.0229 (8)	0.0007 (6)	0.0006 (6)	0.0011 (6)
C11	0.0264 (9)	0.0137 (8)	0.0215 (8)	-0.0019 (6)	0.0011 (7)	-0.0012 (6)
C12	0.0276 (9)	0.0181 (8)	0.0183 (8)	-0.0074 (7)	-0.0039 (7)	-0.0013 (6)
C13	0.0184 (8)	0.0181 (8)	0.0196 (8)	-0.0040 (6)	-0.0048 (6)	0.0016 (6)
C14	0.0159 (7)	0.0115 (7)	0.0150 (7)	-0.0034 (6)	0.0007 (6)	0.0020 (6)
S1	0.0126 (2)	0.0130 (2)	0.0160 (2)	-0.00190 (14)	-0.00241 (14)	0.00158 (14)
O1	0.0199 (6)	0.0211 (6)	0.0178 (6)	0.0032 (5)	-0.0026 (5)	0.0026 (4)
O2	0.0169 (6)	0.0131 (6)	0.0272 (6)	-0.0019 (4)	-0.0025 (5)	0.0015 (4)
O3	0.0240 (6)	0.0181 (6)	0.0201 (6)	-0.0012 (5)	0.0001 (5)	-0.0022 (4)
O4	0.0172 (6)	0.0248 (6)	0.0338 (7)	-0.0080 (5)	-0.0048 (5)	0.0066 (5)
O1S	0.0175 (6)	0.0211 (6)	0.0223 (6)	-0.0022 (5)	-0.0007 (5)	0.0008 (5)

Geometric parameters (\AA , $^\circ$)

N1—C2	1.342 (2)	C9—C14	1.431 (2)
N1—C14	1.347 (2)	C10—C11	1.360 (2)

N1—H1	0.86 (2)	C10—H10	0.9300
C2—C3	1.412 (2)	C11—C12	1.417 (2)
C2—C7	1.433 (2)	C11—H11	0.9300
C3—C4	1.363 (2)	C12—C13	1.366 (2)
C3—H3	0.9300	C12—H12	0.9300
C4—C5	1.428 (2)	C13—C14	1.410 (2)
C4—H4	0.9300	C13—H13	0.9300
C5—C6	1.359 (2)	S1—O4	1.4465 (12)
C5—H5	0.9300	S1—O3	1.4595 (12)
C6—C7	1.427 (2)	S1—O1	1.4685 (12)
C6—H6	0.9300	S1—O2	1.5452 (11)
C7—N8	1.340 (2)	O2—H2	0.93 (2)
N8—C9	1.345 (2)	O1S—H1A	0.89 (2)
C9—C10	1.427 (2)	O1S—H1B	0.84 (2)
C2—N1—C14	122.42 (14)	C10—C9—C14	118.10 (14)
C2—N1—H1	117.8 (13)	C11—C10—C9	119.91 (15)
C14—N1—H1	119.6 (13)	C11—C10—H10	120.0
N1—C2—C3	121.43 (14)	C9—C10—H10	120.0
N1—C2—C7	117.80 (14)	C10—C11—C12	120.87 (15)
C3—C2—C7	120.77 (14)	C10—C11—H11	119.6
C4—C3—C2	119.09 (15)	C12—C11—H11	119.6
C4—C3—H3	120.5	C13—C12—C11	121.57 (15)
C2—C3—H3	120.5	C13—C12—H12	119.2
C3—C4—C5	121.01 (15)	C11—C12—H12	119.2
C3—C4—H4	119.5	C12—C13—C14	118.48 (15)
C5—C4—H4	119.5	C12—C13—H13	120.8
C6—C5—C4	120.90 (15)	C14—C13—H13	120.8
C6—C5—H5	119.5	N1—C14—C13	121.24 (14)
C4—C5—H5	119.5	N1—C14—C9	117.71 (14)
C5—C6—C7	120.12 (15)	C13—C14—C9	121.05 (14)
C5—C6—H6	119.9	O4—S1—O3	113.27 (7)
C7—C6—H6	119.9	O4—S1—O1	112.32 (7)
N8—C7—C6	120.05 (14)	O3—S1—O1	110.75 (7)
N8—C7—C2	121.85 (14)	O4—S1—O2	104.85 (7)
C6—C7—C2	118.09 (14)	O3—S1—O2	107.93 (7)
C7—N8—C9	118.37 (14)	O1—S1—O2	107.28 (7)
N8—C9—C10	120.09 (14)	S1—O2—H2	111.1 (13)
N8—C9—C14	121.81 (14)	H1A—O1S—H1B	107 (2)
C14—N1—C2—C3	-177.42 (14)	C7—N8—C9—C10	-178.66 (14)
C14—N1—C2—C7	1.9 (2)	C7—N8—C9—C14	1.3 (2)
N1—C2—C3—C4	179.87 (15)	N8—C9—C10—C11	-179.55 (15)
C7—C2—C3—C4	0.6 (2)	C14—C9—C10—C11	0.5 (2)
C2—C3—C4—C5	0.5 (3)	C9—C10—C11—C12	0.7 (2)
C3—C4—C5—C6	-0.7 (3)	C10—C11—C12—C13	-1.3 (3)
C4—C5—C6—C7	-0.3 (3)	C11—C12—C13—C14	0.6 (2)
C5—C6—C7—N8	-177.83 (15)	C2—N1—C14—C13	179.42 (14)

C5—C6—C7—C2	1.4 (2)	C2—N1—C14—C9	−0.6 (2)
N1—C2—C7—N8	−1.6 (2)	C12—C13—C14—N1	−179.43 (15)
C3—C2—C7—N8	177.64 (15)	C12—C13—C14—C9	0.6 (2)
N1—C2—C7—C6	179.15 (13)	N8—C9—C14—N1	−1.1 (2)
C3—C2—C7—C6	−1.6 (2)	C10—C9—C14—N1	178.86 (14)
C6—C7—N8—C9	179.27 (14)	N8—C9—C14—C13	178.92 (14)
C2—C7—N8—C9	0.1 (2)	C10—C9—C14—C13	−1.1 (2)

Hydrogen-bond geometry (Å, °)

D—H···A	D—H	H···A	D···A	D—H···A
N1—H1···O1	0.86 (2)	1.81 (2)	2.6685 (18)	173.3 (19)
O2—H2···O1 <i>S</i>	0.93 (2)	1.59 (2)	2.5223 (16)	177 (2)
O1 <i>S</i> —H1 <i>A</i> ···O4 ⁱ	0.89 (2)	1.87 (2)	2.7577 (18)	176 (2)
O1 <i>S</i> —H1 <i>B</i> ···O3 ⁱⁱ	0.84 (2)	1.90 (2)	2.7405 (18)	173 (2)
C6—H6···N8 ⁱⁱⁱ	0.93	2.61	3.538 (2)	172

Symmetry codes: (i) $x-1, y, z$; (ii) $-x, -y+1, -z+2$; (iii) $-x-2, -y+2, -z+1$.