

Received 30 May 2022

Accepted 15 June 2022

Edited by S. Parkin, University of Kentucky, USA

Keywords: crystal structure; zirconium; hafnium; arsenate; ionic conduction.**CCDC references:** 2179420; 2179419**Supporting information:** this article has supporting information at journals.iucr.org/e

Flux syntheses and single-crystal structures of $\text{CsNa}_{10}M_4(\text{AsO}_4)_9$ ($M = \text{Zr}, \text{Hf}$)

William T. A. Harrison*

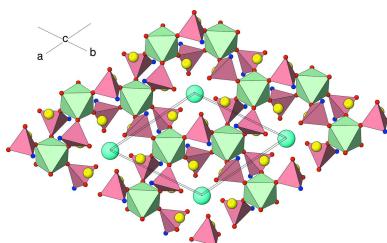
Department of Chemistry, University of Aberdeen, Meston Walk, Aberdeen AB24 3UE, Scotland. *Correspondence e-mail: w.harrison@abdn.ac.uk

The isostructural compounds caesium decasodium tetrazirconium nonaarsenate, $\text{CsNa}_{10}\text{Zr}_4(\text{AsO}_4)_9$, and caesium decasodium tetrahafnium nonaarsenate, $\text{CsNa}_{10}\text{Hf}_4(\text{AsO}_4)_9$, arose as unexpected single-crystal products from the reactions of Na_2CO_3 , MO_2 ($M = \text{Zr}, \text{Hf}$) and As_2O_5 in a eutectic flux of NaCl and CsCl . They consist of MO_6 octahedra and AsO_4 tetrahedra sharing vertices to generate three-dimensional polyhedral networks encapsulating the caesium and sodium ions. The MO_6 groups share all their vertices with adjacent As atoms but the As atoms have one or two ‘terminal’ O atoms not bonded to Zr or Hf. The Cs^+ ion adopts a squashed octahedral geometry and the coordination polyhedra of the partially occupied sodium ions are variously trigonal bipyramidal, tetrahedral, square pyramidal and trigonal pyramidal. Site symmetries: $\text{Cs } \bar{3}$; $M 3$; As 1 and 2; O 1; Na 1, 2 and 3. The $M = \text{Zr}$ crystal was refined as an obverse/reverse rhombohedral twin.

1. Chemical context

Potassium titanyl phosphate (KTiOPO_4 ; KTP) has long been recognized as an important non-linear optical (NLO) material (Zumsteg *et al.*, 1976) due to its unique combination of desirable physical properties including ‘a large hyperpolarizability, excellent temperature window, wide wavelength for phase matching and outstanding crystal stability’ (Stucky *et al.*, 1989). Work continues to improve the performance of KTP waveguides in optoelectronics (Kores *et al.*, 2021) and it is finding new uses as a frequency doubler (to 532 nm green light) for 1064 nm Nd-YAG laser radiation in many areas of medicine (Shim & Kim, 2021; McGarey *et al.*, 2021). So far as crystal chemistry is concerned, the KTiOPO_4 structure type (space group $Pna2_1$, $a \approx 12.8$, $b \approx 6.4$, $c \approx 10.6$ Å, $Z = 8$, $Z' = 2$) is remarkably accommodating with respect to partial or complete isovalent or aleovalent substitution at the potassium ($\text{Na}^+, \text{Rb}^+, \text{Cs}^+, \text{Tl}^+, \text{NH}_4^+ \dots$), titanium ($\text{Zr}^{IV}, \text{Hf}^{IV}, \text{V}^{IV}, \text{Sn}^{IV}, \text{Sb}^V, \text{Ga}^{3+}, \text{Fe}^{3+}, \text{Al}^{3+}, \text{Cr}^{3+} \dots$), phosphorus ($\text{As}^V, \text{Si}^{IV}, \text{Ge}^{IV}$) and even oxygen (OH^-, F^-) sites and comprehensive reviews on its substitution chemistry have appeared (Sorokina & Voronkova, 2007).

In an attempt to grow single crystals of the possible new KTP analogues NaZrOAsO_4 and NaHfOAsO_4 by reacting Na_2CO_3 , MO_2 ($M = \text{Zr}, \text{Hf}$) and As_2O_5 in a low-melting flux of NaCl and CsCl , the isostructural title compounds $\text{CsNa}_{10}\text{Zr}_4(\text{AsO}_4)_9$ (I) and $\text{CsNa}_{10}\text{Hf}_4(\text{AsO}_4)_9$ (II)



OPEN ACCESS

Published under a CC BY 4.0 licence

were the unexpected result and their crystal structures are now described.

2. Structural commentary

Compounds (I) and (II) are isostructural and crystallize in the rhombohedral space group $\bar{R}\bar{3}c$ (No. 167) with an unusually long c unit-cell parameter of nearly 77 Å. This is of course partly a consequence of our choosing the hexagonal (R -centred) setting of the unit cell [the equivalent primitive rhombohedral lattice for (I) has $a = b = c \approx 26.21$ Å and $\alpha = \beta = \gamma \approx 20.3^\circ$] but even so, it is notable that the l index runs well into three figures for (I) in the R -centred setting. This description will focus on the structure of (I) and note significant differences for (II) where applicable.

The asymmetric unit of (I), expanded to show the full coordination polyhedra of the zirconium and arsenic atoms, is shown in Fig. 1. It consists of two zirconium atoms (both with site symmetry 3 on Wyckoff site 12c), two arsenic atoms [As1 on a general position (36f) and As2 with site symmetry 2 (18e)] and six oxygen atoms, one of which is disordered over two adjacent sites (all lying on general positions, 36f), which leads to the unusual 4:9 stoichiometry for the Zr^{IV} and AsO_4^{3-} moieties with a net charge of -11 . The structure of (I) is completed by a Cs^+ ion (site symmetry $\bar{3}$, 6b) and four partly occupied sodium cations [one on a general position (36f), one with site symmetry 2 (18e) and two with site symmetry 3 (12c)]. To maintain charge balance, the four sodium ions must have a total occupancy of 10 based on $Z = 6$ (full occupancy of the four sites would give 13 sodium ions per caesium ion).

Both zirconium atoms adopt almost regular ZrO_6 octahedral geometries (Müller-Buschbaum, 2010) when crystal symmetry is taken into account: the mean $Zr1-O$ separation (to $3 \times O3$ and $3 \times O5$) is 2.070 Å and the quadratic elongation and angular variance are 1.001 and $4.43^{\circ 2}$, respectively

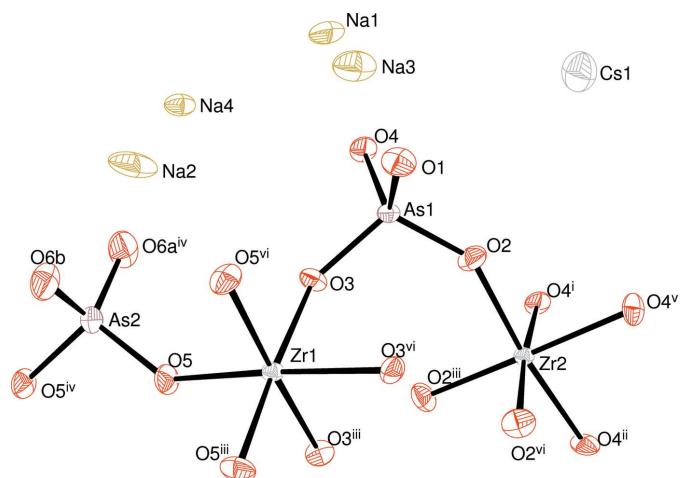


Figure 1

The asymmetric unit of (I) expanded to include the full Zr and As coordination polyhedra showing 50% displacement ellipsoids. Only one disorder component about As2 is shown. Symmetry codes: (i) $1 - x, 1 - y, -z$; (ii) $y, 1 - x - y, -z$; (iii) $1 - y, 1 + x - y, z$; (iv) $\frac{4}{3} - x, \frac{2}{3} - x + y, \frac{1}{6} - z$; (v) $x - y, x, -z$; (vi) $y - x, 1 - x, z$.

(Robinson *et al.*, 1971). Equivalent data for Zr2 (bonded to $3 \times O2$ and $3 \times O4$) are 2.072 Å, 1.003 and $9.86^{\circ 2}$, respectively. The ‘extrapolated’ (Brese & O’Keeffe, 1991) bond-valence sums (BVS) in valence units are 4.10 and 4.07 for Zr1 and Zr2, respectively, in acceptable agreement with the expected value of 4.00. The mean Hf–O distances in (II) are 2.062 Å for Hf1 (BVS = 4.13, quadratic elongation = 1.002, angular variance = $5.38^{\circ 2}$) and 2.065 Å for Hf2 (4.10, 1.004, $13.20^{\circ 2}$). It may be seen that the Hf–O bonds are slightly shorter than the Zr–O bonds, which is in accordance with ionic radii data (Shannon, 1976): $r_6(Zr^{IV}) = 0.72$ (6 = six-coordinate) and $r_6(Hf^{IV}) = 0.71$ Å and is presumed to arise from the lanthanide contraction effect.

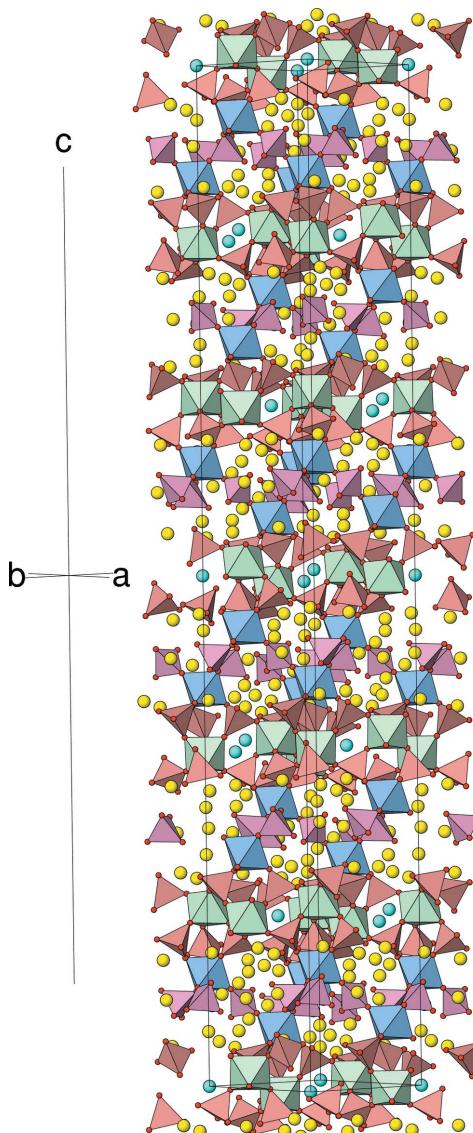
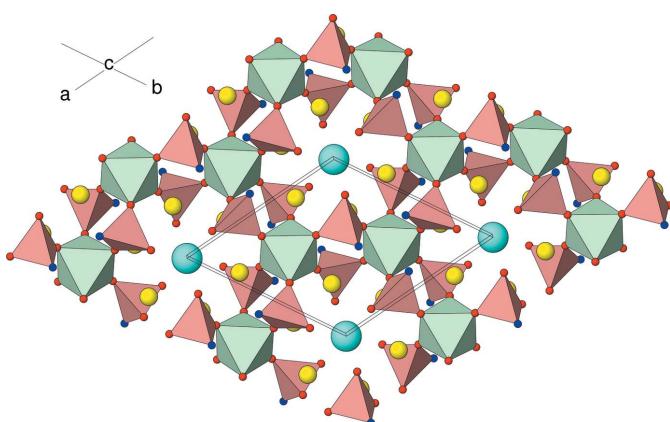


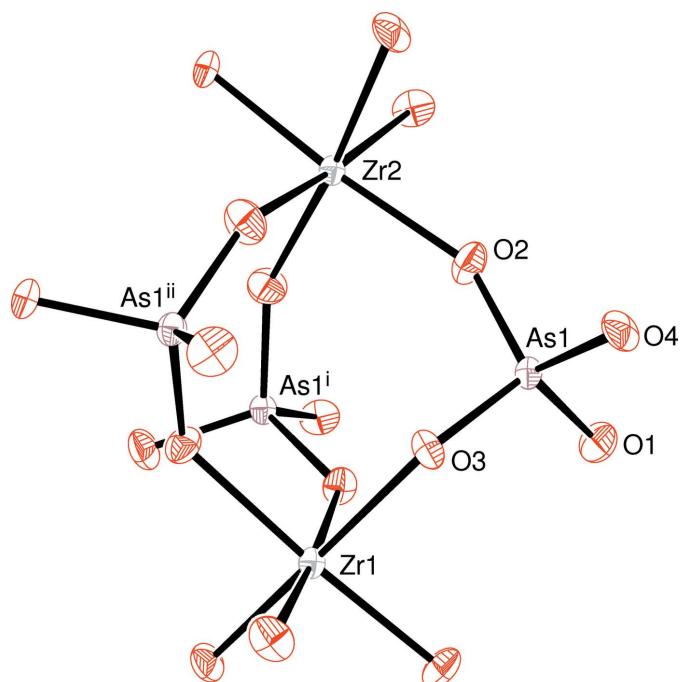
Figure 2

The unit-cell of (I) in polyhedral representation viewed approximately down [110]. A single O atom at the average location of O6A and O6B in the asymmetric unit has been used to construct the As2 tetrahedron. Colour code: $Zr1O_6$ octahedra blue, $Zr2O_6$ octahedra green, $As1O_4$ tetrahedra peach, $As2O_4$ tetrahedra rose, Cs sky blue, Na yellow, O (polyhedral corners) red.

**Figure 3**

View down [001] of an 'A'-type layer in the structure of (I) in polyhedral representation. Atom and polyhedron colours as in Fig. 2 except O3 is blue.

The As1 atom in (I) is surrounded by four oxygen atoms (O1–O4) in the geometry of a slightly distorted tetrahedron [mean As–O = 1.677 Å, spread of O–As–O angles = 103.0 (2)–114.9 (2)°, τ_4 (Yang *et al.*, 2007) = 0.95]. Atom As2 is also tetrahedral (to 2 × O5 and 2 × O6), with the latter O atom disordered over two adjacent sites in almost equal occupancies of 0.45 (3):0.55 (3) [O6A···O6B = 0.909 (13) Å]. Of the six oxygen atoms in the structure of (I), four of them (O2–O5) bridge zirconium and arsenic atoms with a mean Zr–O–As bond angle of 141.5° [equivalent mean Hf–O–As bond angle in (II) = 140.4°] and two (O1 and O6) are 'terminal' and only bonded to arsenic: all of the O atoms also

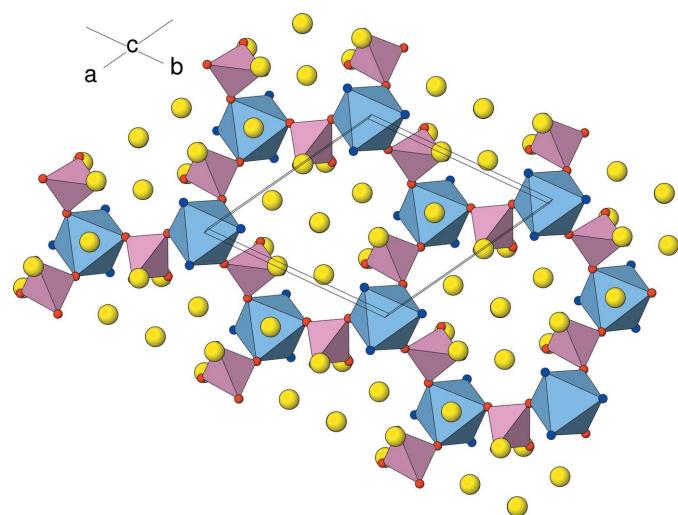
**Figure 4**

Detail of the extended structure of (I) showing a $Zr_2As_3O_{18}$ 'lantern' motif of Zr1 and Zr2 octahedra linked by three As1 tetrahedra *via* atoms O2 and O3. In (I), this motif has crystallographically imposed threefold symmetry about a rotation axis passing through the zirconium atoms. Symmetry codes: (i) $1 - y, 1 + x - y, z$; (ii) $y - x, 1 - x, z$.

form one or more bonds to nearby caesium and/or sodium ions.

The caesium ion in (I) adopts a grossly squashed octahedral coordination to six O1 atoms with $Cs1-O1 = 3.235$ (4) Å: the *cis* O–Cs–O bond angles are compressed to 62.30 (10) or expanded to 117.70 (10)°: the Cs1 BVS of 0.61 compared to an expected value of 1.00 suggests significant underbonding. The interpretation of the sodium-ion coordination polyhedra are complicated by the positional disorder of atom O6 but can be described as distorted trigonal bipyramidal (Na1), very distorted tetrahedral (Na2), square-based pyramidal (Na3) and squashed trigonal pyramidal (Na4). It is notable that Na4 is only three coordinate but similar NaO_3 geometries have been observed in dehydrated sodium aluminosilicate zeolites (Adams *et al.*, 1982).

The extended structure of (I) (Fig. 2) can be conceptually broken down into two different types of layers lying parallel to (001). The first layer (type 'A') occurs at $z \simeq 0, 1/6, 1/3, 1/2, 2/3$ and 5/6 with adjacent A-layers laterally displaced by 1/3 in x and 2/3 in y and consists of the Zr2 and As1 centred polyhedra as well as the caesium ions. Fig. 3 shows that each Zr_2O_6 octahedron is connected by two As_1O_4 tetrahedra (*via* O2 and O4) to result in a 'honeycomb' array of polyhedral 12-rings (six octahedra and 12 tetrahedra) encapsulating the Cs^+ ions. Atom O3 of the arsenate group provides the link to the type 'B' layers on either side of the A layer. This inter-octahedral connectivity *via* O3 leads to a distinctive 'lantern' motif (Fig. 4) in which three tetrahedra link two octahedra [$Zr_1 \cdots Zr_2 = 4.886$ (2); $Hf_1 \cdots Hf_2$ in (II) = 4.863 (2) Å]: similar 'lanterns' are a feature of the polyhedral connectivity in the scandium tungstate $[M_2(XO_4)_3]$ (Abrahams & Bernstein, 1966), Nasicon $[AM_2(XO_4)_3]$ (Anantharamulu *et al.*, 2011) and langbeinite $[A_2M_2(XO_4)_3]$ (Norberg, 2002) structure types but they differ from (I) because all the vertices of the constituent tetrahedra in these structures link to adjacent octahedra, hence their 2:3 $M:X$ ratios compared to the 4:9 ratio for (I).

**Figure 5**

View down [001] of a 'B'-type layer in the structure of (I) in polyhedral representation. Atom and polyhedron colours as in Fig. 2 except O3 is blue.

Table 1
Experimental details.

| | (I) | (II) |
|--|---|---|
| Crystal data | | |
| Chemical formula | CsNa ₁₀ Zr ₄ (AsO ₄) ₉ | CsNa ₁₀ Hf ₄ (AsO ₄) ₉ |
| <i>M</i> _r | 1977.97 | 2327.05 |
| Crystal system, space group | Trigonal, <i>R</i> ̄3 <i>c</i> : <i>H</i> | Trigonal, <i>R</i> ̄3 <i>c</i> : <i>H</i> |
| Temperature (K) | 293 | 120 |
| <i>a</i> , <i>c</i> (Å) | 9.2218 (5), 76.982 (5) | 9.1795 (2), 76.527 (8) |
| <i>V</i> (Å ³) | 5669.6 (7) | 5584.5 (6) |
| <i>Z</i> | 6 | 6 |
| Radiation type | Mo <i>K</i> α | Mo <i>K</i> α |
| <i>μ</i> (mm ⁻¹) | 10.07 | 20.25 |
| Crystal size (mm) | 0.10 × 0.10 × 0.10 | 0.08 × 0.08 × 0.08 |
| Data collection | | |
| Diffractometer | Bruker SMART CCD | Nonius KappaCCD |
| Absorption correction | Multi-scan (<i>SADABS</i> ; Bruker, 1999) | Multi-scan (<i>SORTAV</i> ; Blessing, 1995) |
| <i>T</i> _{min} , <i>T</i> _{max} | 0.350, 0.495 | 0.40, 0.50 |
| No. of measured, independent and observed [<i>I</i> > 2σ(<i>I</i>)] reflections | 2288, 2288, 1694 | 11660, 1434, 1164 |
| <i>R</i> _{int} | — | 0.070 |
| (sin θ/λ) _{max} (Å ⁻¹) | 0.756 | 0.650 |
| Refinement | | |
| <i>R</i> [<i>F</i> ² > 2σ(<i>F</i> ²)], <i>wR</i> (<i>F</i> ²), <i>S</i> | 0.040, 0.093, 1.00 | 0.032, 0.078, 1.06 |
| No. of reflections | 2288 | 1434 |
| No. of parameters | 112 | 107 |
| No. of restraints | 1 | 7 |
| Δρ _{max} , Δρ _{min} (e Å ⁻³) | 1.85, -1.63 | 2.57, -2.00 |

Computer programs: SMART and SAINT (Bruker, 1999), DENZO/SCALEPACK (Otwinowski & Minor, 1997), SHELXS and SHELXS97 (Sheldrick, 2008), SHELXL2018/3 (Sheldrick, 2015), ORTEP-3 for Windows (Farrugia, 2012), ATOMS (Dowty, 2005) and publCIF (Westrip, 2010).

The B layers in (I) (Fig. 5) lie at *z* ≈ 1/12, 1/4, 5/12, 7/12, 3/4 and 11/12 and are associated with the Zr1 and As2 species. These also feature polyhedral 12-rings (six octahedra and six tetrahedra) but only one As2 tetrahedron (with two terminal As2—O6 bonds) links adjacent Zr1 octahedra via atom O5. There are numerous sodium sites associated with the B layers. The disorder of the sodium ions in the vicinities of the B layers and possible small [110] channels (see Fig. 2) suggests the possibility of ionic conductivity (Norberg, 2002). An analysis of the stucture with PLATON (Spek, 2020) with the sodium ions removed indicated that there was 119.4 Å³ of free space per unit cell (~2.1%).

3. Database survey

A survey of the Inorganic Crystal Structure Database (ICSD) (Belsky *et al.*, 2002) revealed 11 matches for crystal structures containing Zr + As + O, the majority of these being Nasicon (Anantharamulu *et al.*, 2011) derivatives such as NaZr₂(AsO₄)₃ (Chakir *et al.*, 2003) or KZr₂(AsO₄)₃ (Elbrahimi & Durand, 1990) as well as one KTP analogue, *viz.* RbZrOAsO₄ (Simpson & Harrison, 2004). There were no hits for the combination of Hf + As + O.

4. Synthesis and crystallization

Compound (I) was prepared by mixing 1.00 g of Na₂CO₃, 0.581 g of ZrO₂ and 1.399 g of As₂O₅ (Na:Zr:As molar ratio ≈ 4:1:3) in an agate mortar: 1.00 g of this mixture was added to

3.0 g of a eutectic-melt mixture (*T*_{melt} ≈ 500°C) of NaCl/CsCl (~0.35:0.65 mol) and placed in a flat-bottom alumina crucible. The crucible was rapidly heated to 500°C in a muffle furnace and then ramped at 12°C min⁻¹ to 700°C and cooled at the same rate to 400°C and then removed from the furnace and left to cool. The gummy white product was washed with copious amounts of hot water followed by acetone to result in a mass of tiny colourless rods of (I). Compound (II) was made in the same way starting from a pre-mixture of 1.00 g Na₂CO₃, 1.12 g HfO₂ and 1.57 g As₂O₅ and tiny colourless rods of (II) were the result.

Caution! Arsenic compounds are highly toxic and carcinogenic. Take all appropriate safety precautions, especially with respect to dust contamination.

5. Refinement

Crystal data, data collection and structure refinement details are summarized in Table 1. The crystal chosen for data collection for (I) was found to be twinned over its rhombohedral obverse and reverse settings (Herbst-Irmer & Sheldrick, 2002) in a 0.797 (3):0.203 (3) ratio, which was processed as a SHELXL HKLF 5 refinement. To ensure charge balance, the occupancies of the four partially occupied sodium sites must sum to 10.0 Na per caesium ion and this was achieved by using a SUMP card (linear free variable restraint) in SHELXL, as unrestrained refinements tended to drift to a collective occupancy of above 10 (full occupancy of the four sodium sites would give 13 Na to 1 Cs). This needed cautious

damped refinement cycles to begin with, but as the refinement converged, the damping could be removed to give refined fractional site occupancies of Na1 = 0.852 (5), Na2 = 0.860 (9), Na3 = 0.731 (12) and Na4 = 0.423 (11) for (I) and Na1 = 0.887 (7), Na2 = 0.846 (11), Na3 = 0.735 (16) and Na4 = 0.337 (14) for (II). The final difference map for (II) features electron density peaks of $\sim 2 \text{ e Å}^{-3}$ near some of the sodium ions, perhaps suggesting that they are localizing over split multiple sites at low temperatures, but efforts to model this did not lead to satisfactory refinements. The value of U_{eq} for Na4 is small, which might indicate partial occupancy of caesium on this site (*i.e.*, a formula of $\text{Cs}_{1+x}\text{Na}_{10-x}\text{Hf}_4(\text{AsO}_4)_9$, but attempts to model this were inconclusive.

Acknowledgements

We thank the EPSRC National Crystallography Service (University of Southampton) for the X-ray data collection for (II).

References

- Abrahams, S. C. & Bernstein, J. L. (1966). *J. Chem. Phys.* **45**, 2745–2752.
- Adams, J. M., Haselden, D. A. & Hewat, A. W. (1982). *J. Solid State Chem.* **44**, 245–253.
- Anantharamulu, N., Koteswara Rao, K., Rambabu, G., Vijaya Kumar, B., Radha, V. & Vithal, M. (2011). *J. Mater. Sci.* **46**, 2821–2837.
- Belsky, A., Hellenbrandt, M., Karen, V. L. & Luksch, P. (2002). *Acta Cryst.* **B58**, 364–369.
- Blessing, R. H. (1995). *Acta Cryst.* **A51**, 33–38.
- Brese, N. E. & O'Keeffe, M. (1991). *Acta Cryst.* **B47**, 192–197.
- Bruker (1999). SMART, SAINT and SADABS. Bruker AXS Inc., Madison, Wisconsin, USA.
- Chakir, M., El Jazouli, A. & de Waal, A. (2003). *Mater. Res. Bull.* **38**, 1773–1779.
- Dowty, E. W. (2005). ATOMS. Shape Software, Kingsport, Tennessee, USA.
- Elbrahimi, M. & Durand, J. (1990). *Z. Anorg. Allg. Chem.* **584**, 178–184.
- Farrugia, L. J. (2012). *J. Appl. Cryst.* **45**, 849–854.
- Herbst-Irmer, R. & Sheldrick, G. M. (2002). *Acta Cryst.* **B58**, 477–481.
- Kores, C. C., Canalias, C. & Laurell, F. (2021). *APL Photonics*, **6**, article 091102.
- McGarey, P. O., Collins, A., Dominguez, L. M., Dion, G. R. & Simpson, G. B. (2021). *J. Voice*, **35**, 800–803.
- Müller-Buschbaum, H. K. (2010). *Z. Anorg. Allg. Chem.* **636**, 1667–1685.
- Norberg, S. T. (2002). *Acta Cryst.* **B58**, 743–749.
- Otwinowski, Z. & Minor, W. (1997). *Methods in Enzymology*, Vol. 276, *Macromolecular Crystallography*, Part A, edited by C. W. Carter Jr & R. M. Sweet, pp. 307–326. New York: Academic Press.
- Robinson, K., Gibbs, G. V. & Ribbe, P. H. (1971). *Science*, **172**, 567–570.
- Shannon, R. D. (1976). *Acta Cryst.* **A32**, 751–767.
- Sheldrick, G. M. (2008). *Acta Cryst.* **A64**, 112–122.
- Sheldrick, G. M. (2015). *Acta Cryst.* **C71**, 3–8.
- Shim, H.-K. & Kim, M. R. (2021). *Amer. J. Case Rep.* **22**, article e931042.
- Simpson, M. & Harrison, W. T. A. (2004). *Solid State Sci.* **6**, 981–985.
- Sorokina, N. I. & Voronkova, V. I. (2007). *Crystallogr. Rep.* **52**, 80–93.
- Spek, A. L. (2020). *Acta Cryst.* **E76**, 1–11.
- Stucky, G. D., Phillips, M. L. F. & Gier, T. E. (1989). *Chem. Mater.* **1**, 492–509.
- Westrip, S. P. (2010). *J. Appl. Cryst.* **43**, 920–925.
- Yang, L., Powell, D. R. & Houser, R. P. (2007). *Dalton Trans.* pp. 955–964.
- Zumsteg, F. C., Bierlein, J. D. & Gier, T. E. (1976). *J. Appl. Phys.* **47**, 4980–4985.

supporting information

Acta Cryst. (2022). E78, 737-741 [https://doi.org/10.1107/S2056989022006338]

Flux syntheses and single-crystal structures of $\text{CsNa}_{10}\text{M}_4(\text{AsO}_4)_9$ ($\text{M} = \text{Zr}, \text{Hf}$)

William T. A. Harrison

Computing details

Data collection: SMART (Bruker, 1999) for (I); DENZO/SCALEPACK (Otwinowski & Minor, 1997) for (II). Cell refinement: SAINT (Bruker, 1999) for (I); DENZO/SCALEPACK (Otwinowski & Minor, 1997) for (II). Data reduction: SAINT (Bruker, 1999) for (I); DENZO/SCALEPACK (Otwinowski & Minor, 1997) for (II). Program(s) used to solve structure: SHELXS (Sheldrick, 2008) for (I); SHELXS97 (Sheldrick, 2008) for (II). For both structures, program(s) used to refine structure: SHELXL2018/3 (Sheldrick, 2015); molecular graphics: ORTEP-3 for Windows (Farrugia, 2012) and ATOMS (Dowty, 2005); software used to prepare material for publication: SHELXL2018/3 (Sheldrick, 2015) and publCIF (Westrip, 2010).

Caesium decasodium tetrazirconium nonaarsenate (I)

Crystal data



$$M_r = 1977.97$$

Trigonal, $R\bar{3}c:H$

$$a = 9.2218 (5) \text{ \AA}$$

$$c = 76.982 (5) \text{ \AA}$$

$$V = 5669.6 (7) \text{ \AA}^3$$

$$Z = 6$$

$$F(000) = 5460$$

$$D_x = 3.476 \text{ Mg m}^{-3}$$

Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ \AA}$

Cell parameters from 2999 reflections

$$\theta = 2.6\text{--}30.8^\circ$$

$$\mu = 10.07 \text{ mm}^{-1}$$

$$T = 293 \text{ K}$$

Prism, colourless

$$0.10 \times 0.10 \times 0.10 \text{ mm}$$

Data collection

Bruker SMART CCD
diffractometer

ω scans

Absorption correction: multi-scan
(SADABS; Bruker, 1999)

$$T_{\min} = 0.350, T_{\max} = 0.495$$

2288 measured reflections

2288 independent reflections

1694 reflections with $I > 2\sigma(I)$

$$\theta_{\max} = 32.5^\circ, \theta_{\min} = 2.6^\circ$$

$$h = -12 \rightarrow 12$$

$$k = -13 \rightarrow 13$$

$$l = 0 \rightarrow 114$$

Refinement

Refinement on F^2

Least-squares matrix: full

$$R[F^2 > 2\sigma(F^2)] = 0.040$$

$$wR(F^2) = 0.093$$

$$S = 1.00$$

2288 reflections

112 parameters

1 restraint

Primary atom site location: structure-invariant
direct methods

$$w = 1/[\sigma^2(F_o^2) + (0.0452P)^2] \\ \text{where } P = (F_o^2 + 2F_c^2)/3$$

$$(\Delta/\sigma)_{\max} < 0.001$$

$$\Delta\rho_{\max} = 1.85 \text{ e \AA}^{-3}$$

$$\Delta\rho_{\min} = -1.63 \text{ e \AA}^{-3}$$

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Refinement. Refined as a 2-component obverse/reverse twin.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

| | <i>x</i> | <i>y</i> | <i>z</i> | $U_{\text{iso}}^*/U_{\text{eq}}$ | Occ. (<1) |
|-----|-------------|-------------|--------------|----------------------------------|------------|
| Cs1 | 0.000000 | 0.000000 | 0.000000 | 0.0381 (2) | |
| Na1 | 0.3350 (5) | 0.0681 (4) | 0.04049 (4) | 0.0410 (9) | 0.852 (5) |
| Na2 | 0.4054 (5) | 0.333333 | 0.083333 | 0.0411 (13) | 0.860 (9) |
| Na3 | 0.000000 | 0.000000 | 0.05355 (8) | 0.0321 (17) | 0.731 (12) |
| Na4 | 0.666667 | 0.333333 | 0.06014 (12) | 0.021 (2) | 0.423 (11) |
| Zr1 | 0.333333 | 0.666667 | 0.05681 (2) | 0.01237 (15) | |
| Zr2 | 0.333333 | 0.666667 | -0.00666 (2) | 0.01204 (15) | |
| As1 | 0.34556 (6) | 0.39774 (6) | 0.02640 (2) | 0.01350 (11) | |
| As2 | 0.666667 | 0.73010 (9) | 0.083333 | 0.0309 (2) | |
| O1 | 0.1757 (5) | 0.2319 (4) | 0.03370 (5) | 0.0251 (8) | |
| O2 | 0.3084 (5) | 0.4671 (5) | 0.00779 (5) | 0.0251 (8) | |
| O3 | 0.4373 (5) | 0.5591 (4) | 0.04062 (5) | 0.0192 (7) | |
| O4 | 0.4946 (5) | 0.3445 (5) | 0.02328 (5) | 0.0217 (8) | |
| O5 | 0.5457 (5) | 0.7825 (5) | 0.07152 (5) | 0.0234 (8) | |
| O6A | 0.603 (2) | 0.5691 (13) | 0.09411 (18) | 0.036 (5) | 0.45 (3) |
| O6B | 0.5238 (19) | 0.5873 (11) | 0.09900 (16) | 0.034 (4) | 0.55 (3) |

Atomic displacement parameters (\AA^2)

| | U^{11} | U^{22} | U^{33} | U^{12} | U^{13} | U^{23} |
|-----|-------------|-------------|-------------|--------------|--------------|--------------|
| Cs1 | 0.0436 (4) | 0.0436 (4) | 0.0271 (4) | 0.02182 (18) | 0.000 | 0.000 |
| Na1 | 0.072 (2) | 0.0286 (15) | 0.0375 (16) | 0.0369 (17) | -0.0102 (17) | -0.0033 (13) |
| Na2 | 0.0307 (18) | 0.0138 (18) | 0.073 (3) | 0.0069 (9) | -0.0044 (10) | -0.009 (2) |
| Na3 | 0.0216 (19) | 0.0216 (19) | 0.053 (4) | 0.0108 (9) | 0.000 | 0.000 |
| Na4 | 0.015 (3) | 0.015 (3) | 0.034 (5) | 0.0074 (14) | 0.000 | 0.000 |
| Zr1 | 0.0109 (2) | 0.0109 (2) | 0.0153 (3) | 0.00546 (10) | 0.000 | 0.000 |
| Zr2 | 0.0109 (2) | 0.0109 (2) | 0.0144 (3) | 0.00543 (10) | 0.000 | 0.000 |
| As1 | 0.0135 (2) | 0.0114 (2) | 0.0162 (2) | 0.00670 (18) | 0.00020 (18) | 0.00004 (18) |
| As2 | 0.0460 (5) | 0.0276 (3) | 0.0254 (4) | 0.0230 (3) | -0.0191 (4) | -0.0095 (2) |
| O1 | 0.0227 (19) | 0.0166 (17) | 0.029 (2) | 0.0041 (15) | 0.0059 (16) | 0.0051 (16) |
| O2 | 0.029 (2) | 0.0199 (18) | 0.0268 (19) | 0.0131 (17) | -0.0026 (17) | 0.0055 (16) |
| O3 | 0.0199 (17) | 0.0165 (16) | 0.0220 (17) | 0.0097 (14) | 0.0002 (15) | -0.0050 (15) |
| O4 | 0.0246 (19) | 0.0293 (19) | 0.0227 (18) | 0.0219 (17) | 0.0003 (15) | -0.0034 (17) |
| O5 | 0.0178 (17) | 0.028 (2) | 0.0252 (18) | 0.0123 (16) | -0.0095 (15) | -0.0076 (17) |
| O6A | 0.034 (8) | 0.024 (5) | 0.034 (6) | 0.001 (4) | -0.010 (6) | 0.003 (4) |
| O6B | 0.032 (7) | 0.021 (4) | 0.032 (5) | 0.000 (4) | -0.014 (5) | 0.004 (4) |

Geometric parameters (\AA , $^{\circ}$)

| | | | |
|--|-------------|--|-------------|
| Cs1—O1 ⁱ | 3.235 (4) | Na4—O6A ^{vi} | 2.694 (17) |
| Cs1—O1 ⁱⁱ | 3.235 (4) | Na4—O6A ^{xii} | 2.694 (17) |
| Cs1—O1 ⁱⁱⁱ | 3.235 (4) | Zr1—O5 | 2.041 (3) |
| Cs1—O1 | 3.235 (4) | Zr1—O5 ^{xiii} | 2.041 (3) |
| Cs1—O1 ^{iv} | 3.235 (4) | Zr1—O5 ^{ix} | 2.041 (3) |
| Cs1—O1 ^v | 3.235 (4) | Zr1—O3 ^{ix} | 2.099 (3) |
| Na1—O6B ^{vi} | 2.193 (9) | Zr1—O3 ^{xiii} | 2.099 (3) |
| Na1—O3 ^{vii} | 2.394 (5) | Zr1—O3 | 2.099 (3) |
| Na1—O1 ^v | 2.482 (5) | Zr2—O2 ^{xiii} | 2.062 (4) |
| Na1—O6A ^{vi} | 2.485 (16) | Zr2—O2 ^{ix} | 2.062 (4) |
| Na1—O4 | 2.582 (5) | Zr2—O2 | 2.062 (4) |
| Na1—O1 | 2.632 (5) | Zr2—O4 ^{xiv} | 2.081 (3) |
| Na2—O6A | 2.185 (10) | Zr2—O4 ^{iv} | 2.081 (3) |
| Na2—O6A ^{vi} | 2.185 (10) | Zr2—O4 ^{xv} | 2.081 (3) |
| Na2—O6B | 2.361 (12) | As1—O1 | 1.647 (4) |
| Na2—O6B ^{vi} | 2.361 (12) | As1—O2 | 1.673 (4) |
| Na2—O5 ^{viii} | 2.495 (5) | As1—O4 | 1.691 (3) |
| Na2—O5 ^{ix} | 2.495 (5) | As1—O3 | 1.694 (4) |
| Na3—O1 ⁱⁱ | 2.463 (5) | As2—O6A | 1.538 (10) |
| Na3—O1 | 2.463 (5) | As2—O6A ^{xii} | 1.538 (10) |
| Na3—O1 ^v | 2.463 (5) | As2—O5 ^{xii} | 1.686 (4) |
| Na3—O6B ^{viii} | 2.47 (2) | As2—O5 | 1.686 (4) |
| Na3—O6B ^x | 2.47 (2) | As2—O6B | 1.786 (13) |
| Na3—O6B ^{vi} | 2.47 (2) | As2—O6B ^{xii} | 1.786 (13) |
| Na4—O6A ^{xi} | 2.694 (17) | O6A—O6B | 0.909 (13) |
| | | | |
| O1 ⁱ —Cs1—O1 ⁱⁱ | 180.0 (3) | O5 ^{xiii} —Zr1—O3 ^{ix} | 87.67 (16) |
| O1 ⁱ —Cs1—O1 ⁱⁱⁱ | 62.30 (10) | O5 ^{ix} —Zr1—O3 ^{ix} | 91.79 (15) |
| O1 ⁱⁱ —Cs1—O1 ⁱⁱⁱ | 117.70 (10) | O5—Zr1—O3 ^{xiii} | 87.66 (16) |
| O1 ⁱ —Cs1—O1 | 117.70 (10) | O5 ^{xiii} —Zr1—O3 ^{xiii} | 91.79 (15) |
| O1 ⁱⁱ —Cs1—O1 | 62.30 (10) | O5 ^{ix} —Zr1—O3 ^{xiii} | 176.01 (15) |
| O1 ⁱⁱⁱ —Cs1—O1 | 180.00 (9) | O3 ^{ix} —Zr1—O3 ^{xiii} | 88.35 (14) |
| O1 ⁱ —Cs1—O1 ^{iv} | 62.30 (10) | O5—Zr1—O3 | 91.79 (15) |
| O1 ⁱⁱ —Cs1—O1 ^{iv} | 117.70 (10) | O5 ^{xiii} —Zr1—O3 | 176.01 (15) |
| O1 ⁱⁱⁱ —Cs1—O1 ^{iv} | 62.30 (10) | O5 ^{ix} —Zr1—O3 | 87.67 (16) |
| O1—Cs1—O1 ^{iv} | 117.70 (10) | O3 ^{ix} —Zr1—O3 | 88.35 (14) |
| O1 ⁱ —Cs1—O1 ^v | 117.70 (10) | O3 ^{xiii} —Zr1—O3 | 88.35 (14) |
| O1 ⁱⁱ —Cs1—O1 ^v | 62.30 (10) | O2 ^{xiii} —Zr2—O2 ^{ix} | 93.66 (15) |
| O1 ⁱⁱⁱ —Cs1—O1 ^v | 117.70 (10) | O2 ^{xiii} —Zr2—O2 | 93.66 (15) |
| O1—Cs1—O1 ^v | 62.30 (10) | O2 ^{ix} —Zr2—O2 | 93.66 (15) |
| O1 ^{iv} —Cs1—O1 ^v | 180.00 (16) | O2 ^{xiii} —Zr2—O4 ^{xiv} | 92.00 (16) |
| O6B ^{vi} —Na1—O3 ^{vii} | 104.6 (4) | O2 ^{ix} —Zr2—O4 ^{iv} | 88.01 (15) |
| O6B ^{vi} —Na1—O1 ^v | 93.4 (5) | O2—Zr2—O4 ^{xiv} | 173.98 (15) |
| O3 ^{vii} —Na1—O1 ^v | 87.41 (15) | O2 ^{xiii} —Zr2—O4 ^{iv} | 173.98 (15) |
| O6B ^{vi} —Na1—O6A ^{vi} | 21.3 (3) | O2 ^{ix} —Zr2—O4 ^{iv} | 92.00 (16) |
| O3 ^{vii} —Na1—O6A ^{vi} | 90.3 (4) | O2—Zr2—O4 ^{iv} | 88.01 (15) |

| | | | |
|--|-------------|--|-------------|
| O1 ^v —Na1—O6A ^{vi} | 108.7 (4) | O4 ^{xiv} —Zr2—O4 ^{iv} | 86.15 (14) |
| O6B ^{vi} —Na1—O4 | 118.5 (3) | O2 ^{xiii} —Zr2—O4 ^{xv} | 88.01 (15) |
| O3 ^{vii} —Na1—O4 | 119.01 (18) | O2 ^{ix} —Zr2—O4 ^{xv} | 173.98 (15) |
| O1 ^v —Na1—O4 | 127.39 (17) | O2—Zr2—O4 ^{xv} | 92.01 (16) |
| O6A ^{vi} —Na1—O4 | 115.1 (3) | O4 ^{xiv} —Zr2—O4 ^{xv} | 86.15 (14) |
| O6B ^{vi} —Na1—O1 | 85.3 (5) | O4 ^{iv} —Zr2—O4 ^{xv} | 86.15 (14) |
| O3 ^{vii} —Na1—O1 | 165.74 (19) | O1—As1—O2 | 111.5 (2) |
| O1 ^v —Na1—O1 | 81.68 (19) | O1—As1—O4 | 108.17 (19) |
| O6A ^{vi} —Na1—O1 | 101.8 (5) | O2—As1—O4 | 109.94 (19) |
| O4—Na1—O1 | 62.47 (13) | O1—As1—O3 | 114.88 (19) |
| O6B ^{vi} —Na1—O4 ^{vii} | 132.4 (6) | O2—As1—O3 | 108.98 (18) |
| O3 ^{vii} —Na1—O4 ^{vii} | 58.02 (13) | O6A—As2—O6A ^{xii} | 78.4 (18) |
| O1 ^v —Na1—O4 ^{vii} | 125.80 (15) | O6A—As2—O5 ^{xii} | 112.1 (4) |
| O6A ^{vi} —Na1—O4 ^{vii} | 111.4 (6) | O6A ^{xii} —As2—O5 ^{xii} | 125.4 (7) |
| O4—Na1—O4 ^{vii} | 61.11 (16) | O6A—As2—O5 | 125.4 (7) |
| O1—Na1—O4 ^{vii} | 122.35 (15) | O6A ^{xii} —As2—O5 | 112.1 (4) |
| O6A—Na2—O6A ^{vi} | 140.7 (13) | O5 ^{xii} —As2—O5 | 103.8 (3) |
| O6A—Na2—O6B | 22.7 (4) | O6A—As2—O6B | 30.6 (6) |
| O6A ^{vi} —Na2—O6B | 161.0 (11) | O6A ^{xii} —As2—O6B | 106.8 (15) |
| O6A—Na2—O6B ^{vi} | 161.0 (11) | O5 ^{xii} —As2—O6B | 103.3 (4) |
| O6A ^{vi} —Na2—O6B ^{vi} | 22.7 (4) | O5—As2—O6B | 103.1 (5) |
| O6B—Na2—O6B ^{vi} | 176.2 (9) | O6A—As2—O6B ^{xii} | 106.8 (15) |
| O6A—Na2—O5 ^{viii} | 118.7 (7) | O6A ^{xii} —As2—O6B ^{xii} | 30.6 (6) |
| O6A ^{vi} —Na2—O5 ^{viii} | 95.2 (5) | O5 ^{xii} —As2—O6B ^{xii} | 103.0 (5) |
| O6B—Na2—O5 ^{viii} | 96.8 (5) | O5—As2—O6B ^{xii} | 103.2 (4) |
| O6B ^{vi} —Na2—O5 ^{viii} | 79.9 (4) | O6B—As2—O6B ^{xii} | 136.7 (12) |
| O6A—Na2—O5 ^{ix} | 95.2 (5) | As1—O1—Na3 | 157.7 (2) |
| O6A ^{vi} —Na2—O5 ^{ix} | 118.7 (7) | As1—O1—Na1 ⁱⁱ | 117.0 (2) |
| O6B—Na2—O5 ^{ix} | 79.9 (4) | Na3—O1—Na1 ⁱⁱ | 74.73 (13) |
| O6B ^{vi} —Na2—O5 ^{ix} | 96.8 (5) | Na1 ⁱⁱ —O1—Na1 | 93.24 (18) |
| O5 ^{viii} —Na2—O5 ^{ix} | 64.2 (2) | As1—O1—Cs1 | 72.10 (12) |
| O6A—Na2—O6A ^{vii} | 113.6 (6) | Na3—O1—Cs1 | 146.6 (2) |
| O6A ^{vi} —Na2—O6A ^{vii} | 40.3 (6) | Na1 ⁱⁱ —O1—Cs1 | 105.65 (17) |
| O6B—Na2—O6A ^{vii} | 124.1 (3) | As1—O1—Cs1 | 91.66 (16) |
| O6B ^{vi} —Na2—O6A ^{vii} | 58.3 (4) | Na1 ⁱⁱ —O1—Cs1 | 93.89 (14) |
| O5 ^{viii} —Na2—O6A ^{vii} | 92.7 (2) | Na1—O1—Cs1 | 91.09 (13) |
| O5 ^{ix} —Na2—O6A ^{vii} | 149.8 (3) | As1—O2—Zr2 | 148.2 (2) |
| O6A—Na2—O6A ^{xii} | 40.3 (6) | As1—O3—Zr1 | 130.8 (2) |
| O6A ^{vi} —Na2—O6A ^{xii} | 113.6 (6) | As1—O3—Na1 ^{xvi} | 108.79 (18) |
| O6B—Na2—O6A ^{xii} | 58.3 (5) | Zr1—O3—Na1 ^{xvi} | 120.42 (18) |
| O6B ^{vi} —Na2—O6A ^{xii} | 124.1 (3) | As1—O4—Zr2 ^{xv} | 148.4 (2) |
| O5 ^{viii} —Na2—O6A ^{xii} | 149.8 (2) | As1—O4—Na1 | 93.97 (17) |
| O5 ^{ix} —Na2—O6A ^{xii} | 92.7 (2) | Zr2 ^{xv} —O4—Na1 | 109.81 (17) |
| O6A ^{vii} —Na2—O6A ^{xii} | 114.9 (5) | As1—O4—Na1 ^{xvi} | 87.30 (16) |
| O1 ⁱⁱ —Na3—O1 | 85.6 (2) | Zr2 ^{xv} —O4—Na1 ^{xvi} | 96.88 (15) |
| O1 ⁱⁱ —Na3—O1 ^v | 85.6 (2) | Na1—O4—Na1 ^{xvi} | 121.76 (18) |
| O1—Na3—O1 ^v | 85.6 (2) | As2—O5—Zr1 | 138.4 (2) |
| O1 ⁱⁱ —Na3—O6B ^{viii} | 83.5 (2) | | |

| | | | |
|--|-------------|--|-------------|
| O1—Na3—O6B ^{viii} | 87.5 (2) | As2—O5—Na2 ^{xiii} | 95.98 (16) |
| O1 ^v —Na3—O6B ^{viii} | 167.5 (3) | Zr1—O5—Na2 ^{xiii} | 124.11 (18) |
| O1 ⁱⁱ —Na3—O6B ^x | 87.5 (2) | As2—O6A—Na2 | 118.8 (6) |
| O1—Na3—O6B ^x | 167.5 (3) | As2—O6A—Na1 ^{vi} | 116.7 (8) |
| O1 ^v —Na3—O6B ^x | 83.5 (2) | Na2—O6A—Na1 ^{vi} | 115.9 (6) |
| O6B ^{viii} —Na3—O6B ^x | 102.1 (3) | As2—O6A—Na4 ^{xi} | 147.0 (14) |
| O1 ⁱⁱ —Na3—O6B ^{vi} | 167.5 (3) | Na2—O6A—Na4 ^{xi} | 75.0 (4) |
| O1—Na3—O6B ^{vi} | 83.5 (2) | Na1 ^{vi} —O6A—Na4 ^{xi} | 75.8 (3) |
| O1 ^v —Na3—O6B ^{vi} | 87.5 (2) | As2—O6A—Na2 ^{xvi} | 83.8 (9) |
| O6B ^{viii} —Na3—O6B ^{vi} | 102.1 (3) | Na2—O6A—Na2 ^{xvi} | 106.0 (9) |
| O6B ^x —Na3—O6B ^{vi} | 102.1 (3) | Na1 ^{vi} —O6A—Na2 ^{xvi} | 109.3 (5) |
| O6A ^{xi} —Na4—O6A ^{vi} | 108.1 (5) | Na4 ^{xi} —O6A—Na2 ^{xvi} | 63.2 (5) |
| O6A ^{xi} —Na4—O6A ^{xii} | 108.1 (5) | As2—O6B—Na1 ^{vi} | 120.5 (5) |
| O6A ^{vi} —Na4—O6A ^{xii} | 108.1 (5) | As2—O6B—Na2 | 101.0 (7) |
| O5—Zr1—O5 ^{xii} | 92.21 (16) | Na1 ^{vi} —O6B—Na2 | 120.8 (4) |
| O5—Zr1—O5 ^{ix} | 92.21 (16) | As2—O6B—Na3 ^{xvii} | 116.8 (7) |
| O5 ^{xiii} —Zr1—O5 ^{ix} | 92.20 (16) | Na1 ^{vi} —O6B—Na3 ^{xvii} | 79.9 (6) |
| O5—Zr1—O3 ^{ix} | 176.01 (15) | Na2—O6B—Na3 ^{xvii} | 118.3 (6) |

Symmetry codes: (i) $y, -x+y, -z$; (ii) $-y, x-y, z$; (iii) $-x, -y, -z$; (iv) $x-y, x, -z$; (v) $-x+y, -x, z$; (vi) $x-y+1/3, -y+2/3, -z+1/6$; (vii) $-y+1, x-y, z$; (viii) $y-2/3, x-1/3, -z+1/6$; (ix) $-x+y, -x+1, z$; (x) $-x+1/3, -x+y-1/3, -z+1/6$; (xi) $y+1/3, x-1/3, -z+1/6$; (xii) $-x+4/3, -x+y+2/3, -z+1/6$; (xiii) $-y+1, x-y+1, z$; (xiv) $y, -x+y+1, -z$; (xv) $-x+1, -y+1, -z$; (xvi) $-x+y+1, -x+1, z$; (xvii) $y+1/3, x+2/3, -z+1/6$.

Caesium decasodium tetrahafnium nonaarsenate (II)

Crystal data


 $M_r = 2327.05$

Trigonal, $R\bar{3}c:H$
 $a = 9.1795 (2) \text{ \AA}$
 $c = 76.527 (8) \text{ \AA}$
 $V = 5584.5 (6) \text{ \AA}^3$
 $Z = 6$
 $F(000) = 6228$
 $D_x = 4.152 \text{ Mg m}^{-3}$

Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ \AA}$

Cell parameters from 22894 reflections

 $\theta = 2.9\text{--}27.5^\circ$
 $\mu = 20.25 \text{ mm}^{-1}$
 $T = 120 \text{ K}$

Prism, colourless

 $0.08 \times 0.08 \times 0.08 \text{ mm}$

Data collection

Nonius KappaCCD
diffractometer

 ω scans

Absorption correction: multi-scan
(SORTAV; Blessing, 1995)

 $T_{\min} = 0.40, T_{\max} = 0.50$

11660 measured reflections

1434 independent reflections

1164 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.070$
 $\theta_{\max} = 27.5^\circ, \theta_{\min} = 3.2^\circ$
 $h = -11 \rightarrow 11$
 $k = -11 \rightarrow 11$
 $l = -99 \rightarrow 99$

Refinement

Refinement on F^2

Least-squares matrix: full

 $R[F^2 > 2\sigma(F^2)] = 0.032$
 $wR(F^2) = 0.078$
 $S = 1.06$

1434 reflections

107 parameters

7 restraints

Primary atom site location: structure-invariant
direct methods

$w = 1/[\sigma^2(F_o^2) + (0.0359P)^2 + 136.7342P]$
 $\text{where } P = (F_o^2 + 2F_c^2)/3$

$(\Delta/\sigma)_{\max} = 0.008$

$\Delta\rho_{\max} = 2.57 \text{ e \AA}^{-3}$

$\Delta\rho_{\min} = -2.00 \text{ e \AA}^{-3}$

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

| | <i>x</i> | <i>y</i> | <i>z</i> | $U_{\text{iso}}^*/U_{\text{eq}}$ | Occ. (<1) |
|-----|-------------|--------------|--------------|----------------------------------|------------|
| Cs1 | 0.000000 | 0.000000 | 0.000000 | 0.0162 (3) | |
| Na1 | 0.3354 (5) | 0.0688 (5) | 0.04043 (5) | 0.0256 (11) | 0.887 (7) |
| Na2 | 0.4061 (6) | 0.333333 | 0.083333 | 0.0208 (15)* | 0.846 (11) |
| Na3 | 0.000000 | 0.000000 | 0.05288 (11) | 0.018 (2) | 0.735 (16) |
| Na4 | 0.666667 | 0.333333 | 0.06123 (16) | 0.002 (4)* | 0.337 (14) |
| Hf1 | 0.333333 | 0.666667 | 0.05673 (2) | 0.00710 (15) | |
| Hf2 | 0.333333 | 0.666667 | -0.00682 (2) | 0.00611 (15) | |
| As1 | 0.34520 (9) | 0.39770 (9) | 0.02639 (2) | 0.00578 (18) | |
| As2 | 0.666667 | 0.73244 (13) | 0.083333 | 0.0205 (3) | |
| O1 | 0.1730 (6) | 0.2332 (6) | 0.03369 (6) | 0.0113 (11) | |
| O2 | 0.3086 (6) | 0.4663 (6) | 0.00745 (6) | 0.0109 (11) | |
| O3 | 0.4389 (6) | 0.5622 (6) | 0.04043 (6) | 0.0068 (10) | |
| O4 | 0.4922 (6) | 0.3405 (6) | 0.02356 (6) | 0.0097 (11) | |
| O5 | 0.5461 (6) | 0.7864 (6) | 0.07152 (6) | 0.0127 (11) | |
| O6A | 0.602 (2) | 0.569 (2) | 0.0942 (2) | 0.008 (2) | 0.35 (2) |
| O6B | 0.5276 (16) | 0.5861 (12) | 0.09848 (14) | 0.029 (4) | 0.65 (2) |

Atomic displacement parameters (\AA^2)

| | U^{11} | U^{22} | U^{33} | U^{12} | U^{13} | U^{23} |
|-----|--------------|--------------|------------|-------------|--------------|--------------|
| Cs1 | 0.0181 (4) | 0.0181 (4) | 0.0125 (5) | 0.0091 (2) | 0.000 | 0.000 |
| Na1 | 0.049 (3) | 0.014 (2) | 0.023 (2) | 0.023 (2) | -0.0094 (18) | -0.0012 (16) |
| Na3 | 0.002 (3) | 0.002 (3) | 0.049 (5) | 0.0012 (13) | 0.000 | 0.000 |
| Hf1 | 0.00580 (19) | 0.00580 (19) | 0.0097 (3) | 0.00290 (9) | 0.000 | 0.000 |
| Hf2 | 0.00499 (19) | 0.00499 (19) | 0.0084 (3) | 0.00250 (9) | 0.000 | 0.000 |
| As1 | 0.0056 (4) | 0.0037 (4) | 0.0086 (3) | 0.0027 (3) | 0.0002 (3) | 0.0002 (3) |
| As2 | 0.0312 (7) | 0.0178 (4) | 0.0170 (6) | 0.0156 (4) | -0.0165 (5) | -0.0083 (3) |
| O1 | 0.007 (3) | 0.007 (3) | 0.015 (3) | 0.000 (2) | 0.001 (2) | 0.001 (2) |
| O2 | 0.015 (3) | 0.009 (3) | 0.011 (2) | 0.007 (2) | -0.003 (2) | 0.000 (2) |
| O3 | 0.005 (2) | 0.005 (2) | 0.011 (2) | 0.003 (2) | -0.0006 (19) | -0.0054 (19) |
| O4 | 0.010 (3) | 0.013 (3) | 0.010 (2) | 0.010 (2) | 0.002 (2) | 0.000 (2) |
| O5 | 0.007 (3) | 0.017 (3) | 0.012 (2) | 0.004 (2) | -0.006 (2) | -0.006 (2) |
| O6A | 0.008 (2) | 0.008 (2) | 0.008 (2) | 0.0042 (11) | 0.00000 (10) | 0.00000 (10) |
| O6B | 0.030 (7) | 0.021 (5) | 0.022 (5) | 0.003 (5) | -0.014 (5) | 0.002 (4) |

Geometric parameters (\AA , $^\circ$)

| | | | |
|---------------------|-----------|------------------------|------------|
| Cs1—O1 | 3.218 (5) | Na4—O6A ^{vi} | 2.654 (18) |
| Cs1—O1 ⁱ | 3.218 (5) | Na4—O6A ^{xii} | 2.654 (18) |

| | | | |
|--|-------------|---|-------------|
| Cs1—O1 ⁱⁱ | 3.218 (5) | Hf1—O5 ^{xiii} | 2.039 (5) |
| Cs1—O1 ⁱⁱⁱ | 3.218 (5) | Hf1—O5 ^{ix} | 2.039 (5) |
| Cs1—O1 ^{iv} | 3.218 (5) | Hf1—O5 | 2.039 (5) |
| Cs1—O1 ^v | 3.218 (5) | Hf1—O3 ^{ix} | 2.084 (4) |
| Na1—O6B ^{vi} | 2.212 (10) | Hf1—O3 ^{xiii} | 2.084 (4) |
| Na1—O3 ^{vii} | 2.377 (6) | Hf1—O3 | 2.084 (4) |
| Na1—O1 ⁱⁱⁱ | 2.443 (6) | Hf2—O2 | 2.051 (5) |
| Na1—O6A ^{vi} | 2.467 (17) | Hf2—O2 ^{ix} | 2.052 (5) |
| Na1—O4 | 2.524 (6) | Hf2—O2 ^{xiii} | 2.052 (5) |
| Na1—O1 | 2.649 (6) | Hf2—O4 ^{xiv} | 2.077 (5) |
| Na1—O4 ^{vii} | 2.972 (6) | Hf2—O4 ⁱⁱ | 2.077 (5) |
| Na2—O6A | 2.170 (16) | Hf2—O4 ^{xv} | 2.077 (5) |
| Na2—O6A ^{vi} | 2.170 (16) | As1—O1 | 1.644 (5) |
| Na2—O6B | 2.320 (10) | As1—O2 | 1.680 (5) |
| Na2—O6B ^{vi} | 2.320 (10) | As1—O4 | 1.689 (5) |
| Na2—O5 ^{viii} | 2.458 (7) | As1—O3 | 1.696 (4) |
| Na2—O5 ^{ix} | 2.458 (7) | As2—O6A | 1.552 (15) |
| Na3—O1 ^v | 2.421 (7) | As2—O6A ^{xi} | 1.552 (15) |
| Na3—O1 ⁱⁱⁱ | 2.421 (7) | As2—O5 | 1.684 (5) |
| Na3—O1 | 2.421 (7) | As2—O5 ^{xi} | 1.684 (5) |
| Na3—O6B ^{viii} | 2.534 (17) | As2—O6B | 1.750 (11) |
| Na3—O6B ^x | 2.534 (17) | As2—O6B ^{xi} | 1.750 (11) |
| Na3—O6B ^{vi} | 2.534 (17) | O6A—O6B | 0.842 (15) |
| Na4—O6A ^{xi} | 2.654 (18) | | |
| O1—Cs1—O1 ⁱ | 180.00 (19) | O5 ^{ix} —Hf1—O3 | 87.7 (2) |
| O1—Cs1—O1 ⁱⁱ | 117.59 (14) | O5—Hf1—O3 | 92.3 (2) |
| O1 ⁱ —Cs1—O1 ⁱⁱ | 62.41 (14) | O3 ^{ix} —Hf1—O3 | 87.88 (18) |
| O1—Cs1—O1 ⁱⁱⁱ | 62.41 (14) | O3 ^{xiii} —Hf1—O3 | 87.88 (18) |
| O1 ⁱ —Cs1—O1 ⁱⁱⁱ | 117.59 (14) | O2—Hf2—O2 ^{ix} | 94.29 (18) |
| O1 ⁱⁱ —Cs1—O1 ⁱⁱⁱ | 180.00 (19) | O2—Hf2—O2 ^{xiii} | 94.29 (18) |
| O1—Cs1—O1 ^{iv} | 117.59 (14) | O2 ^{ix} —Hf2—O2 ^{xiii} | 94.28 (18) |
| O1 ⁱ —Cs1—O1 ^{iv} | 62.41 (14) | O2—Hf2—O4 ^{xiv} | 92.38 (19) |
| O1 ⁱⁱ —Cs1—O1 ^{iv} | 62.41 (14) | O2 ^{ix} —Hf2—O4 ^{xiv} | 173.05 (19) |
| O1 ⁱⁱⁱ —Cs1—O1 ^{iv} | 117.59 (14) | O2 ^{xiii} —Hf2—O4 ^{xiv} | 87.19 (19) |
| O1—Cs1—O1 ^v | 62.41 (14) | O2—Hf2—O4 ⁱⁱ | 87.18 (19) |
| O1 ⁱ —Cs1—O1 ^v | 117.59 (14) | O2 ^{ix} —Hf2—O4 ⁱⁱ | 92.38 (19) |
| O1 ⁱⁱ —Cs1—O1 ^v | 117.59 (14) | O2 ^{xiii} —Hf2—O4 ⁱⁱ | 173.05 (19) |
| O1 ⁱⁱⁱ —Cs1—O1 ^v | 62.41 (14) | O4 ^{xiv} —Hf2—O4 ⁱⁱ | 85.96 (19) |
| O1 ^{iv} —Cs1—O1 ^v | 180.0 (3) | O2—Hf2—O4 ^{xv} | 173.04 (19) |
| O6B ^{vi} —Na1—O3 ^{vii} | 103.8 (4) | O2 ^{ix} —Hf2—O4 ^{xv} | 87.18 (19) |
| O6B ^{vi} —Na1—O1 ⁱⁱⁱ | 94.4 (4) | O2 ^{xiii} —Hf2—O4 ^{xv} | 92.38 (19) |
| O3 ^{vii} —Na1—O1 ⁱⁱⁱ | 86.5 (2) | O4 ^{xiv} —Hf2—O4 ^{xv} | 85.96 (19) |
| O6B ^{vi} —Na1—O6A ^{vi} | 19.8 (4) | O4 ⁱⁱ —Hf2—O4 ^{xv} | 85.96 (19) |
| O3 ^{vii} —Na1—O6A ^{vi} | 90.7 (5) | O1—As1—O2 | 110.9 (3) |
| O1 ⁱⁱⁱ —Na1—O6A ^{vi} | 108.7 (5) | O1—As1—O4 | 108.0 (2) |
| O6B ^{vi} —Na1—O4 | 118.4 (3) | O2—As1—O4 | 110.3 (2) |
| O3 ^{vii} —Na1—O4 | 119.4 (2) | O1—As1—O3 | 115.4 (2) |

| | | | |
|--|-------------|---|------------|
| O1 ⁱⁱⁱ —Na1—O4 | 127.6 (2) | O2—As1—O3 | 108.7 (2) |
| O6A ^{vi} —Na1—O4 | 115.0 (4) | O4—As1—O3 | 103.3 (2) |
| O6B ^{vi} —Na1—O1 | 86.1 (4) | O6A—As2—O6A ^{xi} | 78.0 (15) |
| O3 ^{vii} —Na1—O1 | 165.2 (2) | O6A—As2—O5 | 125.7 (7) |
| O1 ⁱⁱⁱ —Na1—O1 | 81.7 (2) | O6A ^{xi} —As2—O5 | 112.6 (6) |
| O6A ^{vi} —Na1—O1 | 101.5 (5) | O6A—As2—O5 ^{xi} | 112.6 (6) |
| O4—Na1—O1 | 62.78 (17) | O6A ^{xi} —As2—O5 ^{xi} | 125.7 (7) |
| O6B ^{vi} —Na1—O4 ^{vii} | 130.4 (5) | O5—As2—O5 ^{xi} | 103.0 (3) |
| O3 ^{vii} —Na1—O4 ^{vii} | 58.22 (16) | O6A—As2—O6B | 28.8 (6) |
| O1 ⁱⁱⁱ —Na1—O4 ^{vii} | 126.1 (2) | O6A ^{xi} —As2—O6B | 104.5 (12) |
| O6A ^{vi} —Na1—O4 ^{vii} | 110.9 (5) | O5—As2—O6B | 104.3 (5) |
| O4—Na1—O4 ^{vii} | 61.4 (2) | O5 ^{xi} —As2—O6B | 104.8 (4) |
| O1—Na1—O4 ^{vii} | 123.09 (19) | O6A—As2—O6B ^{xi} | 104.5 (12) |
| O6A—Na2—O6A ^{vi} | 141.3 (12) | O6A ^{xi} —As2—O6B ^{xi} | 28.8 (6) |
| O6A—Na2—O6B | 21.3 (4) | O5—As2—O6B ^{xi} | 104.8 (4) |
| O6A ^{vi} —Na2—O6B | 160.8 (9) | O5 ^{xi} —As2—O6B ^{xi} | 104.3 (5) |
| O6A—Na2—O6B ^{vi} | 160.8 (9) | O6B—As2—O6B ^{xi} | 132.5 (10) |
| O6A ^{vi} —Na2—O6B ^{vi} | 21.3 (4) | As1—O1—Na3 | 157.3 (3) |
| O6B—Na2—O6B ^{vi} | 177.8 (8) | As1—O1—Na1 ^v | 118.2 (3) |
| O6A—Na2—O5 ^{viii} | 118.4 (6) | Na3—O1—Na1 ^v | 75.36 (17) |
| O6A ^{vi} —Na2—O5 ^{viii} | 94.8 (5) | As1—O1—Na1 | 91.9 (2) |
| O6B—Na2—O5 ^{viii} | 97.9 (4) | Na3—O1—Na1 | 71.66 (16) |
| O6B ^{vi} —Na2—O5 ^{viii} | 80.2 (3) | Na1 ^v —O1—Na1 | 146.7 (3) |
| O6A—Na2—O5 ^{ix} | 94.8 (5) | As1—O1—Cs1 | 105.5 (2) |
| O6A ^{vi} —Na2—O5 ^{ix} | 118.4 (6) | Na3—O1—Cs1 | 90.6 (2) |
| O6B—Na2—O5 ^{ix} | 80.2 (3) | Na1 ^v —O1—Cs1 | 94.33 (17) |
| O6B ^{vi} —Na2—O5 ^{ix} | 97.9 (4) | Na1—O1—Cs1 | 90.47 (16) |
| O5 ^{viii} —Na2—O5 ^{ix} | 64.8 (3) | As1—O2—Hf2 | 147.4 (3) |
| O1 ^v —Na3—O1 ⁱⁱⁱ | 87.0 (3) | As1—O3—Hf1 | 130.0 (3) |
| O1 ^v —Na3—O1 | 87.0 (3) | As1—O3—Na1 ^{xvi} | 108.8 (2) |
| O1 ⁱⁱⁱ —Na3—O1 | 87.0 (3) | Hf1—O3—Na1 ^{xvi} | 121.1 (2) |
| O1 ^v —Na3—O6B ^{viii} | 84.6 (2) | As1—O4—Hf2 ^{xiv} | 146.9 (3) |
| O1 ⁱⁱⁱ —Na3—O6B ^{viii} | 170.0 (4) | As1—O4—Na1 | 95.3 (2) |
| O1—Na3—O6B ^{viii} | 87.2 (2) | Hf2 ^{xiv} —O4—Na1 | 110.6 (2) |
| O1 ^v —Na3—O6B ^x | 87.2 (2) | As1—O4—Na1 ^{xvi} | 86.8 (2) |
| O1 ⁱⁱⁱ —Na3—O6B ^x | 84.5 (2) | Hf2 ^{xiv} —O4—Na1 ^{xvi} | 95.70 (19) |
| O1—Na3—O6B ^x | 170.0 (4) | Na1—O4—Na1 ^{xvi} | 122.6 (2) |
| O6B ^{viii} —Na3—O6B ^x | 100.3 (3) | As2—O5—Hf1 | 137.1 (3) |
| O1 ^v —Na3—O6B ^{vi} | 170.0 (4) | As2—O5—Na2 ^{xiii} | 96.1 (2) |
| O1 ⁱⁱⁱ —Na3—O6B ^{vi} | 87.2 (2) | Hf1—O5—Na2 ^{xiii} | 125.3 (2) |
| O1—Na3—O6B ^{vi} | 84.6 (2) | As2—O6A—Na2 | 119.0 (8) |
| O6B ^{viii} —Na3—O6B ^{vi} | 100.3 (3) | As2—O6A—Na1 ^{vi} | 116.5 (9) |
| O6B ^x —Na3—O6B ^{vi} | 100.3 (3) | Na2—O6A—Na1 ^{vi} | 116.2 (7) |
| O6A ^{xi} —Na4—O6A ^{vi} | 110.0 (4) | As2—O6A—Na4 ^{xii} | 146.0 (12) |
| O6A ^{xi} —Na4—O6A ^{xii} | 110.0 (4) | Na2—O6A—Na4 ^{xii} | 74.0 (5) |
| O6A ^{vi} —Na4—O6A ^{xii} | 110.0 (4) | Na1 ^{vi} —O6A—Na4 ^{xii} | 77.5 (5) |
| O5 ^{xiii} —Hf1—O5 ^{ix} | 92.17 (19) | As2—O6A—Na2 ^{xvi} | 83.9 (8) |
| O5 ^{xiii} —Hf1—O5 | 92.17 (19) | Na2—O6A—Na2 ^{xvi} | 105.6 (8) |

| | | | |
|--|-------------|--|-----------|
| O5 ^{ix} —Hf1—O5 | 92.17 (19) | Na1 ^{vi} —O6A—Na2 ^{xvi} | 109.2 (6) |
| O5 ^{xiii} —Hf1—O3 ^{ix} | 87.7 (2) | Na4 ^{xii} —O6A—Na2 ^{xvi} | 62.2 (5) |
| O5 ^{ix} —Hf1—O3 ^{ix} | 92.3 (2) | As2—O6B—Na1 ^{vi} | 120.8 (5) |
| O5—Hf1—O3 ^{ix} | 175.57 (19) | As2—O6B—Na2 | 103.8 (6) |
| O5 ^{xiii} —Hf1—O3 ^{xiii} | 92.3 (2) | Na1 ^{vi} —O6B—Na2 | 120.7 (4) |
| O5 ^{ix} —Hf1—O3 ^{xiii} | 175.56 (19) | As2—O6B—Na3 ^{xvii} | 115.6 (6) |
| O5—Hf1—O3 ^{xiii} | 87.7 (2) | Na1 ^{vi} —O6B—Na3 ^{xvii} | 77.3 (5) |
| O3 ^{ix} —Hf1—O3 ^{xiii} | 87.89 (18) | Na2—O6B—Na3 ^{xvii} | 117.8 (5) |
| O5 ^{xiii} —Hf1—O3 | 175.56 (19) | | |

Symmetry codes: (i) $-x, -y, -z$; (ii) $x-y, x, -z$; (iii) $-x+y, -x, z$; (iv) $y, -x+y, -z$; (v) $-y, x-y, z$; (vi) $x-y+1/3, -y+2/3, -z+1/6$; (vii) $-y+1, x-y, z$; (viii) $y-2/3, x-1/3, -z+1/6$; (ix) $-x+y, -x+1, z$; (x) $-x+1/3, -x+y-1/3, -z+1/6$; (xi) $-x+4/3, -x+y+2/3, -z+1/6$; (xii) $y+1/3, x-1/3, -z+1/6$; (xiii) $-y+1, x-y+1, z$; (xiv) $-x+1, -y+1, -z$; (xv) $y, -x+y+1, -z$; (xvi) $-x+y+1, -x+1, z$; (xvii) $y+1/3, x+2/3, -z+1/6$.