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Redetermination of the crystal structures of rare-earth trirhodium diboride $RERh_3B_2$ ($RE = Pr, Nd$ and Sm) from single-crystal X-ray data

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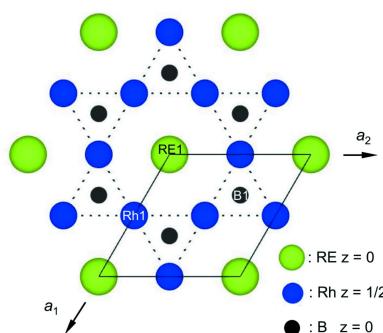
The crystal structures of the rare-earth (RE) trirhodium diborides praseodymium trirhodium diboride, $PrRh_3B_2$, neodymium trirhodium diboride, $NdRh_3B_2$, and samarium trirhodium diboride, $SmRh_3B_2$, were refined on the basis of single-crystal X-ray diffraction data. The crystal chemistry of $RERh_3B_2$ (RE : Pr, Nd, and Sm) compounds has previously been analyzed mainly on the basis of powder samples [Ku *et al.* (1980). *Solid State Commun.* **35**, 91–96], and no structural investigation by single-crystal X-ray diffraction has been reported so far. The crystal structures of the three hexagonal $RERh_3B_2$ compounds are isotopic with that of $CeRh_3B_2$; RE , Rh and B sites are situated on special positions with site symmetry $6/mmm$ (Wyckoff position 1a), mmm (3g) and $\bar{6}m2$ (2c), respectively. In comparison with the previous powder X-ray study of hexagonal $RERh_3B_2$, the present redetermination against single-crystal X-ray data has allowed for the modeling of all atoms with anisotropic displacement parameters (ADPs). The ADPs of the Rh atom in each of the structures result in an elongated displacement ellipsoid in the direction of the stacking of the Rh kagomé-type layer. The features of obtained ADPs of atoms are discussed in relation to $RERh_3B_2$ -type and analogous structures.

1. Chemical context

$CeCo_3B_2$ -type $RERh_3B_2$ (RE = rare-earth element) compounds exhibit anomalous ferromagnetic properties (Malik *et al.*, 1983; Yamada *et al.*, 2004), and the unit-cell parameters of these compounds have been reported using powder X-ray diffraction (XRD) data (Ku *et al.*, 1980; Ku & Meissner, 1981). Higashi *et al.* (1987) analyzed the crystal structure of $CeRh_3B_2$ by using single-crystal XRD data and discussed the characteristics of the anisotropic atomic displacement parameters (ADP) of atoms in $CeRh_3B_2$ in relation to the structure. We report here the results of structural refinements using single crystals of $RERh_3B_2$ (RE = Pr, Nd, and Sm) grown by the arc-melting method.

2. Structural commentary

The crystal structures of hexagonal $RERh_3B_2$ (RE : La–Gd) compounds are isotopic with $CeCo_3B_2$ and crystallize in space-group type $P6/mmm$ (Kuz'ma *et al.*, 1969). The $CeCo_3B_2$ type of structure is ordered and can be derived from the $CaCu_5$ type of structure, whereby two distinct atoms (Rh and B) occupy the corresponding Cu sites. Each B atom is surrounded by six Rh atoms, forming a trigonal prism. Such $[BRh_6]$



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trigonal prisms constitute a honeycomb structure and *RE* atoms are accommodated at the centers of the twelve $[RERh_{12}]$ hexagonal prisms, as shown in Fig. 1. The $RERh_3B_2$ type of structure can also be described as being built up of kagomé layers of Rh atoms stacked along the *c* axis with an $\alpha\alpha$ stacking sequence and with B and *RE* atoms at the centers of the Rh triangular and hexagonal prisms, respectively.

The unit-cell parameters *a* and *c* and the unit-cell volume *V* of $RERh_3B_2$ (*RE* = La–Sm) compounds are shown in Fig. 2. The decrease in unit-cell volume results from the lanthanide contraction. The lattice parameters *a* and *c* decrease and increase, respectively. These anisotropic changes in the unit-cell parameters are consistent with those of a previous report using powder XRD analysis (Malik *et al.*, 1983).

The anisotropic change in the unit-cell parameters can be explained by the change in interatomic distances due to the lanthanide contraction. The ranges of B–Rh and *RE*–Rh distances are 2.2129 (1)–2.2151 (1) Å and 3.1370 (1)–3.1447 (1) Å (Table 1), respectively, which are close to the values of the sums of the atomic radii ($r_{Rh} = 1.35$ Å, $r_B = 0.85$ Å, $r_{Pr} = 1.84$ Å, $r_{Nd} = 1.83$ Å, and $r_{Sm} = 1.81$ Å; Daane *et al.*, 1954; Spedding *et al.*, 1956; Zachariasen, 1973). The *RE*–Rh interatomic distances decrease due to the effect of the lanthanoid contraction. Rh–Rh interatomic distances in the *ab* plane also decrease with a decrease in *RE*–Rh distances. By contrast, the Rh–Rh interatomic distances along the *c* axis increase. This causes the $[RERh_{12}]$ hexagonal and $[BRh_6]$ trigonal prisms to shrink horizontally and stretch vertically, resulting in decreases of the volumes of the hexagonal and trigonal prisms. Therefore, the unit-cells of $RERh_3B_2$ compounds change anisotropically, suggesting that the unit-cell changes elastically in response to the substitution of elements of different sizes at the *RE* site.

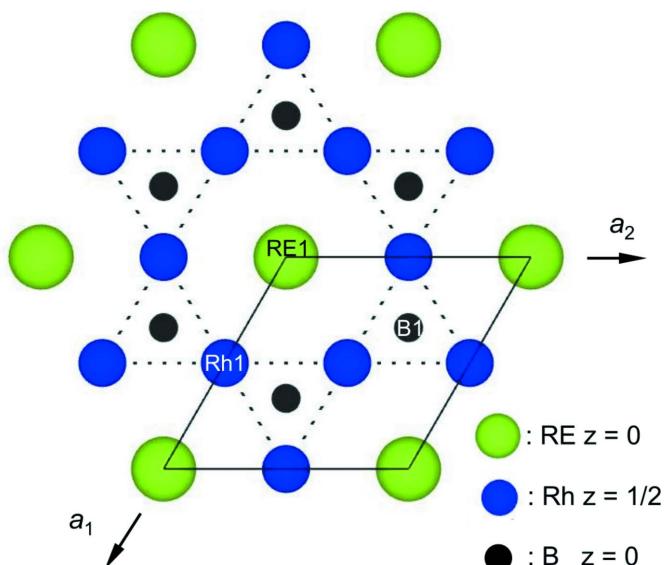


Figure 1

Structure of $RERh_3B_2$ compounds (space group: $P6/mmm$) as viewed along the *c* axis. B and *RE* atoms settle in the center of the trigonal and hexagonal prisms, respectively.

Table 1
Selected bond lengths (Å) in $RERh_3B_2$ (*RE* = Pr, Nd and Sm).

	PrRh ₃ B ₂	NdRh ₃ B ₂	SmRh ₃ B ₂
<i>RE</i> – <i>RE</i> × 2	3.1084 (1)	3.1107 (1)	3.1190 (1)
<i>RE</i> – <i>RE</i> × 6	5.4676 (4)	5.4527 (3)	5.4438 (3)
<i>RE</i> –Rh × 12	3.1447 (1)	3.1388 (1)	3.1370 (1)
<i>RE</i> –B × 6	3.1557 (2)	3.1481 (1)	3.1430 (1)
B–Rh × 6	2.2151 (1)	2.2129 (1)	2.2140 (1)
B–B × 3	3.1084 (1)	3.1107 (1)	3.1190 (1)
B–B × 3	3.1567 (2)	3.1481 (1)	3.1430 (1)
Rh–Rh × 4	2.7338 (2)	2.7264 (1)	2.7219 (1)
Rh–Rh × 2	3.1084 (1)	3.1107 (1)	3.1190 (1)

The obtained ADPs for each atom are summarized in Table 2. The displacement ellipsoid of the Rh atom shows a larger anisotropy than those of the B and *RE* atoms, as shown in Fig. 3. The U_{33} of Rh atoms is approximately 2.1–2.6 times

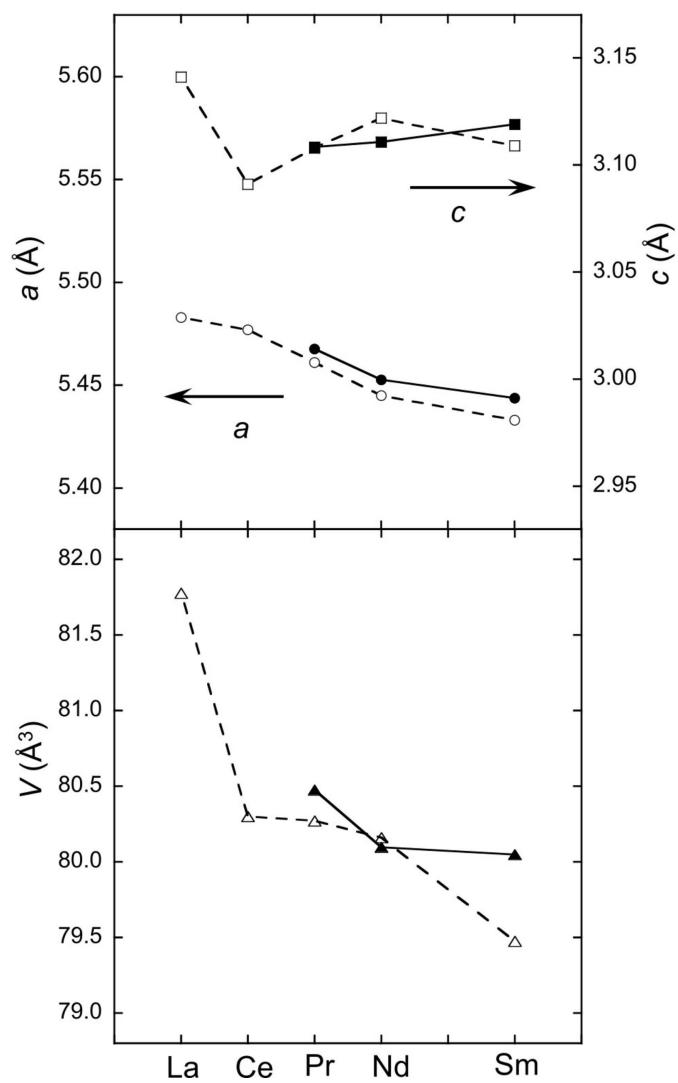


Figure 2

Unit-cell parameters *a* (circles), *c* (squares) and unit-cell volume *V* (triangles) of $RERh_3B_2$ compounds. Closed and open marks refer to this study and previous work (Malik *et al.*, 1983), respectively.

Table 2Atomic displacement parameters of *RE*, Rh, and B atoms in *RERh₃B₂* (*RE* = Pr, Nd, and Sm).

Atom	<i>U</i> ₁₁ (Å ²)	<i>U</i> ₂₂ (Å ²)	<i>U</i> ₃₃ (Å ²)	<i>U</i> ₁₂ (Å ²)	<i>U</i> _{eq} (10 ⁻³ Å ²)
<i>PrRh₃B₂</i>					
Pr	0.00861 (18)	0.00861	0.00780 (20)	0.00430 (9)	8.35 (1)
Rh	0.00495 (16)	0.00386 (18)	0.01040 (20)	0.00193 (9)	6.53 (1)
B	0.0095 (16)	0.0095	0.009 (2)	0.0048 (8)	9.3 (10)
<i>NdRh₃B₂</i>					
Nd	0.00896 (10)	0.00896	0.00662 (12)	0.00448 (5)	8.18 (9)
Rh	0.00492 (9)	0.00390 (11)	0.01104 (12)	0.00195 (5)	6.74 (8)
B	0.0100 (9)	0.0100	0.0079 (12)	0.0050 (4)	9.3 (6)
<i>SmRh₃B₂</i>					
Sm	0.00841 (12)	0.00841	0.00658 (14)	0.00420 (6)	7.80 (10)
Rh	0.00502 (11)	0.00389 (13)	0.01287 (14)	0.00194 (6)	7.39 (10)
B	0.0085 (10)	0.0085	0.0102 (15)	0.0043 (5)	9.1 (7)

larger than *U*₁₁, which means that the displacement ellipsoids of Rh atoms are elongated along the *c* axis. The displacement ellipsoids of Rh atoms with large anisotropy correspond to the anisotropic electric resistivity of *RERh₃B₂* compounds (Yamada *et al.*, 2004; Obiraki *et al.*, 2006). The ADPs of *RE* atoms are described as displacement ellipsoids suppressed in the *c* axis (*U*₁₁ < *U*₃₃). The feature of displacement ellipsoids of Rh and *RE* atoms is attributed to the unusually short *RE*–*RE* interatomic distances of 3.1084 (1)–3.1190 (1) Å, which are much shorter (15%) than the distance in the metal Pr, Nd, and Sm with hexagonal close-packed structures, (*i.e.*, 3.67, 3.66, and 3.62 Å, respectively). The short *RE*–*RE* interatomic distance is a common feature of the CeCo₃B₂ type of structure. Anisotropy of electric or thermal conductivity is also expected to be observed in CeRh₃B₂ compounds.

The obtained anisotropic ADPs of each atom in the structures of *RERh₃B₂* compounds can be discussed in terms of the nucleation of interstitial atoms or layers in PrRh_{4.8}B₂ (Higashi *et al.*, 1988). Higashi *et al.* (1988) discovered a new layered structure, namely, PrRh_{4.8}B₂, which is regarded as a stacking variant of a modified PrRh₃B₂ structure. The interstitial single Rh layer is positioned between the Rh kagomé layers of the

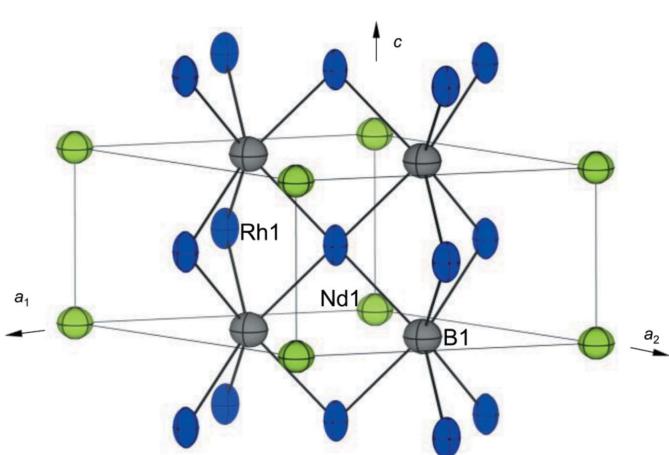
modified PrRh₃B₂ blocks. The displacement ellipsoid in the stacking direction of the Rh atom in the PrRh₃B₂ structure implies that the Rh kagomé layer in PrRh₃B₂ could be a base for the nucleation of interstitial atoms or layers. The appearance of disordered La_{1-x}Rh₃B₂ type and/or Nd_{1-x}Rh_xRh₃B₂ type of structures (Ohtani *et al.*, 1983; Vlasse *et al.*, 1983; Ku *et al.*, 1985) might be associated with the anisotropic ADPs of Rh and *RE* atoms.

3. Synthesis and crystallization

RERh₃B₂ (*RE* = Pr, Nd, and Sm) single crystals were grown using the arc-melting method. The starting materials used were *RE* elements (99.9%), along with Rh (99.95%), and B (99.5%). They were weighed at an atomic ratio of (*RE*+3Rh+2B), and the mixtures of the starting materials were placed in an argon-arc melting furnace (ACM-01, Diavac). Each product was remelted three times to improve homogeneity. The grown crystals were composed of homogeneous *RERh₃B₂*, and the atomic ratio Rh/*RE* was confirmed to be 3.00 by energy dispersive X-ray spectroscopy.

4. Refinement details

Crystal data, data collection and structure refinement details are summarized in Table 3. A reciprocal space plot using all reflection data was in good agreement with the hexagonal lattice (*a* ≈ 5 Å and *c* ≈ 3 Å), and there was no evidence of superstructure reflections. The refinement was conducted under the assumption that the space group type was *P*6/mmm, as reported by Ku *et al.* (1980). Based on structural reports of La_{1-x}Rh₃B₂ and Nd_{1-x}Rh_xRh₃B₂, we determined whether Rh substitution and vacancies at the *RE* site were possible; however, the results were negative. Therefore, we concluded that the *RE* sites were completely occupied by *RE* elements. A correction for isotropic extinction was applied during the least-squares refinements. The final refinements were performed by applying anisotropic ADPs to each atom. The remaining electron densities located 0.7–0.6 Å around rhodium and *RE* heavy elements are censoring effects caused by the finite Fourier series.

**Figure 3**

Displacement ellipsoids of each atom in NdRh₃B₂, with displacement ellipsoids drawn at the 99% probability level.

Table 3

Experimental details.

	PrRh ₃ B ₂	NdRh ₃ B ₂	SmRh ₃ B ₂
Crystal data			
<i>M</i> _r	471.26	474.59	480.70
Crystal system, space group	Hexagonal, <i>P</i> 6/mmm	Hexagonal, <i>P</i> 6/mmm	Hexagonal, <i>P</i> 6/mmm
Temperature (K)	293	293	293
<i>a</i> , <i>c</i> (Å)	5.4676 (3), 3.10837 (16)	5.4527 (2), 3.11066 (13)	5.4438 (2), 3.11901 (12)
<i>V</i> (Å ³)	80.47 (1)	80.10 (1)	80.05 (1)
<i>Z</i>	1	1	1
Radiation type	Mo <i>K</i> α	Mo <i>K</i> α	Mo <i>K</i> α
μ (mm ⁻¹)	29.43	30.57	32.61
Crystal size (mm)	0.05 × 0.03 × 0.03	0.05 × 0.05 × 0.02	0.06 × 0.05 × 0.02
Data collection			
Diffractometer	XtaLAB Synergy, Dualflex, HyPix	XtaLAB Synergy, Dualflex, HyPix	XtaLAB Synergy, Dualflex, HyPix
Absorption correction	Numerical (<i>CrysAlis PRO</i> ; Rigaku OD, 2021)	Numerical (<i>CrysAlis PRO</i> ; Rigaku OD, 2021)	Numerical (<i>CrysAlis PRO</i> ; Rigaku OD, 2021)
<i>T</i> _{min} , <i>T</i> _{max}	0.423, 0.601	0.424, 0.611	0.324, 0.542
No. of measured, independent and observed [<i>I</i> > 2σ(<i>I</i>)] reflections	733, 131, 126	827, 131, 130	696, 129, 128
<i>R</i> _{int}	0.017	0.010	0.011
(sin <θ>/<λ>) _{max} (Å ⁻¹)	0.909	0.908	0.907
Refinement			
<i>R</i> [<i>F</i> ² > 2σ(<i>F</i> ²)], <i>wR</i> (<i>F</i> ²), <i>S</i>	0.018, 0.053, 1.21	0.012, 0.032, 1.15	0.012, 0.032, 1.13
No. of reflections	131	131	129
No. of parameters	8	8	9
Δρ _{max} , Δρ _{min} (e Å ⁻³)	1.80, -1.18	0.97, -2.46	1.76, -0.97

Computer programs: *CrysAlis PRO* (Rigaku OD, 2021), *SHELXT* (Sheldrick, 2015a), *SHELXL* (Sheldrick, 2015b), *VESTA* (Momma & Izumi, 2011) and *publCIF* (Westrip, 2010).

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Redetermination of the crystal structures of rare-earth trirhodium diboride $RE\text{Rh}_3\text{B}_2$ ($RE = \text{Pr}$, Nd and Sm) from single-crystal X-ray data

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Computing details

For all structures, data collection: *CrysAlis PRO* (Rigaku OD, 2021); cell refinement: *CrysAlis PRO* (Rigaku OD, 2021); data reduction: *CrysAlis PRO* (Rigaku OD, 2021); program(s) used to solve structure: *SHELXT* (Sheldrick, 2015a); program(s) used to refine structure: *SHELXL* (Sheldrick, 2015b); molecular graphics: *VESTA* (Momma & Izumi, 2011); software used to prepare material for publication: *publCIF* (Westrip, 2010).

Praseodymium trirhodium diboride (I)

Crystal data

PrRh_3B_2	$D_x = 9.724 \text{ Mg m}^{-3}$
$M_r = 471.26$	$\text{Mo } K\alpha \text{ radiation, } \lambda = 0.71073 \text{ \AA}$
Hexagonal, $P6/mmm$	Cell parameters from 623 reflections
$a = 5.4676 (3) \text{ \AA}$	$\theta = 4.3\text{--}39.9^\circ$
$c = 3.10837 (16) \text{ \AA}$	$\mu = 29.43 \text{ mm}^{-1}$
$V = 80.47 (1) \text{ \AA}^3$	$T = 293 \text{ K}$
$Z = 1$	Block, metallic
$F(000) = 204$	$0.05 \times 0.03 \times 0.03 \text{ mm}$

Data collection

XtaLAB Synergy, Dualflex, HyPix	$T_{\min} = 0.423$, $T_{\max} = 0.601$
diffractometer	733 measured reflections
Radiation source: micro-focus sealed X-ray	131 independent reflections
tube, PhotonJet (Mo) X-ray Source	126 reflections with $I > 2\sigma(I)$
Mirror monochromator	$R_{\text{int}} = 0.017$
Detector resolution: 10.0000 pixels mm^{-1}	$\theta_{\max} = 40.3^\circ$, $\theta_{\min} = 4.3^\circ$
ω scans	$h = -9 \rightarrow 7$
Absorption correction: numerical	$k = -9 \rightarrow 9$
(CrysAlisPro; Rigaku OD, 2021)	$l = -3 \rightarrow 5$

Refinement

Refinement on F^2	0 restraints
Least-squares matrix: full	$w = 1/[\sigma^2(F_o^2) + (0.0347P)^2]$
$R[F^2 > 2\sigma(F^2)] = 0.018$	where $P = (F_o^2 + 2F_c^2)/3$
$wR(F^2) = 0.053$	$(\Delta/\sigma)_{\max} < 0.001$
$S = 1.21$	$\Delta\rho_{\max} = 1.80 \text{ e } \text{\AA}^{-3}$
131 reflections	$\Delta\rho_{\min} = -1.18 \text{ e } \text{\AA}^{-3}$
8 parameters	

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
Pr1	0.000000	0.000000	0.000000	0.00835 (14)
Rh1	0.500000	0.000000	0.500000	0.00653 (13)
B1	0.333333	0.666667	0.000000	0.0093 (10)

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Pr1	0.00861 (18)	0.00861 (18)	0.0078 (2)	0.00430 (9)	0.000	0.000
Rh1	0.00495 (16)	0.00386 (18)	0.0104 (2)	0.00193 (9)	0.000	0.000
B1	0.0095 (16)	0.0095 (16)	0.009 (2)	0.0048 (8)	0.000	0.000

Geometric parameters (\AA , $^\circ$)

Pr1—Pr1 ⁱ	3.1084 (2)	Pr1—Rh1 ^x	3.1447 (1)
Pr1—Pr1 ⁱⁱ	3.1084 (2)	Rh1—B1 ^{xi}	2.2151 (1)
Pr1—Rh1 ⁱⁱⁱ	3.1447 (1)	Rh1—B1 ^{xii}	2.2151 (1)
Pr1—Rh1 ^{iv}	3.1447 (1)	Rh1—B1 ^{xiii}	2.2151 (1)
Pr1—Rh1	3.1447 (1)	Rh1—B1 ^{xiv}	2.2151 (1)
Pr1—Rh1 ^v	3.1447 (1)	Rh1—Rh1 ^{xv}	2.7338 (2)
Pr1—Rh1 ^{vi}	3.1447 (1)	Rh1—Rh1 ^{xvi}	2.7338 (2)
Pr1—Rh1 ^{vii}	3.1447 (1)	Rh1—Rh1 ^{xii}	2.7338 (2)
Pr1—Rh1 ^{viii}	3.1447 (1)	Rh1—Rh1 ^{xvii}	2.7338 (2)
Pr1—Rh1 ^{ix}	3.1447 (1)	Rh1—Rh1 ⁱ	3.1084 (2)
Pr1—Rh1 ⁱⁱ	3.1447 (1)	Rh1—Rh1 ⁱⁱ	3.1084 (2)
Pr1 ⁱ —Pr1—Pr1 ⁱⁱ	180.0	B1 ^{xiii} —Rh1—Rh1 ^{xv}	51.897 (2)
Pr1 ⁱ —Pr1—Rh1 ⁱⁱⁱ	60.381 (1)	B1 ^{xiv} —Rh1—Rh1 ^{xv}	128.103 (2)
Pr1 ⁱⁱ —Pr1—Rh1 ⁱⁱⁱ	119.619 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvi}	128.103 (1)
Pr1 ⁱ —Pr1—Rh1 ^{iv}	119.619 (1)	B1 ^{xii} —Rh1—Rh1 ^{xvi}	51.897 (1)
Pr1 ⁱⁱ —Pr1—Rh1 ^{iv}	60.381 (1)	B1 ^{xiii} —Rh1—Rh1 ^{xvi}	128.103 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^{iv}	180.0	B1 ^{xiv} —Rh1—Rh1 ^{xvi}	51.897 (2)
Pr1 ⁱ —Pr1—Rh1	60.381 (2)	Rh1 ^{xv} —Rh1—Rh1 ^{xvi}	180.0
Pr1 ⁱⁱ —Pr1—Rh1	119.619 (2)	B1 ^{xi} —Rh1—Rh1 ⁱⁱⁱ	51.896 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1	51.528 (1)	B1 ^{xii} —Rh1—Rh1 ⁱⁱⁱ	128.104 (2)
Rh1 ^{iv} —Pr1—Rh1	128.472 (1)	B1 ^{xiii} —Rh1—Rh1 ⁱⁱⁱ	51.896 (2)
Pr1 ⁱ —Pr1—Rh1 ^v	119.619 (2)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱⁱ	128.104 (1)
Pr1 ⁱⁱ —Pr1—Rh1 ^v	60.381 (2)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱⁱ	60.0
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^v	128.472 (1)	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱⁱ	120.0
Rh1 ^{iv} —Pr1—Rh1 ^v	51.528 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvii}	128.104 (2)

Rh1—Pr1—Rh1 ^v	180.0	B1 ^{xii} —Rh1—Rh1 ^{xvii}	51.896 (2)
Pr1 ⁱ —Pr1—Rh1 ^{vi}	60.381 (2)	B1 ^{xiii} —Rh1—Rh1 ^{xvii}	128.104 (2)
Pr1 ⁱⁱ —Pr1—Rh1 ^{vi}	119.619 (2)	B1 ^{xiv} —Rh1—Rh1 ^{xvii}	51.896 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^{vi}	51.528 (1)	Rh1 ^{xv} —Rh1—Rh1 ^{xvii}	120.0
Rh1 ^{iv} —Pr1—Rh1 ^{vi}	128.472 (1)	Rh1 ^{xvi} —Rh1—Rh1 ^{xvii}	60.0
Rh1—Pr1—Rh1 ^{vi}	97.678 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ^{xvii}	180.0
Rh1 ^v —Pr1—Rh1 ^{vi}	82.322 (2)	B1 ^{xi} —Rh1—Rh1 ⁱ	45.442 (2)
Pr1 ⁱ —Pr1—Rh1 ^{vii}	119.619 (2)	B1 ^{xii} —Rh1—Rh1 ⁱ	134.558 (2)
Pr1 ⁱⁱ —Pr1—Rh1 ^{vii}	60.381 (2)	B1 ^{xiii} —Rh1—Rh1 ⁱ	134.558 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^{vii}	128.472 (1)	B1 ^{xiv} —Rh1—Rh1 ⁱ	45.442 (2)
Rh1 ^{iv} —Pr1—Rh1 ^{vii}	51.528 (1)	Rh1 ^{xv} —Rh1—Rh1 ⁱ	90.0
Rh1—Pr1—Rh1 ^{vii}	82.322 (2)	Rh1 ^{xvi} —Rh1—Rh1 ⁱ	90.0
Rh1 ^v —Pr1—Rh1 ^{vii}	97.678 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱ	90.0
Rh1 ^{vi} —Pr1—Rh1 ^{vii}	180.0	Rh1 ^{xvii} —Rh1—Rh1 ⁱ	90.0
Pr1 ⁱ —Pr1—Rh1 ^{viii}	60.381 (2)	B1 ^{xi} —Rh1—Rh1 ⁱⁱ	134.558 (2)
Pr1 ⁱⁱ —Pr1—Rh1 ^{viii}	119.619 (2)	B1 ^{xii} —Rh1—Rh1 ⁱⁱ	45.442 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^{viii}	120.763 (4)	B1 ^{xiii} —Rh1—Rh1 ⁱⁱ	45.442 (2)
Rh1 ^{iv} —Pr1—Rh1 ^{viii}	59.238 (4)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱ	134.558 (2)
Rh1—Pr1—Rh1 ^{viii}	97.678 (3)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^v —Pr1—Rh1 ^{viii}	82.322 (3)	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vi} —Pr1—Rh1 ^{viii}	97.678 (3)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vii} —Pr1—Rh1 ^{viii}	82.322 (3)	Rh1 ^{xvii} —Rh1—Rh1 ⁱⁱ	90.0
Pr1 ⁱ —Pr1—Rh1 ^{ix}	119.619 (2)	Rh1 ⁱ —Rh1—Rh1 ⁱⁱ	180.0
Pr1 ⁱⁱ —Pr1—Rh1 ^{ix}	60.381 (2)	B1 ^{xi} —Rh1—Pr1	110.289 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^{ix}	59.238 (4)	B1 ^{xii} —Rh1—Pr1	69.711 (3)
Rh1 ^{iv} —Pr1—Rh1 ^{ix}	120.763 (4)	B1 ^{xiii} —Rh1—Pr1	69.710 (2)
Rh1—Pr1—Rh1 ^{ix}	82.322 (3)	B1 ^{xiv} —Rh1—Pr1	110.290 (2)
Rh1 ^v —Pr1—Rh1 ^{ix}	97.678 (3)	Rh1 ^{xv} —Rh1—Pr1	115.764 (1)
Rh1 ^{vi} —Pr1—Rh1 ^{ix}	82.322 (3)	Rh1 ^{xvi} —Rh1—Pr1	64.236 (1)
Rh1 ^{vii} —Pr1—Rh1 ^{ix}	97.678 (3)	Rh1 ⁱⁱⁱ —Rh1—Pr1	64.236 (1)
Rh1 ^{viii} —Pr1—Rh1 ^{ix}	180.0	Rh1 ^{xvii} —Rh1—Pr1	115.764 (1)
Pr1 ⁱ —Pr1—Rh1 ⁱⁱ	119.619 (2)	Rh1 ⁱ —Rh1—Pr1	119.619 (1)
Pr1 ⁱⁱ —Pr1—Rh1 ⁱⁱ	60.381 (2)	Rh1 ⁱⁱ —Rh1—Pr1	60.381 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ⁱⁱ	82.322 (3)	B1 ^{xi} —Rh1—Pr1 ^{xviii}	69.711 (2)
Rh1 ^{iv} —Pr1—Rh1 ⁱⁱ	97.678 (3)	B1 ^{xii} —Rh1—Pr1 ^{xviii}	110.289 (3)
Rh1—Pr1—Rh1 ⁱⁱ	59.238 (4)	B1 ^{xiii} —Rh1—Pr1 ^{xviii}	110.290 (2)
Rh1 ^v —Pr1—Rh1 ⁱⁱ	120.762 (4)	B1 ^{xiv} —Rh1—Pr1 ^{xviii}	69.710 (2)
Rh1 ^{vi} —Pr1—Rh1 ⁱⁱ	128.472 (1)	Rh1 ^{xv} —Rh1—Pr1 ^{xviii}	64.236 (1)
Rh1 ^{vii} —Pr1—Rh1 ⁱⁱ	51.528 (1)	Rh1 ^{xvi} —Rh1—Pr1 ^{xviii}	115.764 (1)
Rh1 ^{viii} —Pr1—Rh1 ⁱⁱ	128.472 (1)	Rh1 ⁱⁱⁱ —Rh1—Pr1 ^{xviii}	115.764 (1)
Rh1 ^{ix} —Pr1—Rh1 ⁱⁱ	51.528 (1)	Rh1 ^{xvii} —Rh1—Pr1 ^{xviii}	64.236 (1)
Pr1 ⁱ —Pr1—Rh1 ^x	60.381 (2)	Rh1 ⁱ —Rh1—Pr1 ^{xviii}	60.381 (2)
Pr1 ⁱⁱ —Pr1—Rh1 ^x	119.619 (2)	Rh1 ⁱⁱ —Rh1—Pr1 ^{xviii}	119.619 (2)
Rh1 ⁱⁱⁱ —Pr1—Rh1 ^x	97.678 (3)	Pr1—Rh1—Pr1 ^{xviii}	180.0
Rh1 ^{iv} —Pr1—Rh1 ^x	82.322 (3)	Rh1 ^{xix} —B1—Rh1 ^{xx}	138.257 (2)
Rh1—Pr1—Rh1 ^x	120.762 (4)	Rh1 ^{xix} —B1—Rh1 ^{vi}	89.116 (4)
Rh1 ^v —Pr1—Rh1 ^x	59.238 (4)	Rh1 ^{xx} —B1—Rh1 ^{vi}	76.206 (4)
Rh1 ^{vi} —Pr1—Rh1 ^x	51.528 (1)	Rh1 ^{xix} —B1—Rh1 ^{xxi}	76.206 (4)

Rh1 ^{vii} —Pr1—Rh1 ^x	128.472 (1)	Rh1 ^{xx} —B1—Rh1 ^{xxi}	89.116 (4)
Rh1 ^{viii} —Pr1—Rh1 ^x	51.528 (1)	Rh1 ^{vi} —B1—Rh1 ^{xxi}	138.257 (2)
Rh1 ^{ix} —Pr1—Rh1 ^x	128.472 (1)	Rh1 ^{xix} —B1—Rh1 ⁱⁱⁱ	138.257 (2)
Rh1 ⁱⁱ —Pr1—Rh1 ^x	180.0	Rh1 ^{xx} —B1—Rh1 ⁱⁱⁱ	76.206 (4)
B1 ^{xi} —Rh1—B1 ^{xii}	180.0	Rh1 ^{vi} —B1—Rh1 ⁱⁱⁱ	76.206 (4)
B1 ^{xi} —Rh1—B1 ^{xiii}	89.116 (4)	Rh1 ^{xxi} —B1—Rh1 ⁱⁱⁱ	138.257 (2)
B1 ^{xii} —Rh1—B1 ^{xiii}	90.884 (4)	Rh1 ^{xix} —B1—Rh1 ^{ix}	76.206 (4)
B1 ^{xi} —Rh1—B1 ^{xiv}	90.884 (4)	Rh1 ^{xx} —B1—Rh1 ^{ix}	138.257 (2)
B1 ^{xii} —Rh1—B1 ^{xiv}	89.116 (4)	Rh1 ^{vi} —B1—Rh1 ^{ix}	138.257 (2)
B1 ^{xiii} —Rh1—B1 ^{xiv}	180.0	Rh1 ^{xxi} —B1—Rh1 ^{ix}	76.206 (4)
B1 ^{xi} —Rh1—Rh1 ^{xv}	51.897 (1)	Rh1 ⁱⁱⁱ —B1—Rh1 ^{ix}	89.116 (4)
B1 ^{xii} —Rh1—Rh1 ^{xv}	128.103 (1)		

Symmetry codes: (i) $x, y, z+1$; (ii) $x, y, z-1$; (iii) $-x+y+1, -x+1, z$; (iv) $-x+y, -x, z-1$; (v) $x-1, y, z-1$; (vi) $-y, x-y, z$; (vii) $-y, x-y-1, z-1$; (viii) $-x+y, -x, z$; (ix) $-x+y+1, -x+1, z-1$; (x) $x-1, y, z$; (xi) $-x+1, -y+1, -z+1$; (xii) $x, y-1, z$; (xiii) $-x+1, -y+1, -z$; (xiv) $x, y-1, z+1$; (xv) $-y+1, x-y, z$; (xvi) $-y, x-y-1, z$; (xvii) $-x+y+1, -x, z$; (xviii) $x+1, y, z+1$; (xix) $-y, x-y, z-1$; (xx) $x, y+1, z$; (xxi) $x, y+1, z-1$.

Neodymium trirhodium diboride (II)

Crystal data

NdRh ₃ B ₂	$D_x = 9.839 \text{ Mg m}^{-3}$
$M_r = 474.59$	Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ \AA}$
Hexagonal, $P6/mmm$	Cell parameters from 729 reflections
$a = 5.4527 (2) \text{ \AA}$	$\theta = 4.3\text{--}40.7^\circ$
$c = 3.11066 (13) \text{ \AA}$	$\mu = 30.57 \text{ mm}^{-1}$
$V = 80.10 (1) \text{ \AA}^3$	$T = 293 \text{ K}$
$Z = 1$	Block, metallic
$F(000) = 205$	$0.05 \times 0.05 \times 0.02 \text{ mm}$

Data collection

XtaLAB Synergy, Dualflex, HyPix	$T_{\min} = 0.424, T_{\max} = 0.611$
diffractometer	827 measured reflections
Radiation source: micro-focus sealed X-ray	131 independent reflections
tube, PhotonJet (Mo) X-ray Source	130 reflections with $I > 2\sigma(I)$
Mirror monochromator	$R_{\text{int}} = 0.010$
Detector resolution: 10.0000 pixels mm^{-1}	$\theta_{\max} = 40.2^\circ, \theta_{\min} = 4.3^\circ$
ω scans	$h = -9 \rightarrow 8$
Absorption correction: numerical	$k = -7 \rightarrow 9$
(CrysAlisPro; Rigaku OD, 2021)	$l = -3 \rightarrow 5$

Refinement

Refinement on F^2	0 restraints
Least-squares matrix: full	$w = 1/[\sigma^2(F_o^2) + (0.022P)^2]$
$R[F^2 > 2\sigma(F^2)] = 0.012$	where $P = (F_o^2 + 2F_c^2)/3$
$wR(F^2) = 0.032$	$(\Delta/\sigma)_{\max} < 0.001$
$S = 1.15$	$\Delta\rho_{\max} = 0.97 \text{ e \AA}^{-3}$
131 reflections	$\Delta\rho_{\min} = -2.46 \text{ e \AA}^{-3}$
8 parameters	

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
Nd1	0.000000	0.000000	0.000000	0.00818 (9)
Rh1	0.500000	0.000000	0.500000	0.00674 (8)
B1	0.333333	0.666667	0.000000	0.0093 (6)

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Nd1	0.00896 (10)	0.00896 (10)	0.00662 (12)	0.00448 (5)	0.000	0.000
Rh1	0.00492 (9)	0.00390 (11)	0.01104 (12)	0.00195 (5)	0.000	0.000
B1	0.0100 (9)	0.0100 (9)	0.0079 (12)	0.0050 (4)	0.000	0.000

Geometric parameters (\AA , $^\circ$)

Nd1—Nd1 ⁱ	3.1107 (1)	Nd1—Rh1 ⁱⁱ	3.1388 (1)
Nd1—Nd1 ⁱⁱ	3.1107 (1)	Rh1—B1 ^{xi}	2.2129 (1)
Nd1—Rh1 ⁱⁱⁱ	3.1388 (1)	Rh1—B1 ^{xii}	2.2129 (1)
Nd1—Rh1 ^{iv}	3.1388 (1)	Rh1—B1 ^{xiii}	2.2129 (1)
Nd1—Rh1 ^v	3.1388 (1)	Rh1—B1 ^{xiv}	2.2129 (1)
Nd1—Rh1 ^{vi}	3.1388 (1)	Rh1—Rh1 ^{xv}	2.7264 (1)
Nd1—Rh1	3.1388 (1)	Rh1—Rh1 ^{xvi}	2.7264 (1)
Nd1—Rh1 ^{vii}	3.1388 (1)	Rh1—Rh1 ^{xii}	2.7264 (1)
Nd1—Rh1 ^{viii}	3.1388 (1)	Rh1—Rh1 ^{xvii}	2.7264 (1)
Nd1—Rh1 ^{ix}	3.1388 (1)	Rh1—Rh1 ⁱ	3.1107 (1)
Nd1—Rh1 ^x	3.1388 (1)	Rh1—Rh1 ⁱⁱ	3.1107 (1)
Nd1 ⁱ —Nd1—Nd1 ⁱⁱ	180.0	B1 ^{xiii} —Rh1—Rh1 ^{xv}	51.974 (1)
Nd1 ⁱ —Nd1—Rh1 ⁱⁱⁱ	60.296 (1)	B1 ^{xiv} —Rh1—Rh1 ^{xv}	128.026 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ⁱⁱⁱ	119.704 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvi}	128.026 (1)
Nd1 ⁱ —Nd1—Rh1 ^{iv}	119.704 (1)	B1 ^{xii} —Rh1—Rh1 ^{xvi}	51.974 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ^{iv}	60.296 (1)	B1 ^{xiii} —Rh1—Rh1 ^{xvi}	128.026 (2)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^{iv}	180.0	B1 ^{xiv} —Rh1—Rh1 ^{xvi}	51.974 (1)
Nd1 ⁱ —Nd1—Rh1 ^v	60.296 (1)	Rh1 ^{xv} —Rh1—Rh1 ^{xvi}	180.0
Nd1 ⁱⁱ —Nd1—Rh1 ^v	119.704 (1)	B1 ^{xi} —Rh1—Rh1 ⁱⁱⁱ	51.973 (1)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^v	51.481 (1)	B1 ^{xii} —Rh1—Rh1 ⁱⁱⁱ	128.027 (1)
Rh1 ^{iv} —Nd1—Rh1 ^v	128.519 (1)	B1 ^{xiii} —Rh1—Rh1 ⁱⁱⁱ	51.973 (1)
Nd1 ⁱ —Nd1—Rh1 ^{vi}	119.704 (1)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱⁱ	128.027 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ^{vi}	60.296 (1)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱⁱ	60.0
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^{vi}	128.519 (1)	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱⁱ	120.0
Rh1 ^{iv} —Nd1—Rh1 ^{vi}	51.481 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvii}	128.027 (2)

Rh1 ^v —Nd1—Rh1 ^{vi}	180.0	B1 ^{xii} —Rh1—Rh1 ^{xvii}	51.973 (1)
Nd1 ⁱ —Nd1—Rh1	60.296 (1)	B1 ^{xiii} —Rh1—Rh1 ^{xvii}	128.027 (1)
Nd1 ⁱⁱ —Nd1—Rh1	119.704 (1)	B1 ^{xiv} —Rh1—Rh1 ^{xvii}	51.973 (1)
Rh1 ⁱⁱⁱ —Nd1—Rh1	51.481 (1)	Rh1 ^{xv} —Rh1—Rh1 ^{xvii}	120.0
Rh1 ^{iv} —Nd1—Rh1	128.519 (1)	Rh1 ^{xvi} —Rh1—Rh1 ^{xvii}	60.0
Rh1 ^v —Nd1—Rh1	97.568 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ^{xvii}	180.0
Rh1 ^{vi} —Nd1—Rh1	82.432 (2)	B1 ^{xi} —Rh1—Rh1 ⁱ	45.343 (2)
Nd1 ⁱ —Nd1—Rh1 ^{vii}	119.704 (1)	B1 ^{xii} —Rh1—Rh1 ⁱ	134.657 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ^{vii}	60.296 (1)	B1 ^{xiii} —Rh1—Rh1 ⁱ	134.657 (2)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^{vii}	128.519 (1)	B1 ^{xiv} —Rh1—Rh1 ⁱ	45.343 (2)
Rh1 ^{iv} —Nd1—Rh1 ^{vii}	51.481 (1)	Rh1 ^{xv} —Rh1—Rh1 ⁱ	90.0
Rh1 ^v —Nd1—Rh1 ^{vii}	82.432 (2)	Rh1 ^{xvi} —Rh1—Rh1 ⁱ	90.0
Rh1 ^{vi} —Nd1—Rh1 ^{vii}	97.568 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱ	90.0
Rh1—Nd1—Rh1 ^{vii}	180.0	Rh1 ^{xvii} —Rh1—Rh1 ⁱ	90.0
Nd1 ⁱ —Nd1—Rh1 ^{viii}	60.296 (2)	B1 ^{xi} —Rh1—Rh1 ⁱⁱ	134.657 (2)
Nd1 ⁱⁱ —Nd1—Rh1 ^{viii}	119.704 (2)	B1 ^{xii} —Rh1—Rh1 ⁱⁱ	45.343 (2)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^{viii}	120.592 (3)	B1 ^{xiii} —Rh1—Rh1 ⁱⁱ	45.343 (2)
Rh1 ^{iv} —Nd1—Rh1 ^{viii}	59.408 (3)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱ	134.657 (2)
Rh1 ^v —Nd1—Rh1 ^{viii}	97.568 (2)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vi} —Nd1—Rh1 ^{viii}	82.432 (2)	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱ	90.0
Rh1—Nd1—Rh1 ^{viii}	97.568 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vii} —Nd1—Rh1 ^{viii}	82.432 (2)	Rh1 ^{xvii} —Rh1—Rh1 ⁱⁱ	90.0
Nd1 ⁱ —Nd1—Rh1 ^{ix}	119.704 (2)	Rh1 ⁱ —Rh1—Rh1 ⁱⁱ	180.0
Nd1 ⁱⁱ —Nd1—Rh1 ^{ix}	60.296 (2)	B1 ^{xi} —Rh1—Nd1	110.381 (2)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^{ix}	59.408 (3)	B1 ^{xii} —Rh1—Nd1	69.619 (2)
Rh1 ^{iv} —Nd1—Rh1 ^{ix}	120.592 (3)	B1 ^{xiii} —Rh1—Nd1	69.617 (2)
Rh1 ^v —Nd1—Rh1 ^{ix}	82.432 (2)	B1 ^{xiv} —Rh1—Nd1	110.383 (2)
Rh1 ^{vi} —Nd1—Rh1 ^{ix}	97.568 (2)	Rh1 ^{xv} —Rh1—Nd1	115.7
Rh1—Nd1—Rh1 ^{ix}	82.432 (2)	Rh1 ^{xvi} —Rh1—Nd1	64.3
Rh1 ^{vii} —Nd1—Rh1 ^{ix}	97.568 (2)	Rh1 ⁱⁱⁱ —Rh1—Nd1	64.259 (1)
Rh1 ^{viii} —Nd1—Rh1 ^{ix}	180.0	Rh1 ^{xvii} —Rh1—Nd1	115.741 (1)
Nd1 ⁱ —Nd1—Rh1 ^x	60.296 (1)	Rh1 ⁱ —Rh1—Nd1	119.704 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ^x	119.704 (1)	Rh1 ⁱⁱ —Rh1—Nd1	60.296 (1)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ^x	97.568 (3)	B1 ^{xi} —Rh1—Nd1 ^{xviii}	69.619 (2)
Rh1 ^{iv} —Nd1—Rh1 ^x	82.432 (3)	B1 ^{xii} —Rh1—Nd1 ^{xviii}	110.381 (2)
Rh1 ^v —Nd1—Rh1 ^x	51.481 (1)	B1 ^{xiii} —Rh1—Nd1 ^{xviii}	110.383 (2)
Rh1 ^{vi} —Nd1—Rh1 ^x	128.519 (1)	B1 ^{xiv} —Rh1—Nd1 ^{xviii}	69.617 (2)
Rh1—Nd1—Rh1 ^x	120.592 (3)	Rh1 ^{xv} —Rh1—Nd1 ^{xviii}	64.3
Rh1 ^{vii} —Nd1—Rh1 ^x	59.408 (3)	Rh1 ^{xvi} —Rh1—Nd1 ^{xviii}	115.7
Rh1 ^{viii} —Nd1—Rh1 ^x	51.481 (1)	Rh1 ⁱⁱⁱ —Rh1—Nd1 ^{xviii}	115.741 (1)
Rh1 ^{ix} —Nd1—Rh1 ^x	128.519 (1)	Rh1 ^{xvii} —Rh1—Nd1 ^{xviii}	64.259 (1)
Nd1 ⁱ —Nd1—Rh1 ⁱⁱ	119.704 (1)	Rh1 ⁱ —Rh1—Nd1 ^{xviii}	60.296 (1)
Nd1 ⁱⁱ —Nd1—Rh1 ⁱⁱ	60.296 (1)	Rh1 ⁱⁱ —Rh1—Nd1 ^{xviii}	119.704 (1)
Rh1 ⁱⁱⁱ —Nd1—Rh1 ⁱⁱ	82.432 (3)	Nd1—Rh1—Nd1 ^{xviii}	180.0
Rh1 ^{iv} —Nd1—Rh1 ⁱⁱ	97.568 (3)	Rh1 ^{xix} —B1—Rh1 ^{xx}	138.332 (1)
Rh1 ^v —Nd1—Rh1 ⁱⁱ	128.519 (1)	Rh1 ^{xix} —B1—Rh1 ^v	89.314 (4)
Rh1 ^{vi} —Nd1—Rh1 ⁱⁱ	51.481 (1)	Rh1 ^{xx} —B1—Rh1 ^v	76.053 (3)
Rh1—Nd1—Rh1 ⁱⁱ	59.408 (3)	Rh1 ^{xix} —B1—Rh1 ^{xxi}	76.053 (3)

Rh1 ^{vii} —Nd1—Rh1 ⁱⁱ	120.592 (3)	Rh1 ^{xx} —B1—Rh1 ^{xxi}	89.314 (4)
Rh1 ^{viii} —Nd1—Rh1 ⁱⁱ	128.519 (1)	Rh1 ^v —B1—Rh1 ^{xxi}	138.332 (1)
Rh1 ^{ix} —Nd1—Rh1 ⁱⁱ	51.481 (1)	Rh1 ^{xix} —B1—Rh1 ⁱⁱⁱ	138.332 (1)
Rh1 ^x —Nd1—Rh1 ⁱⁱ	180.0	Rh1 ^{xx} —B1—Rh1 ⁱⁱⁱ	76.053 (2)
B1 ^{xi} —Rh1—B1 ^{xii}	180.0	Rh1 ^v —B1—Rh1 ⁱⁱⁱ	76.053 (3)
B1 ^{xi} —Rh1—B1 ^{xiii}	89.314 (4)	Rh1 ^{xxi} —B1—Rh1 ⁱⁱⁱ	138.332 (1)
B1 ^{xii} —Rh1—B1 ^{xiii}	90.686 (4)	Rh1 ^{xix} —B1—Rh1 ^{ix}	76.053 (3)
B1 ^{xi} —Rh1—B1 ^{xiv}	90.686 (4)	Rh1 ^{xx} —B1—Rh1 ^{ix}	138.332 (1)
B1 ^{xii} —Rh1—B1 ^{xiv}	89.314 (4)	Rh1 ^v —B1—Rh1 ^{ix}	138.332 (2)
B1 ^{xiii} —Rh1—B1 ^{xiv}	180.0	Rh1 ^{xxi} —B1—Rh1 ^{ix}	76.053 (3)
B1 ^{xi} —Rh1—Rh1 ^{xv}	51.974 (1)	Rh1 ⁱⁱⁱ —B1—Rh1 ^{ix}	89.314 (4)
B1 ^{xii} —Rh1—Rh1 ^{xv}	128.026 (1)		

Symmetry codes: (i) $x, y, z+1$; (ii) $x, y, z-1$; (iii) $-x+y+1, -x+1, z$; (iv) $-x+y, -x, z-1$; (v) $-y, x-y, z$; (vi) $-y, x-y-1, z-1$; (vii) $x-1, y, z-1$; (viii) $-x+y, -x, z$; (ix) $-x+y+1, -x+1, z-1$; (x) $x-1, y, z$; (xi) $-x+1, -y+1, -z+1$; (xii) $x, y-1, z$; (xiii) $-x+1, -y+1, -z$; (xiv) $x, y-1, z+1$; (xv) $-y+1, x-y, z$; (xvi) $-y, x-y-1, z$; (xvii) $-x+y+1, -x, z$; (xviii) $x+1, y, z+1$; (xix) $-y, x-y, z-1$; (xx) $x, y+1, z$; (xxi) $x, y+1, z-1$.

Samarium trirhodium diboride (III)

Crystal data

SmRh₃B₂
 $M_r = 480.70$
 Hexagonal, $P6/mmm$
 $a = 5.4438 (2)$ Å
 $c = 3.11901 (12)$ Å
 $V = 80.05 (1)$ Å³
 $Z = 1$
 $F(000) = 207$

$D_x = 9.972$ Mg m⁻³
 Mo $K\alpha$ radiation, $\lambda = 0.71073$ Å
 Cell parameters from 649 reflections
 $\theta = 4.3\text{--}40.1^\circ$
 $\mu = 32.61$ mm⁻¹
 $T = 293$ K
 Block, metallic
 $0.06 \times 0.05 \times 0.02$ mm

Data collection

XtaLAB Synergy, Dualflex, HyPix
 diffractometer
 Radiation source: micro-focus sealed X-ray
 tube, PhotonJet (Mo) X-ray Source
 Mirror monochromator
 Detector resolution: 10.0000 pixels mm⁻¹
 ω scans
 Absorption correction: numerical
 (CrysAlisPro; Rigaku OD, 2021)

$T_{\min} = 0.324, T_{\max} = 0.542$
 696 measured reflections
 129 independent reflections
 128 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.011$
 $\theta_{\max} = 40.1^\circ, \theta_{\min} = 4.3^\circ$
 $h = -8 \rightarrow 9$
 $k = -7 \rightarrow 7$
 $l = -3 \rightarrow 5$

Refinement

Refinement on F^2
 Least-squares matrix: full
 $R[F^2 > 2\sigma(F^2)] = 0.012$
 $wR(F^2) = 0.032$
 $S = 1.13$
 129 reflections
 9 parameters
 0 restraints

$w = 1/[\sigma^2(F_o^2) + (0.0213P)^2 + 0.0484P]$
 where $P = (F_o^2 + 2F_c^2)/3$
 $(\Delta/\sigma)_{\max} < 0.001$
 $\Delta\rho_{\max} = 1.76$ e Å⁻³
 $\Delta\rho_{\min} = -0.97$ e Å⁻³
 Extinction correction: SHELXL-2016/6
 (Sheldrick 2016),
 $F_c^* = kFc[1 + 0.001xFc^2\lambda^3/\sin(2\theta)]^{-1/4}$
 Extinction coefficient: 0.034 (3)

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
Sm1	0.000000	0.000000	0.000000	0.00780 (10)
Rh1	0.500000	0.000000	0.500000	0.00739 (10)
B1	0.333333	0.666667	0.000000	0.0091 (7)

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Sm1	0.00841 (12)	0.00841 (12)	0.00658 (14)	0.00420 (6)	0.000	0.000
Rh1	0.00502 (11)	0.00389 (13)	0.01287 (14)	0.00194 (6)	0.000	0.000
B1	0.0085 (10)	0.0085 (10)	0.0102 (15)	0.0043 (5)	0.000	0.000

Geometric parameters (\AA , $^\circ$)

Sm1—Sm1 ⁱ	3.1190 (1)	Sm1—Rh1 ^x	3.1370 (1)
Sm1—Sm1 ⁱⁱ	3.1190 (1)	Rh1—B1 ^{xi}	2.2140 (1)
Sm1—Rh1 ⁱⁱⁱ	3.1370 (1)	Rh1—B1 ^{xii}	2.2140 (1)
Sm1—Rh1 ^{iv}	3.1370 (1)	Rh1—B1 ^{xiii}	2.2140 (1)
Sm1—Rh1	3.1370 (1)	Rh1—B1 ^{xiv}	2.2140 (1)
Sm1—Rh1 ^v	3.1370 (1)	Rh1—Rh1 ^{xv}	2.7219 (1)
Sm1—Rh1 ^{vi}	3.1370 (1)	Rh1—Rh1 ^{xvi}	2.7219 (1)
Sm1—Rh1 ^{vii}	3.1370 (1)	Rh1—Rh1 ^{xii}	2.7219 (1)
Sm1—Rh1 ^{viii}	3.1370 (1)	Rh1—Rh1 ^{xvii}	2.7219 (1)
Sm1—Rh1 ^{ix}	3.1370 (1)	Rh1—Rh1 ⁱ	3.1190 (1)
Sm1—Rh1 ⁱⁱ	3.1370 (1)	Rh1—Rh1 ⁱⁱ	3.1190 (1)
Sm1 ⁱ —Sm1—Sm1 ⁱⁱ	180.0	B1 ^{xiii} —Rh1—Rh1 ^{xv}	52.069 (1)
Sm1 ⁱ —Sm1—Rh1 ⁱⁱⁱ	60.189 (1)	B1 ^{xiv} —Rh1—Rh1 ^{xv}	127.931 (1)
Sm1 ⁱⁱ —Sm1—Rh1 ⁱⁱⁱ	119.811 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvi}	127.931 (1)
Sm1 ⁱ —Sm1—Rh1 ^{iv}	119.811 (1)	B1 ^{xii} —Rh1—Rh1 ^{xvi}	52.069 (1)
Sm1 ⁱⁱ —Sm1—Rh1 ^{iv}	60.189 (1)	B1 ^{xiii} —Rh1—Rh1 ^{xvi}	127.931 (1)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^{iv}	180.0	B1 ^{xiv} —Rh1—Rh1 ^{xvi}	52.069 (1)
Sm1 ⁱ —Sm1—Rh1	60.189 (2)	Rh1 ^{xv} —Rh1—Rh1 ^{xvi}	180.0
Sm1 ⁱⁱ —Sm1—Rh1	119.811 (1)	B1 ^{xi} —Rh1—Rh1 ⁱⁱⁱ	52.069 (1)
Rh1 ⁱⁱⁱ —Sm1—Rh1	51.423 (1)	B1 ^{xii} —Rh1—Rh1 ⁱⁱⁱ	127.931 (1)
Rh1 ^{iv} —Sm1—Rh1	128.6	B1 ^{xiii} —Rh1—Rh1 ⁱⁱⁱ	52.069 (1)
Sm1 ⁱ —Sm1—Rh1 ^v	119.811 (1)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱⁱ	127.931 (1)
Sm1 ⁱⁱ —Sm1—Rh1 ^v	60.189 (2)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱⁱ	60.0
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^v	128.6	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱⁱ	120.0
Rh1 ^{iv} —Sm1—Rh1 ^v	51.423 (1)	B1 ^{xi} —Rh1—Rh1 ^{xvii}	127.931 (1)

Rh1—Sm1—Rh1 ^v	180.0	B1 ^{xii} —Rh1—Rh1 ^{xvii}	52.069 (1)
Sm1 ⁱ —Sm1—Rh1 ^{vi}	60.189 (2)	B1 ^{xiii} —Rh1—Rh1 ^{xvii}	127.931 (1)
Sm1 ⁱⁱ —Sm1—Rh1 ^{vi}	119.811 (1)	B1 ^{xiv} —Rh1—Rh1 ^{xvii}	52.069 (1)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^{vi}	51.423 (1)	Rh1 ^{xv} —Rh1—Rh1 ^{xvii}	120.0
Rh1 ^{iv} —Sm1—Rh1 ^{vi}	128.577 (1)	Rh1 ^{xvi} —Rh1—Rh1 ^{xvii}	60.0
Rh1—Sm1—Rh1 ^{vi}	97.428 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ^{xvii}	180.0
Rh1 ^v —Sm1—Rh1 ^{vi}	82.572 (2)	B1 ^{xi} —Rh1—Rh1 ⁱ	45.219 (1)
Sm1 ⁱ —Sm1—Rh1 ^{vii}	119.811 (1)	B1 ^{xii} —Rh1—Rh1 ⁱ	134.781 (2)
Sm1 ⁱⁱ —Sm1—Rh1 ^{vii}	60.189 (2)	B1 ^{xiii} —Rh1—Rh1 ⁱ	134.781 (1)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^{vii}	128.577 (1)	B1 ^{xiv} —Rh1—Rh1 ⁱ	45.219 (1)
Rh1 ^{iv} —Sm1—Rh1 ^{vii}	51.423 (1)	Rh1 ^{xv} —Rh1—Rh1 ⁱ	90.0
Rh1—Sm1—Rh1 ^{vii}	82.572 (2)	Rh1 ^{xvi} —Rh1—Rh1 ⁱ	90.0
Rh1 ^v —Sm1—Rh1 ^{vii}	97.428 (2)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱ	90.0
Rh1 ^{vi} —Sm1—Rh1 ^{vii}	180.0	Rh1 ^{xvii} —Rh1—Rh1 ⁱ	90.0
Sm1 ⁱ —Sm1—Rh1 ^{viii}	60.189 (1)	B1 ^{xi} —Rh1—Rh1 ⁱⁱ	134.781 (2)
Sm1 ⁱⁱ —Sm1—Rh1 ^{viii}	119.811 (1)	B1 ^{xii} —Rh1—Rh1 ⁱⁱ	45.219 (2)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^{viii}	120.379 (3)	B1 ^{xiii} —Rh1—Rh1 ⁱⁱ	45.219 (1)
Rh1 ^{iv} —Sm1—Rh1 ^{viii}	59.621 (3)	B1 ^{xiv} —Rh1—Rh1 ⁱⁱ	134.781 (1)
Rh1—Sm1—Rh1 ^{viii}	97.428 (2)	Rh1 ^{xv} —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^v —Sm1—Rh1 ^{viii}	82.572 (2)	Rh1 ^{xvi} —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vi} —Sm1—Rh1 ^{viii}	97.428 (1)	Rh1 ⁱⁱⁱ —Rh1—Rh1 ⁱⁱ	90.0
Rh1 ^{vii} —Sm1—Rh1 ^{viii}	82.572 (1)	Rh1 ^{xvii} —Rh1—Rh1 ⁱⁱ	90.0
Sm1 ⁱ —Sm1—Rh1 ^{ix}	119.811 (1)	Rh1 ⁱ —Rh1—Rh1 ⁱⁱ	180.0
Sm1 ⁱⁱ —Sm1—Rh1 ^{ix}	60.189 (1)	B1 ^{xi} —Rh1—Sm1	110.498 (2)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^{ix}	59.621 (3)	B1 ^{xii} —Rh1—Sm1	69.502 (1)
Rh1 ^{iv} —Sm1—Rh1 ^{ix}	120.379 (3)	B1 ^{xiii} —Rh1—Sm1	69.501 (1)
Rh1—Sm1—Rh1 ^{ix}	82.572 (2)	B1 ^{xiv} —Rh1—Sm1	110.499 (1)
Rh1 ^v —Sm1—Rh1 ^{ix}	97.428 (2)	Rh1 ^{xv} —Rh1—Sm1	115.711 (1)
Rh1 ^{vi} —Sm1—Rh1 ^{ix}	82.572 (1)	Rh1 ^{xvi} —Rh1—Sm1	64.3
Rh1 ^{vii} —Sm1—Rh1 ^{ix}	97.428 (1)	Rh1 ⁱⁱⁱ —Rh1—Sm1	64.289 (1)
Rh1 ^{viii} —Sm1—Rh1 ^{ix}	180.0	Rh1 ^{xvii} —Rh1—Sm1	115.7
Sm1 ⁱ —Sm1—Rh1 ⁱⁱ	119.811 (1)	Rh1 ⁱ —Rh1—Sm1	119.811 (2)
Sm1 ⁱⁱ —Sm1—Rh1 ⁱⁱ	60.189 (1)	Rh1 ⁱⁱ —Rh1—Sm1	60.189 (2)
Rh1 ⁱⁱⁱ —Sm1—Rh1 ⁱⁱ	82.572 (2)	B1 ^{xi} —Rh1—Sm1 ^{xvii}	69.502 (2)
Rh1 ^{iv} —Sm1—Rh1 ⁱⁱ	97.428 (2)	B1 ^{xii} —Rh1—Sm1 ^{xvii}	110.498 (1)
Rh1—Sm1—Rh1 ⁱⁱ	59.621 (3)	B1 ^{xiii} —Rh1—Sm1 ^{xvii}	110.499 (1)
Rh1 ^v —Sm1—Rh1 ⁱⁱ	120.379 (4)	B1 ^{xiv} —Rh1—Sm1 ^{xvii}	69.501 (1)
Rh1 ^{vi} —Sm1—Rh1 ⁱⁱ	128.577 (1)	Rh1 ^{xv} —Rh1—Sm1 ^{xvii}	64.3
Rh1 ^{vii} —Sm1—Rh1 ⁱⁱ	51.423 (1)	Rh1 ^{xvi} —Rh1—Sm1 ^{xvii}	115.7
Rh1 ^{viii} —Sm1—Rh1 ⁱⁱ	51.423 (1)	Rh1 ⁱⁱⁱ —Rh1—Sm1 ^{xvii}	115.7
Rh1 ^{vii} —Sm1—Rh1 ⁱⁱ	128.577 (1)	Rh1 ^{xvii} —Rh1—Sm1 ^{xvii}	64.3
Rh1 ^{ix} —Sm1—Rh1 ⁱⁱ	51.423 (1)	Rh1 ⁱ —Rh1—Sm1 ^{xvii}	60.189 (1)
Sm1 ⁱ —Sm1—Rh1 ^x	60.189 (1)	Rh1 ⁱⁱ —Rh1—Sm1 ^{xvii}	119.811 (1)
Sm1 ⁱⁱ —Sm1—Rh1 ^x	119.811 (1)	Sm1—Rh1—Sm1 ^{xvii}	180.0
Rh1 ⁱⁱⁱ —Sm1—Rh1 ^x	97.428 (2)	Rh1 ^{xix} —B1—Rh1 ^{xx}	138.425 (1)
Rh1 ^{iv} —Sm1—Rh1 ^x	82.572 (2)	Rh1 ^{xix} —B1—Rh1 ^{xxi}	75.862 (3)
Rh1—Sm1—Rh1 ^x	120.379 (4)	Rh1 ^{xx} —B1—Rh1 ^{xxi}	89.562 (4)
Rh1 ^v —Sm1—Rh1 ^x	59.621 (3)	Rh1 ^{xix} —B1—Rh1 ^{vi}	89.562 (4)
Rh1 ^{vi} —Sm1—Rh1 ^x	51.423 (1)		

Rh1 ^{vii} —Sm1—Rh1 ^x	128.577 (1)	Rh1 ^{xx} —B1—Rh1 ^{vi}	75.862 (3)
Rh1 ^{viii} —Sm1—Rh1 ^x	51.423 (1)	Rh1 ^{xxi} —B1—Rh1 ^{vi}	138.425 (1)
Rh1 ^{ix} —Sm1—Rh1 ^x	128.577 (1)	Rh1 ^{xix} —B1—Rh1 ⁱⁱⁱ	138.425 (1)
Rh1 ⁱⁱ —Sm1—Rh1 ^x	180.0	Rh1 ^{xx} —B1—Rh1 ⁱⁱⁱ	75.862 (3)
B1 ^{xi} —Rh1—B1 ^{xii}	180.0	Rh1 ^{xxi} —B1—Rh1 ⁱⁱⁱ	138.425 (1)
B1 ^{xi} —Rh1—B1 ^{xiii}	89.561 (4)	Rh1 ^{vi} —B1—Rh1 ⁱⁱⁱ	75.862 (3)
B1 ^{xii} —Rh1—B1 ^{xiii}	90.439 (4)	Rh1 ^{xix} —B1—Rh1 ^{ix}	75.862 (2)
B1 ^{xi} —Rh1—B1 ^{xiv}	90.439 (4)	Rh1 ^{xx} —B1—Rh1 ^{ix}	138.425 (1)
B1 ^{xii} —Rh1—B1 ^{xiv}	89.561 (4)	Rh1 ^{xxi} —B1—Rh1 ^{ix}	75.862 (3)
B1 ^{xiii} —Rh1—B1 ^{xiv}	180.0	Rh1 ^{vi} —B1—Rh1 ^{ix}	138.425 (1)
B1 ^{xi} —Rh1—Rh1 ^{xv}	52.069 (1)	Rh1 ⁱⁱⁱ —B1—Rh1 ^{ix}	89.562 (4)
B1 ^{xii} —Rh1—Rh1 ^{xv}	127.931 (1)		

Symmetry codes: (i) $x, y, z+1$; (ii) $x, y, z-1$; (iii) $-x+y+1, -x+1, z$; (iv) $-x+y, -x, z-1$; (v) $x-1, y, z-1$; (vi) $-y, x-y, z$; (vii) $-y, x-y-1, z-1$; (viii) $-x+y, -x, z$; (ix) $-x+y+1, -x+1, z-1$; (x) $x-1, y, z$; (xi) $-x+1, -y+1, -z+1$; (xii) $x, y-1, z$; (xiii) $-x+1, -y+1, -z$; (xiv) $x, y-1, z+1$; (xv) $-y+1, x-y, z$; (xvi) $-y, x-y-1, z$; (xvii) $-x+y+1, -x, z$; (xviii) $x+1, y, z+1$; (xix) $-y, x-y, z-1$; (xx) $x, y+1, z$; (xxi) $x, y+1, z-1$.